

# Investigating the Impact of Noise Infusion on Seasonal Adjustment in the Quarterly Financial Report

( a work in progress)

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# The Quarterly Financial Report (QFR)

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## Quarterly Financial Report

Main

About

Information for Respondents

Data

Time Series/Trend Charts

Technical Documentation

Release Schedule

Definitions

FAQs

Contact Us

[!\[\]\(f1c5da15572e3e09d343161be98f508d\_img.jpg\) Back to Our Surveys & Programs](#)

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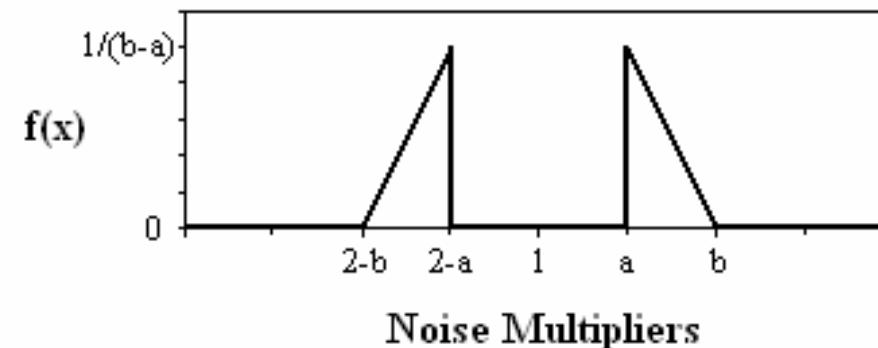
Latest QFR Release for Retail Trade

[Release Schedule](#)

# EZS Noise Infusion

- Randomly assign noise factor using a split symmetric distribution

**Split Triangular Density Function**



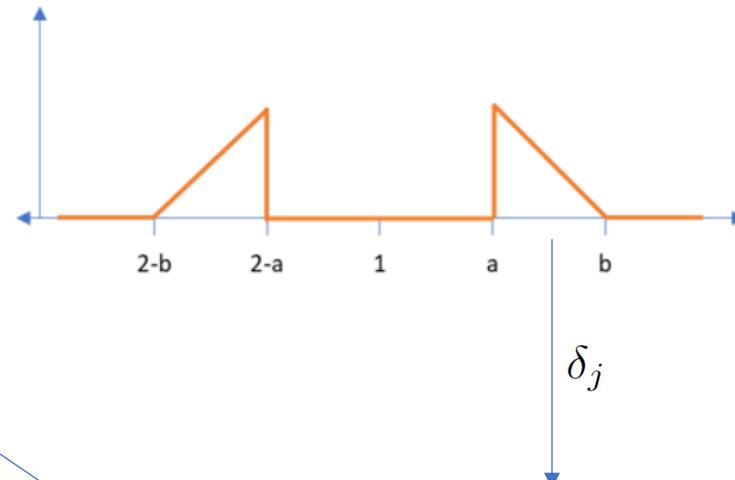
For example, let  $a = 1.10$  and  
 $b = 1.15$

- Apply noise factor at the microdata level for each reported data value
- Sum up all the perturbed values over a specified domain

# EZA Noise Example

	Reported Data Value
company A	114372
company B	126691
company C	43468
company D	482825
company E	977120
company F	457678
company G	837884
company H	522126
company I	808820
...	...

*Fabricated Data*



For example, suppose  $a = 1.10$   
and  $b = 1.15$

Perturbed Data Value

125866
141425
49301
534488
1086068
505780
921840
594336
903371
...

$$X_{dj^t}^* = \delta_j X_{dj^t}$$

Noise Factor

1.1005
1.1163
1.1342
1.107
1.1115
1.1051
1.1002
1.1383
1.1169
...

