



General Camera Calibration Models

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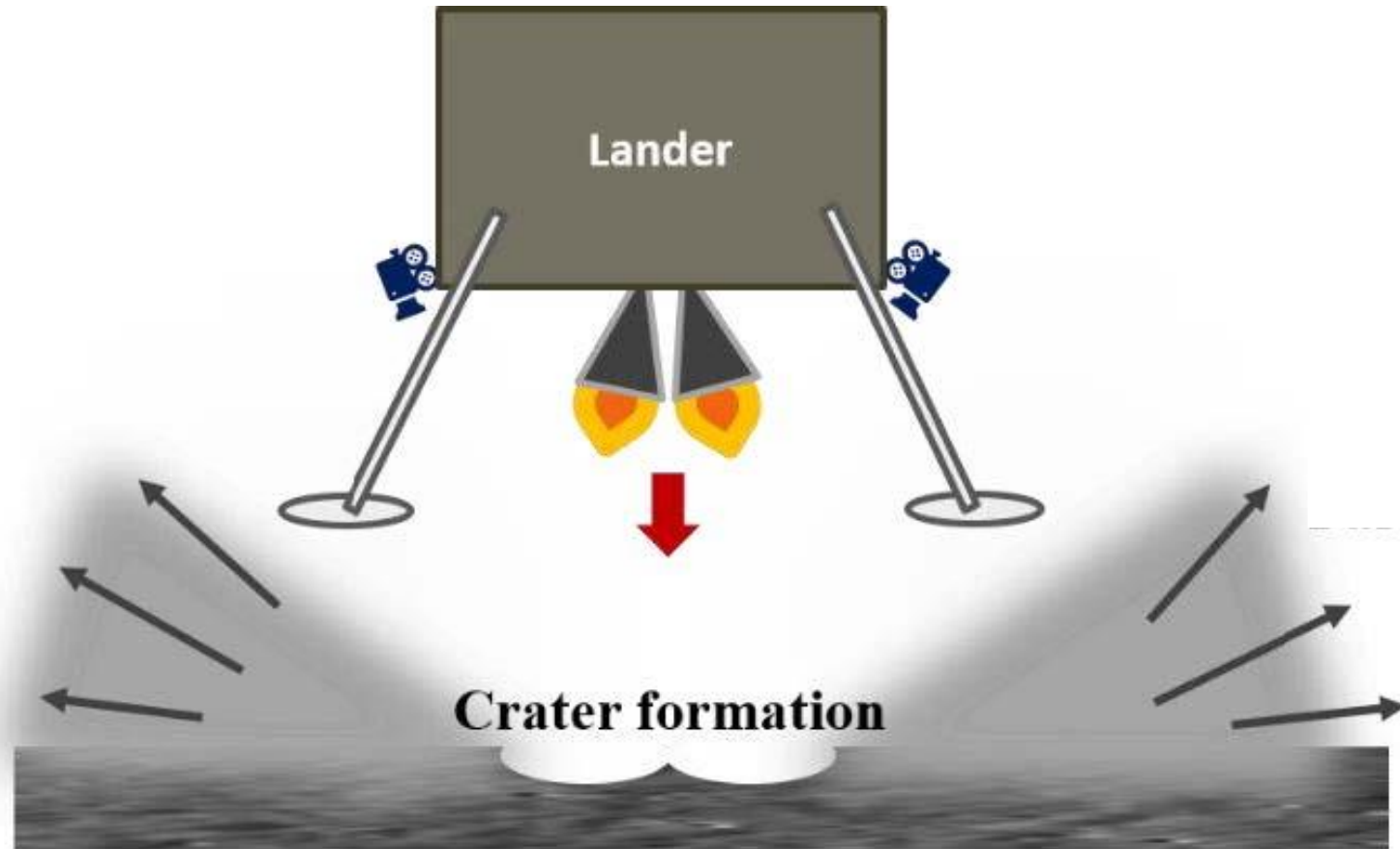
Overview

- The mission, measure Rocket Plume Erosion (RPE)
- Stereo Cameras for Lunar Plume-Surface Studies (SCALPSS)
- Camera calibration data, methods, and models
- The SCALPSS camera calibration data
- Camera model history and categories

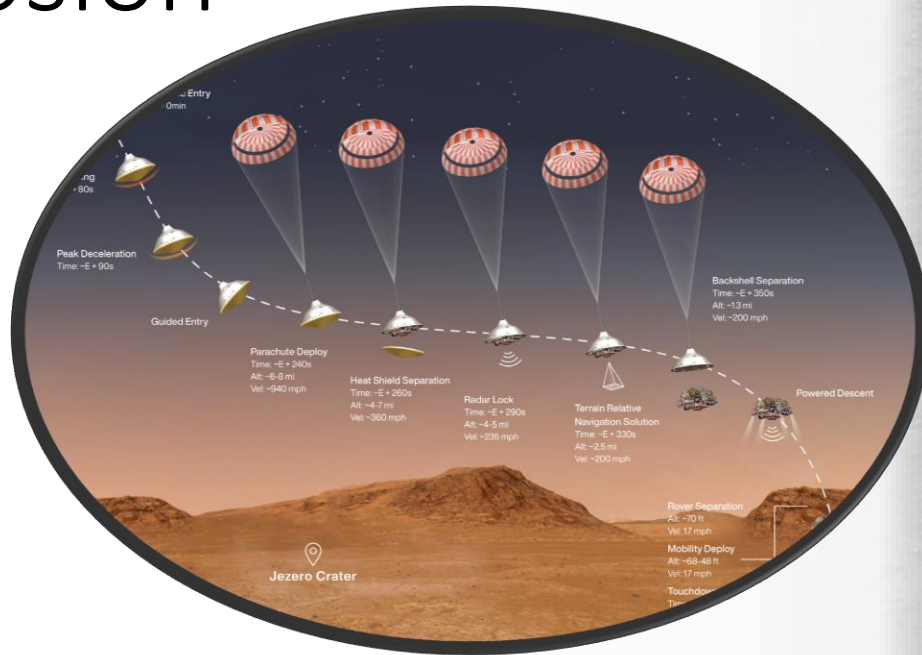
Rocket plume erosion

“interaction between the rocket plume and the surface material beneath the vehicle plays a significant role in the descent dynamics and safety[1]”

Image Source:
[2]