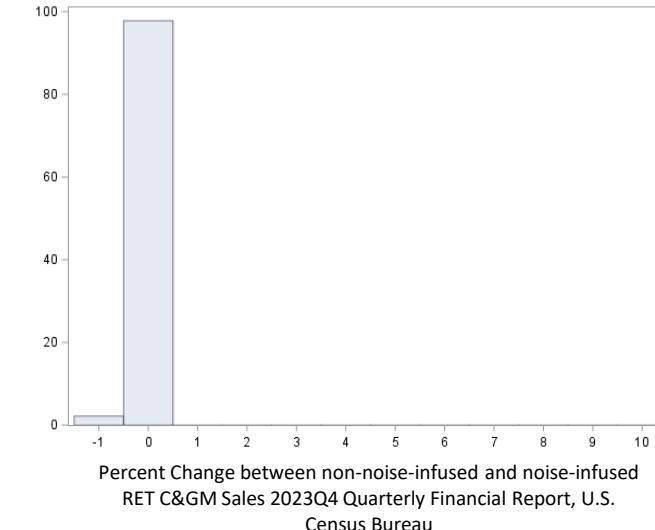
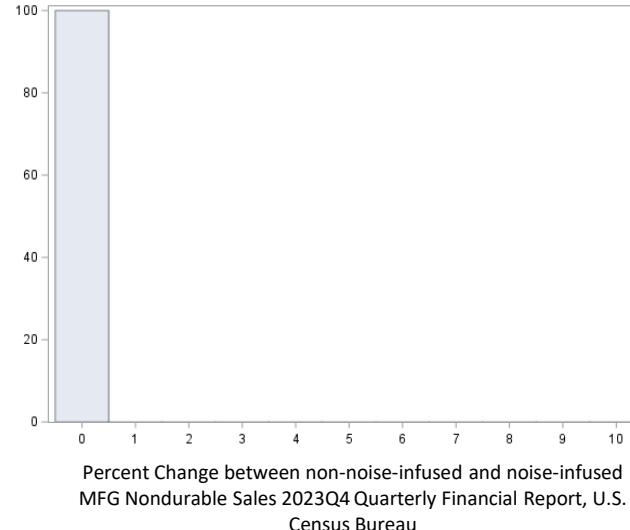
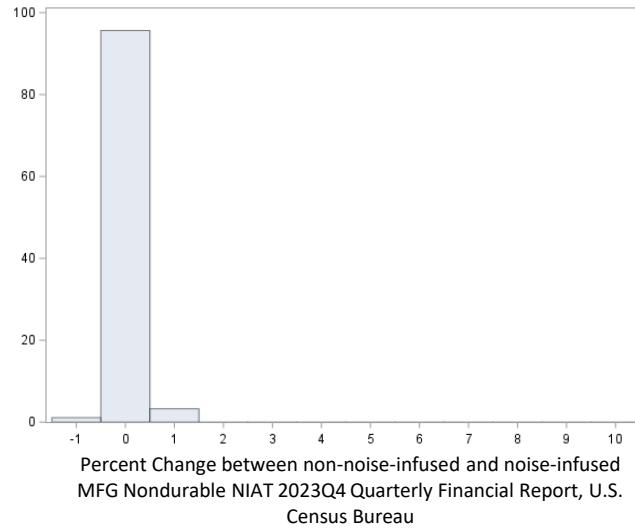
*Fabricated Data*