Rocket plume erosion



Curiosity Rover

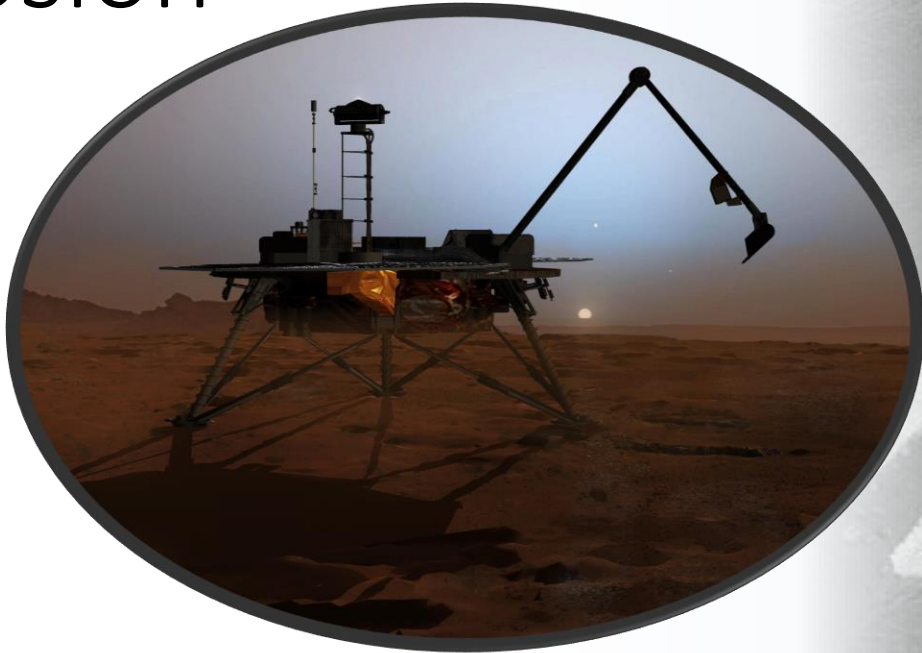
Image Sources:

<https://mars.nasa.gov/msl/multimedia/resources/insight-on-mars-illustration>

See: [Seven Minutes of Terror](#)



Rocket plume erosion



Phoenix Lander

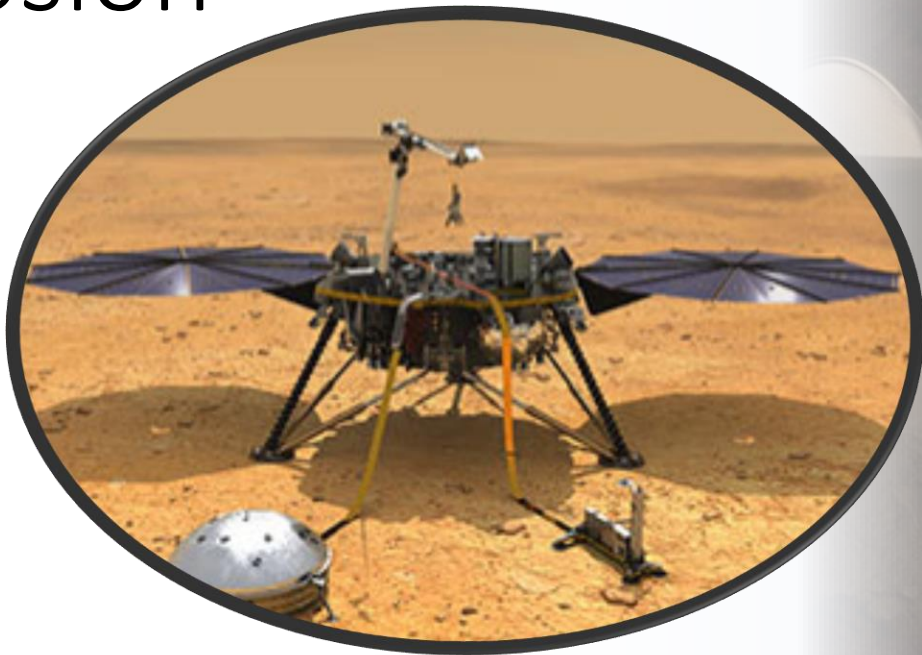
Image Sources:

Jet Propulsion Laboratory PHOTOJOURNAL

NASA Mission pages, Phoenix



Rocket plume erosion

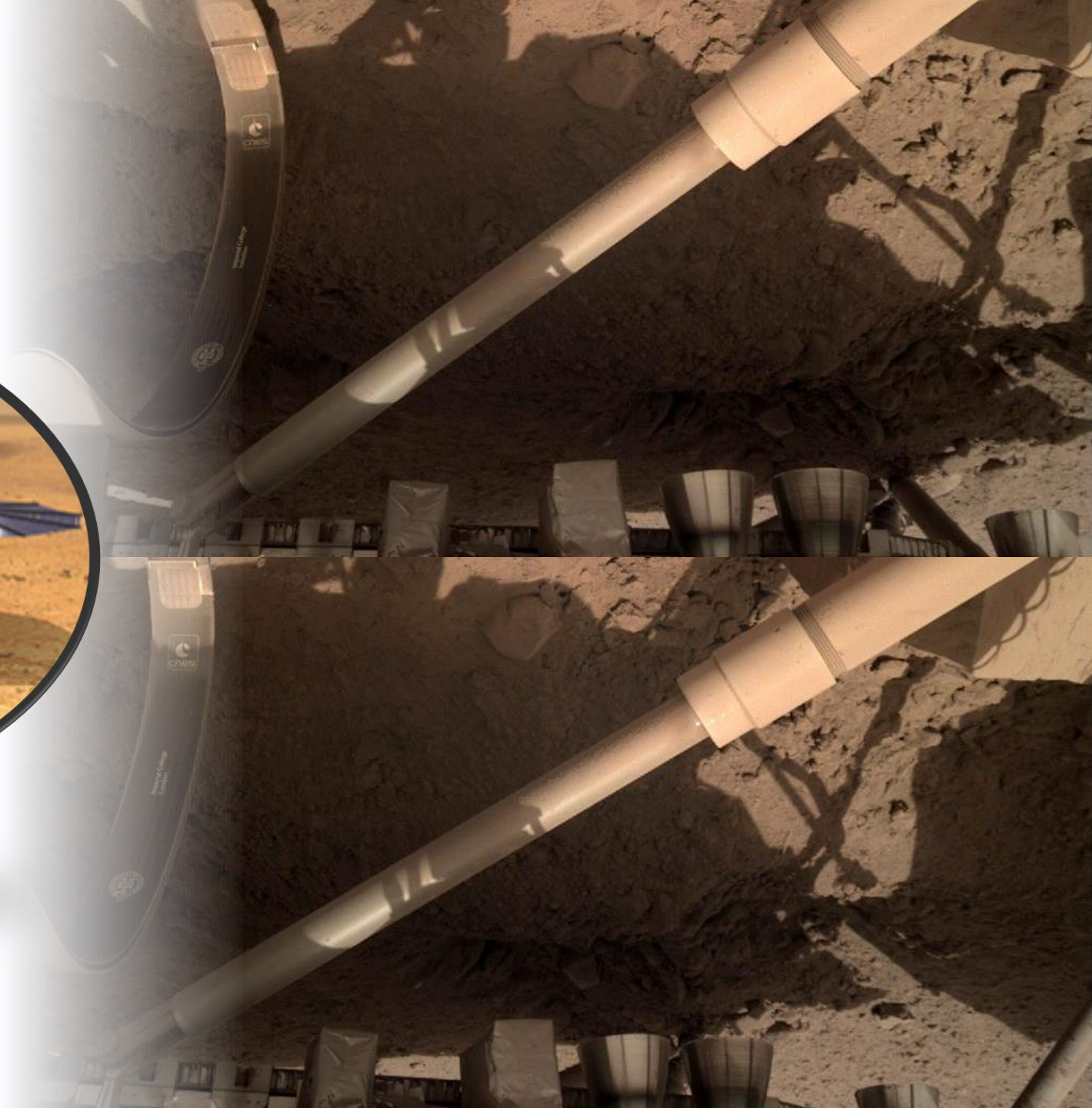


InSight Lander

Image Sources:

<https://mars.nasa.gov/insight/>

<https://mars.nasa.gov/mars-exploration/missions/insight/>



SCALPSS

First Dedicated RPE Study

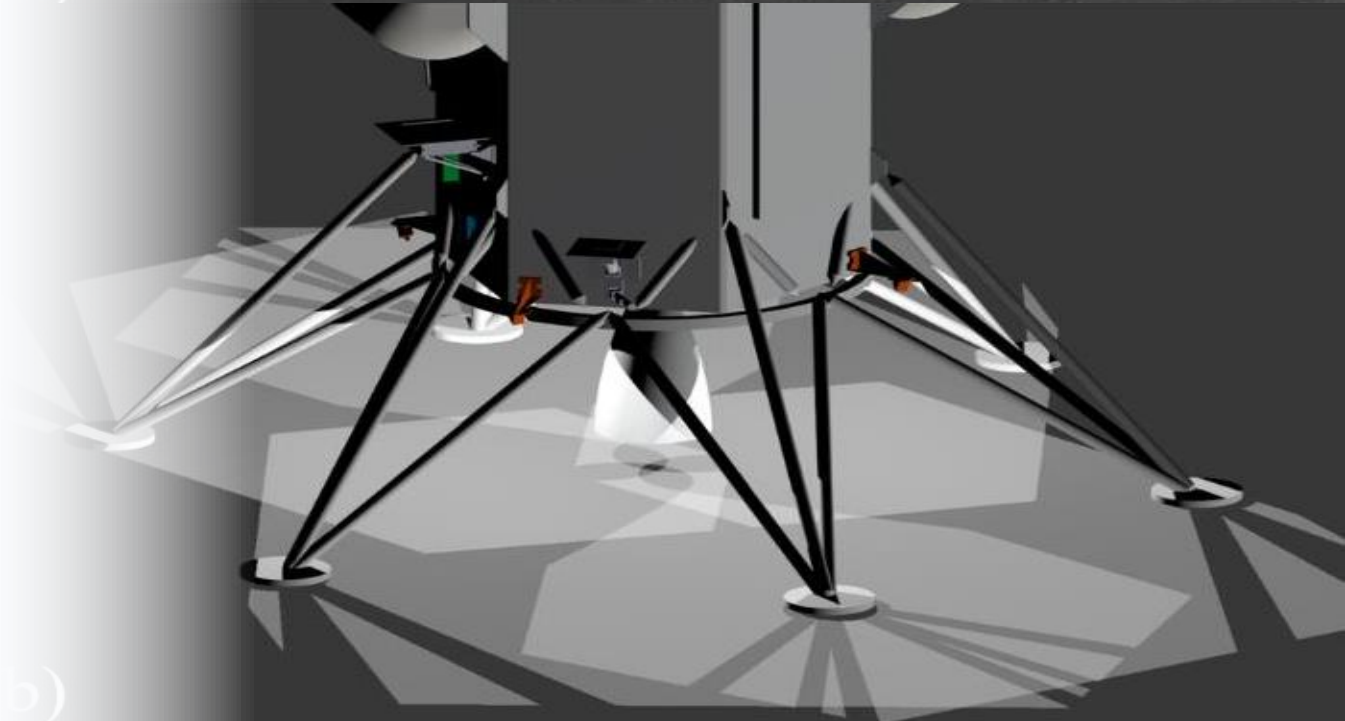
- Involved in the planning
- Measurements before, during, and after landing.
- Pick cameras and **calibrate** them.

Image Sources: [2]

References: [1-2]



a)



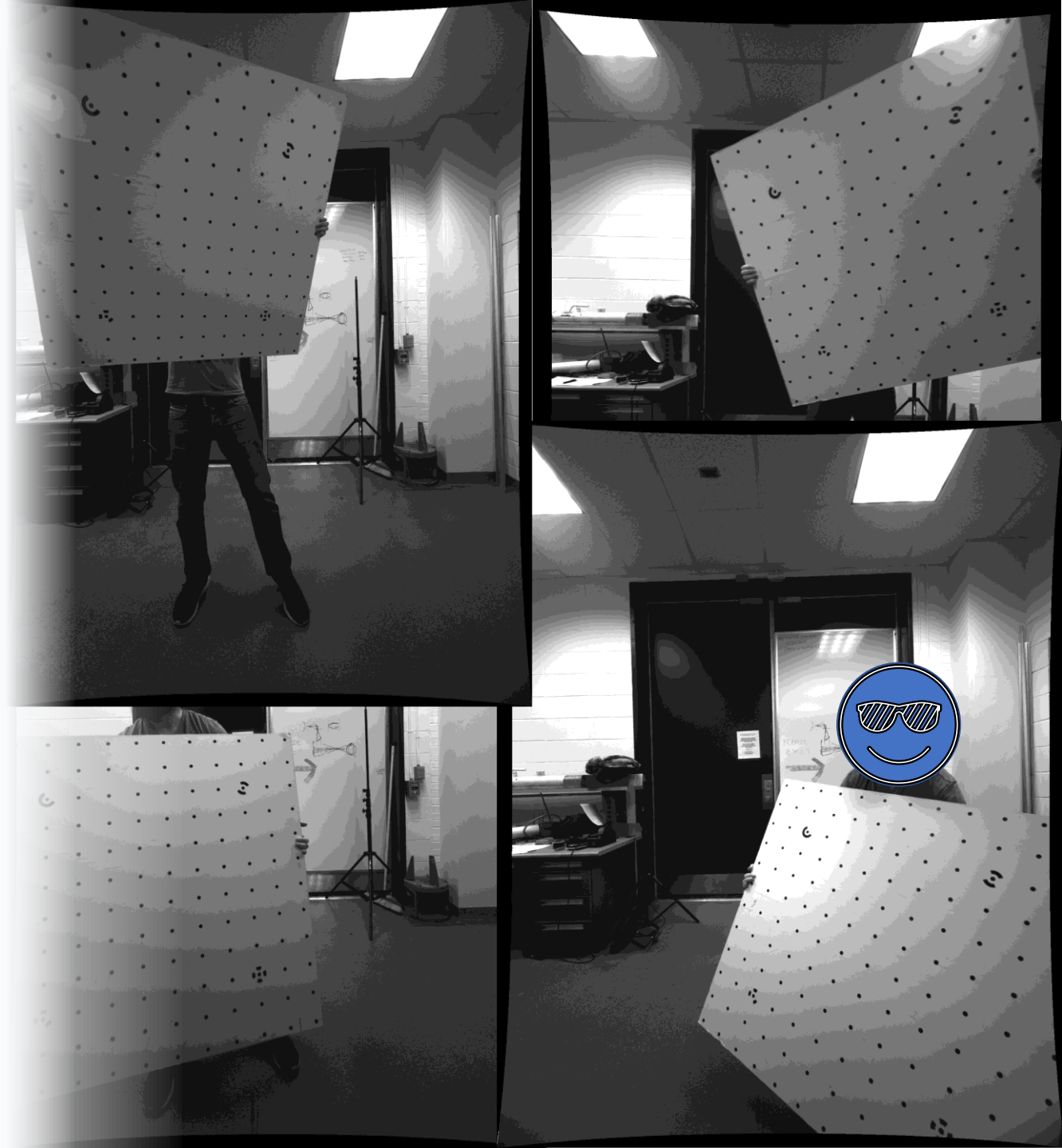
b)