$\sum$

Final Published Estimate

185446045

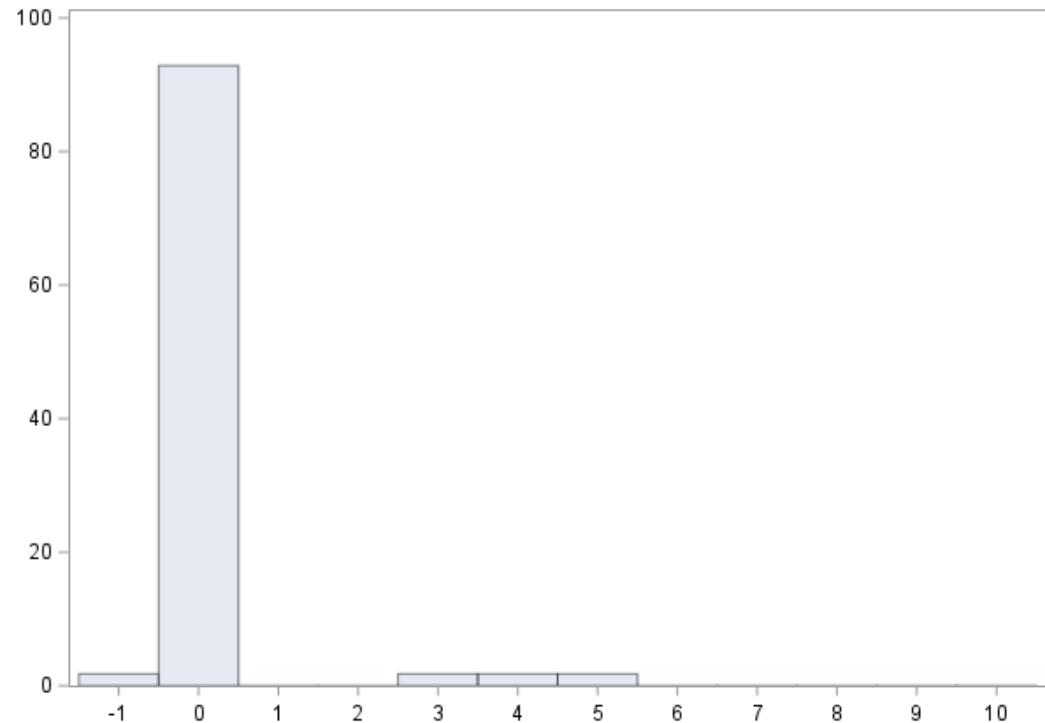
# Time Series Comparison



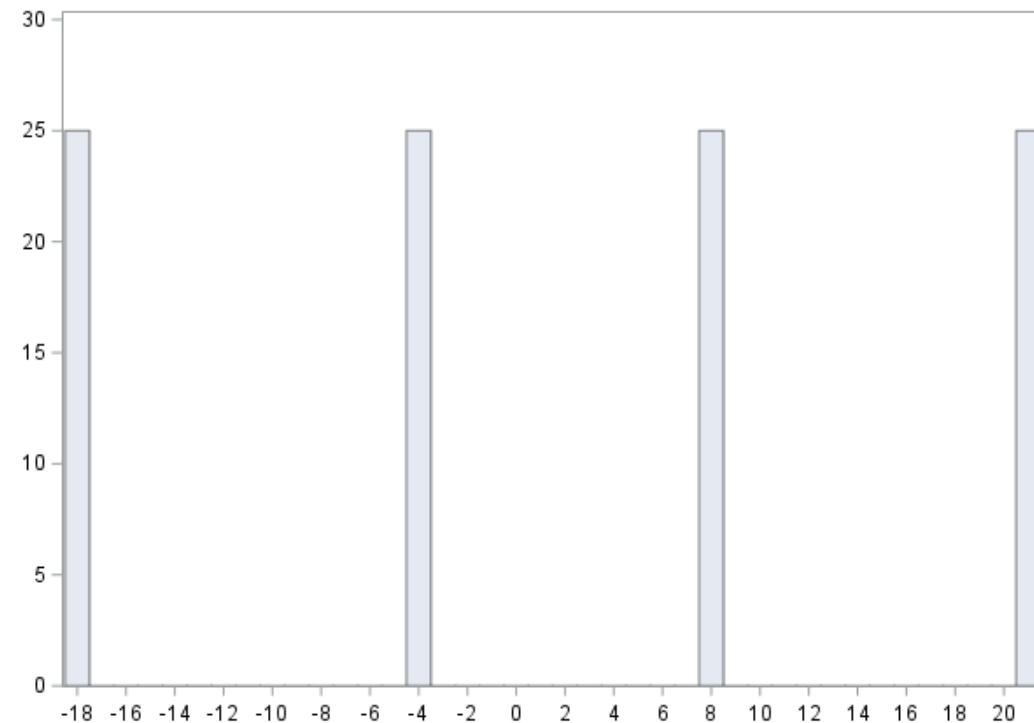
- Our findings indicate that the relative differences between the noise-infused and non-noise-infused series are typically within a 1% threshold

# Time Series Comparison

Unadjusted Series



Adjusted Series



Percent Change between non-noise-infused and noise-infused PTS NIAT  
2023Q4 Quarterly Financial Report, U.S. Census Bureau