Bouguet Calibration

NASA's Legacy SOP

- Measurements of planar target with targets
- Math model is essentially Brown's model
- **Failed!**

References: [3-5]



Plan B

- Calibration harp [6-7]
- Rational distortion model [8]
- Two stage calibration for ultimate de-correlation of parameters [9]
- Let the Johnson Space Flight center team do an exterior calibration.



Categorizing Calibration Models

Geometric Models

Derived from physical sensor characteristics

Few parameters that ostensibly have geometric interpretation

Applicable to families of similar sensors

Empirical Models

Derived/customized from observed distortion patterns or experience.

Moderate parameters that may have geometric interpretations.

Applicable to families of similar sensors

General Models

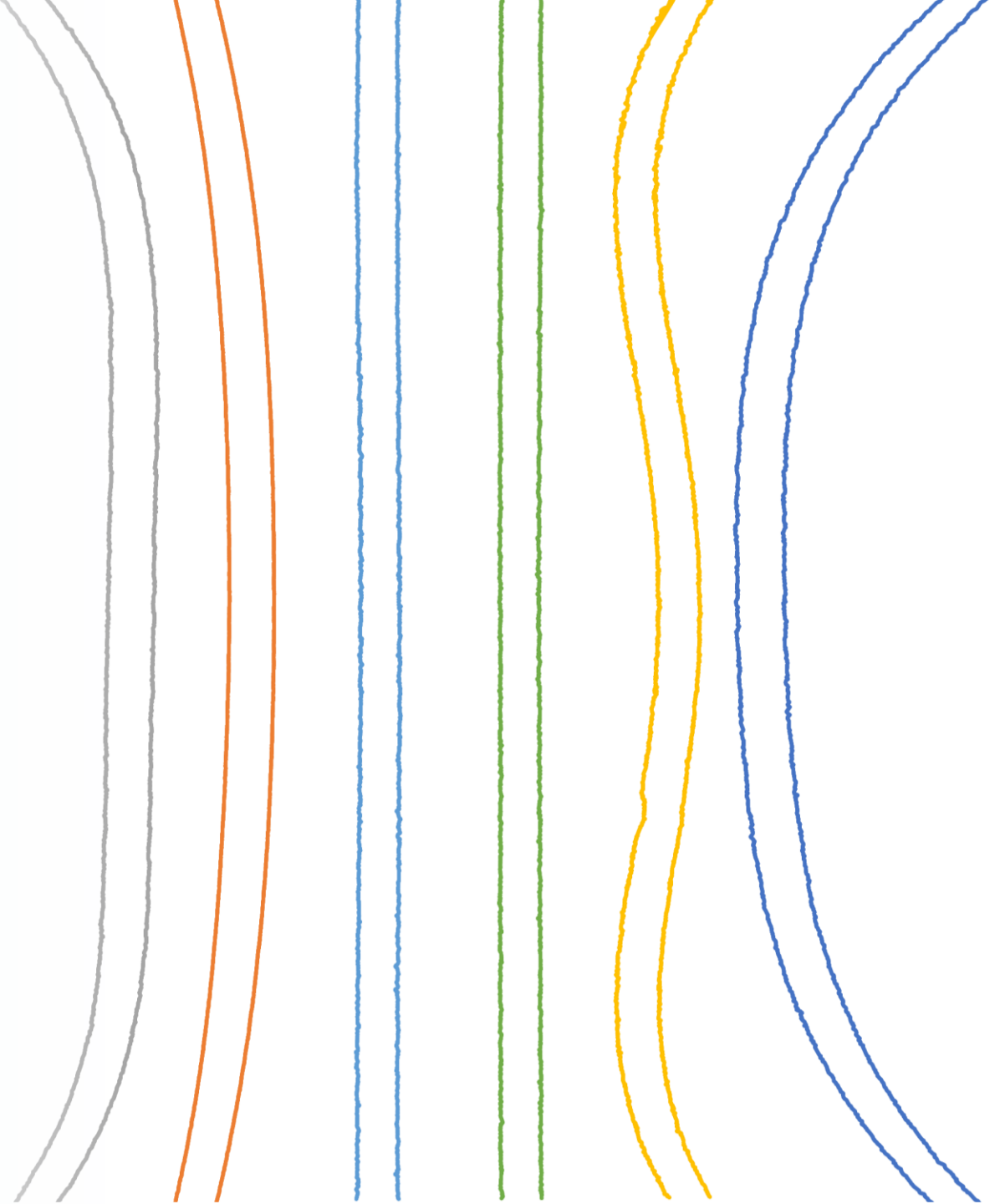
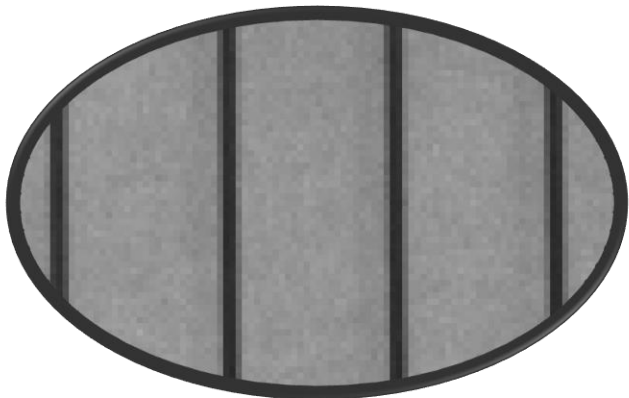
Derived from function approximation theory.

Moderate to enormous numbers of parameters with no claim of geometric interpretation.

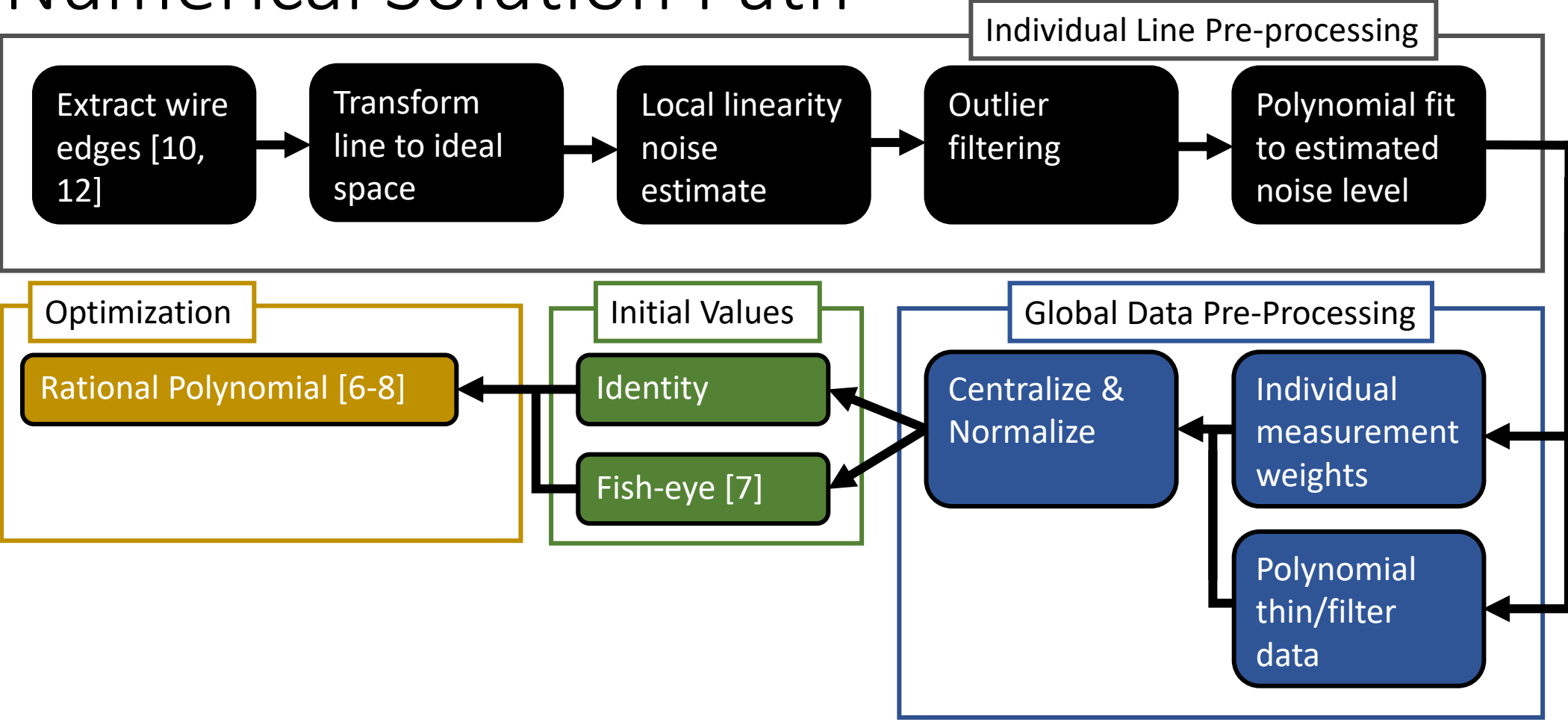
Theoretically applicable to all sensors.

Extracted Harp Lines

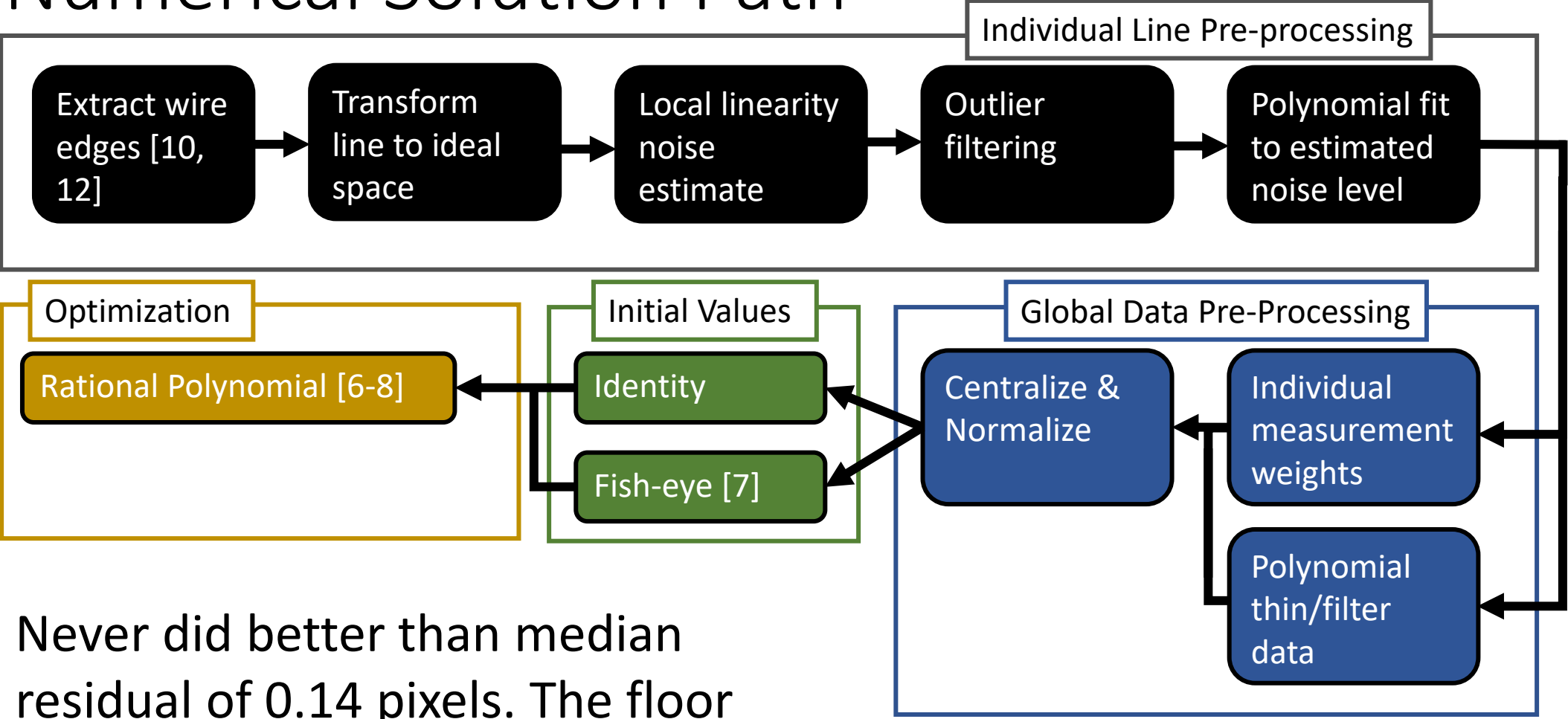
- 500,000 measurements
- Covering 99.8% of the field of view
- Precision of 0.04 pixels RMSE, consistent with [6,10-11]