# Time Series Comparison

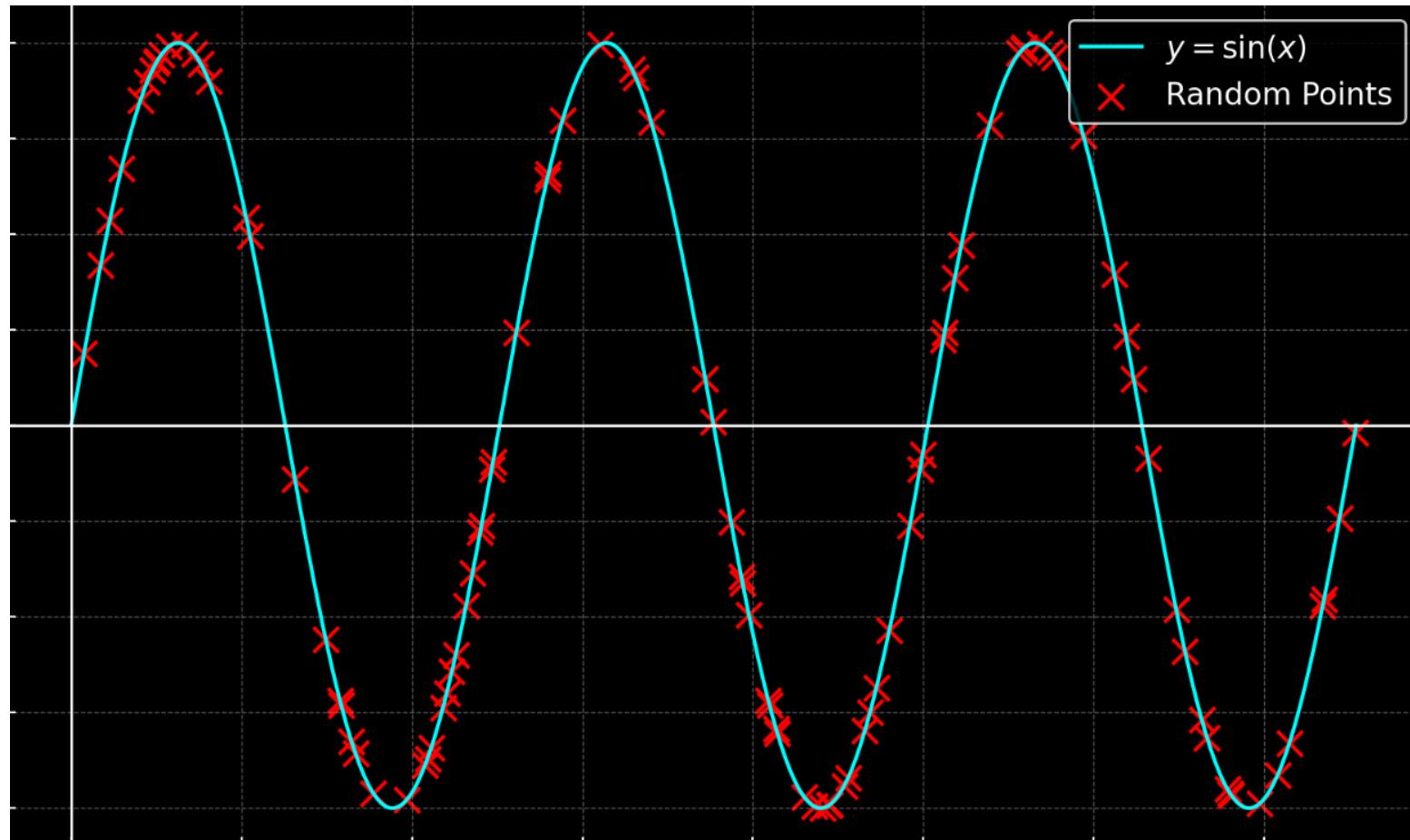
STATP	UnAdj_n	UnAdj_no_n	UnAdj%Δ	SA_Adj_n	SA_Adj_no_n	SA_Adj%Δ	UnAdj_n & SA_Adj_n%Δ	UnAdj_no_n & SA_Adj_no_n%Δ
2022Q3	-13,923	-13,923	0.00	-13,591	-13,591	0.00	2.45	2.45
2022Q4	-24,649	-26,763	8.58	-26,414	-28,516	7.96	6.68	6.15
2023Q1	-10,845	-11,022	1.63	-8,943	-9,084	1.59	21.27	21.33
2023Q2	-16,136	-16,725	3.65	-16,556	-17,159	3.64	2.54	2.53
2023Q3	-5,281	-5,261	0.38	-4,986	-5,002	0.33	5.92	5.17
2023Q4	-2,552	unpublished	unpublished	-4,404	unpublished	unpublished	72.56	65.51

Percent Change between non-noise-infused and noise-infused PTS NIAT 2023Q4 Quarterly Financial Report, U.S. Census Bureau

- Conclusion: the ARIMA model built on non-noisy data was no longer a good candidate for the noisy data.
- Solution: build the ARIMA model on the mixed data and monitor the series over time.

## Future Work

- One possibility is exploring the use of simulated data to derive a more generalized methodology.



- For example, we could take points from a known function
- Build an ARIMA model on non-noisy data
- Apply EZS noise infusion
- Build the ARIMA model on mixed or noisy data
- Analysis of comparison

# Conclusion & Acknowledgements

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