Numerical Solution Path



Numerical Solution Path

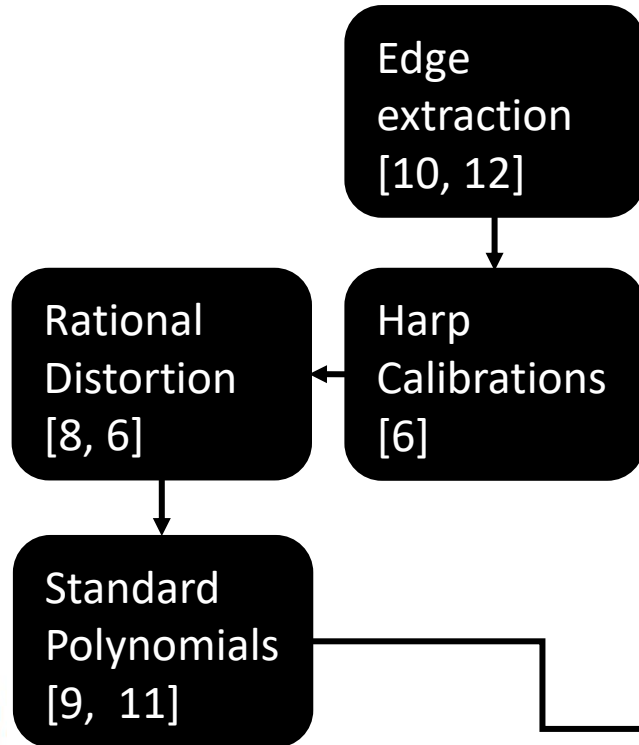


Never did better than median residual of 0.14 pixels. The floor for that value was 0.03 pixels.

Back to literature review

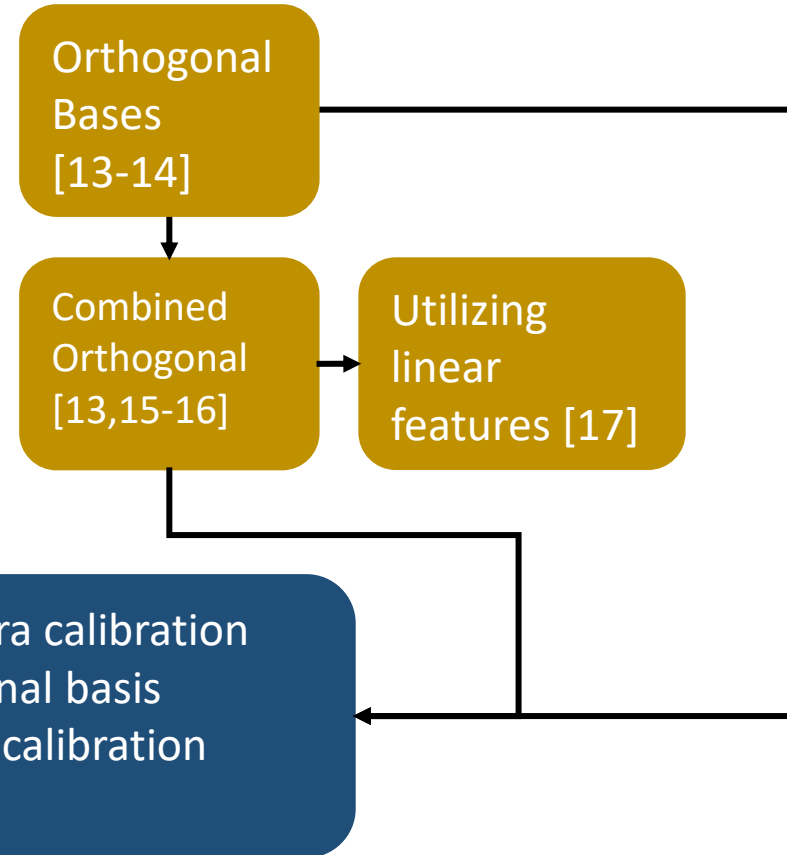
Machine Vision

Research addressing the need to model fish-eye lenses, drone/surveillance cameras



Photogrammetry

Research addressing the need to reduce correlations among parameters in Insitu calibrations.



General camera calibration using orthogonal basis functions and calibration harps.

Orthogonal Basis Functions

Can theoretically model any arbitrary function, to any arbitrary accuracy (see the Stone-Weierstrass or Fourier Theorem).

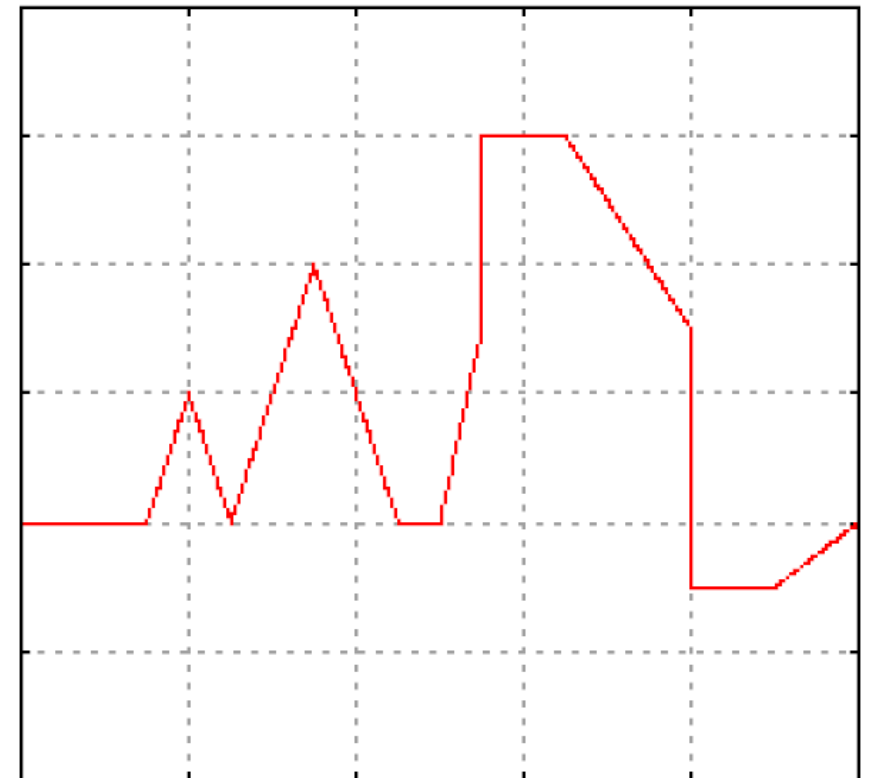


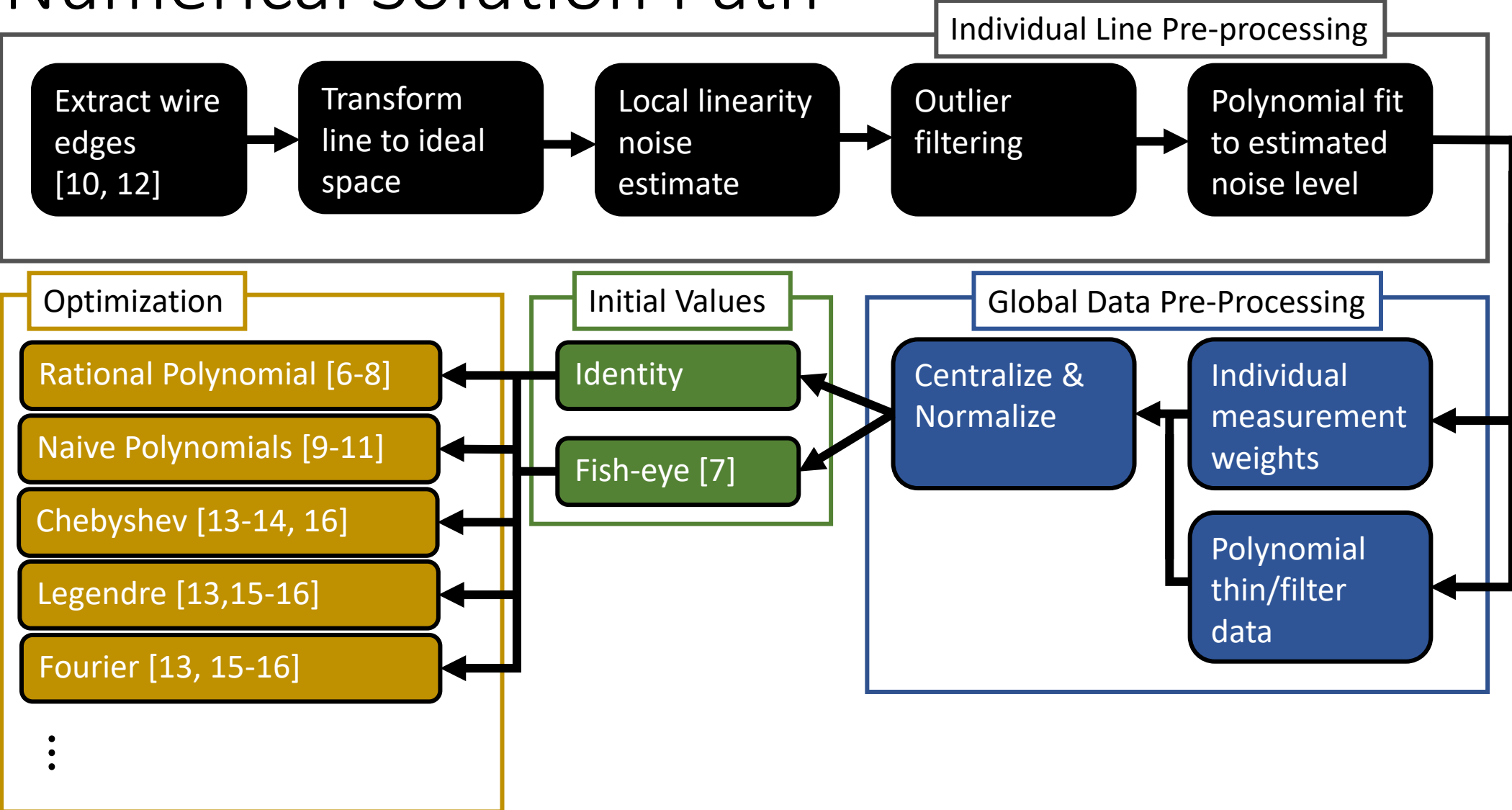
Image Source: Wikipedia commons

2D Orthogonal Basis Functions

$$f_{m,n}(x,y) = g_m(x)h_n(y) \quad \int_{-1}^1 \int_{-1}^1 f_{m_1,n_1}(x,y)f_{m_2,n_2}(x,y) d_x d_y = 1, \text{ if } m_1 = m_2 \text{ and } n_1 = n_2, \text{ else } 0$$

Legendre	Chebyshev (Type 1)	Fourier
1	1	1
x	x	$\sin(\pi x)$
y	y	$\sin(\pi y)$
$(3x^2 - 1)/2$	$2x^2 - 1$	$\cos(\pm\pi x)$
xy	xy	$\cos(\pm\pi y)$
$(3y^2 - 1)/2$	$2y^2 - 1$	$\sin(2\pi x)$
$(5x^3 - 3x)/2$	$4x^3 - 3x$	$\cos(\pm 2\pi x)$
$(3x^2 - 1)y/2$	$(2x^2 - 1)y$	$\sin(\pi x)\cos(\pm\pi y)$
$(3y^2 - 1)x/2$	$(2y^2 - 1)x$	$\cos(\pm\pi x)\sin(\pi y)$
$(5y^3 - 3y)/2$	$4y^3 - 3y$	$\sin(2\pi y)$
\vdots	\vdots	\vdots

Numerical Solution Path



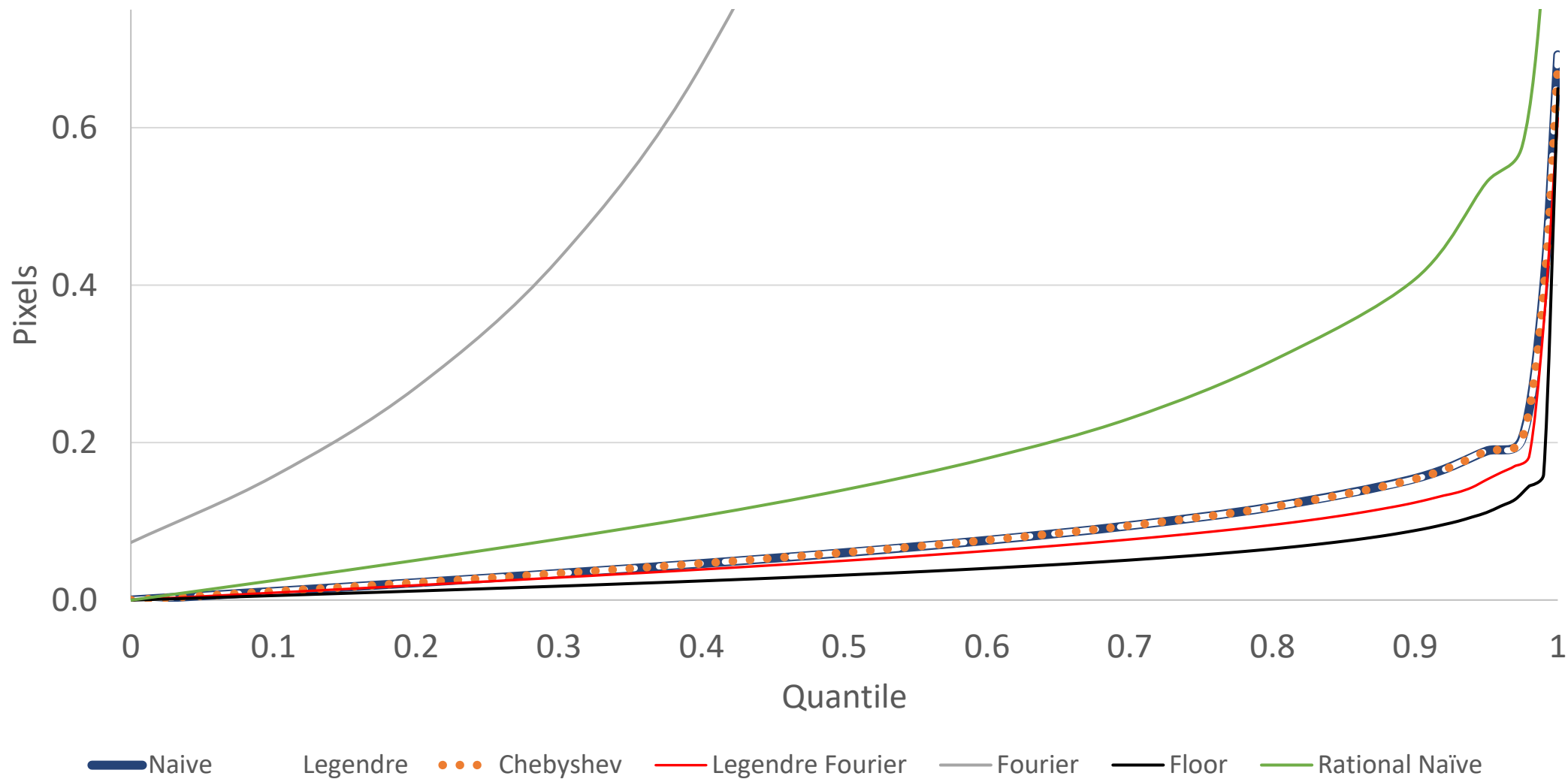
Polymorphic Optimizer

```
interface BasisFunction {  
    // Evaluate the basis function at (x, y)  
    double operator()(double x, double y)  
  
    // Differentiate the basis WRT x at (x, y)  
    double dx(double x, double y)  
  
    // Differentiate the basis WRT y at (x, y)  
    double dy(double x, double y)  
};
```

```
class StandardPolynomialBasis implements BasisFunction {  
    // Evaluate the basis function at (x, y)  
    double operator()(double x, double y) return  $x^m y^n$   
  
    // Differentiate the basis WRT x at (x, y)  
    double dx(double x, double y) return  $m x^{m-1} y^n$   
  
    // Differentiate the basis WRT y at (x, y)  
    double dy(double x, double y) return  $n x^m y^{n-1}$   
};
```

Results

Residual distributions

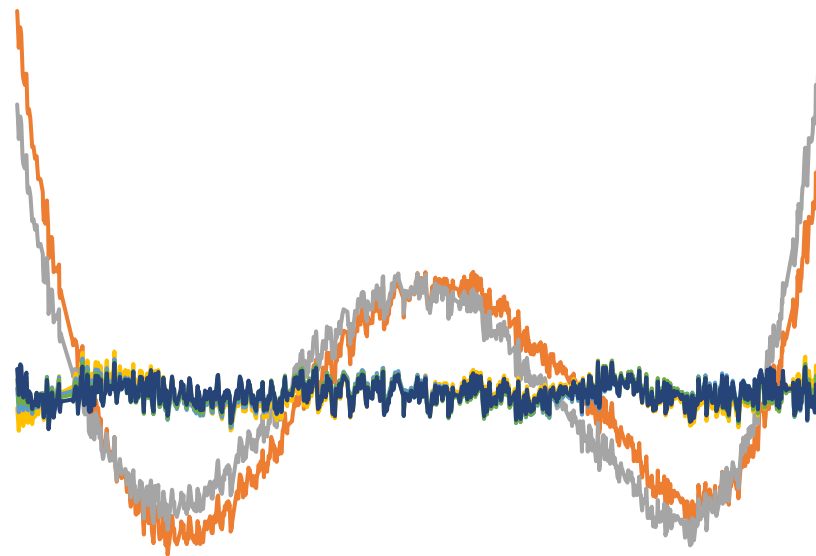


Results



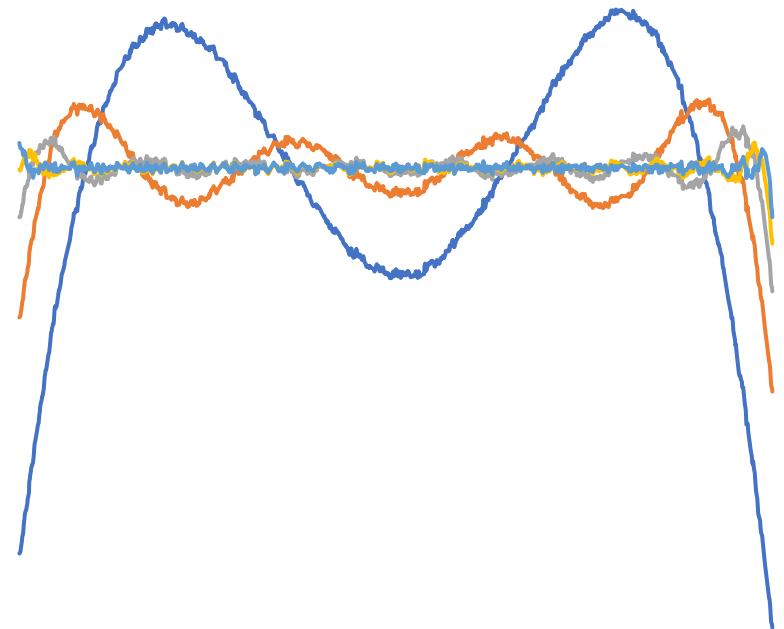
What happened with to Fourier basis?

Residuals of Polynomial Fits



— 3 Bases — 4 Bases — 5 Bases — 6 Bases — 7 Bases — 8 Bases

Residuals of Fourier Basis Fit



— 4 Bases — 8 Bases — 16 Bases — 32 Bases — 64 Bases

Results

Correlations

	Legendre	Chebyshev	Standard	Fourier
Percent < 0.1	95%	94%	94%	96%
99th Percentile	0.74	0.78	0.78	0.34
max	1.00	1.00	1.00	0.45

Conclusions

- Harps are a cheap and practical way to collect abundant high precision data.
- In the context of laboratory harp calibrations:
 - Orthogonal basis functions are a theoretical general approach to modeling distortion that performed well empirically.
 - The type of orthogonal basis function is largely irrelevant.
 - Polynomial bases don't have high correlation issues they do in collinearity adjustments
 - Mixing Fourier and polynomial basis showed promise (though this is an empirical claim).

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- [1] Thompson, R. J., Danehy, P. M., Munk, M. M., Mehta, M., Manginelli, M. S., Nguyen, C., & Thomas, O. H. (2021). Stereo Camera Simulation for Lunar Surface Photogrammetry. In AIAA Scitech 2021 Forum (p. 0358).
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