

Some Historical Perspectives on Seasonal Adjustment

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- 1 Early history of seasonal adjustment
- 2 Use of electronic computers for seasonal adjustment
- 3 Relevant developments in time series modeling
- 4 Combining time series modeling and traditional (X-11) seasonal adjustment
- 5 Model-based seasonal adjustment
- 6 Comparing X-11 and model-based seasonal adjustment
- 7 Some current issues and possible future directions for seasonal adjustment

1. Early history of seasonal adjustment

Very early history

- Nerlove, Grether, and Carvalho (1979) – idea of time series coming from unobserved components came from astronomy and meteorology and became popular in economics in England, 1825-1875.
- Discuss seasonal adjustment work of Dutch meteorologist Buys-Ballot (1847).

Note: For historical reference citations in what follows, and for additional discussion, see Bell and Hillmer (1984, "Issues Involved with the Seasonal Adjustment of Economic Time Series," (with discussion), *Journal of Business and Economic Statistics*, pp. 291–349).

Fundamental paper: Persons (1919)

Viewed economic time series as composed of:

- long-time tendency or secular trend
- wave-like or cyclical movements
- seasonal movements
- residual variation

Persons may have been the first to propose a general method that could adequately decompose an economic time series into the above four components

1920s and 1930s – explosion of interest in seasonal adjustment

Important concepts that became fixed:

- 1 seasonality is often multiplicative – to seasonally adjust, divide data by seasonal factors
- 2 seasonality can change over time – estimate seasonal factors using moving averages
- 3 must account for trends and cycles when estimating the seasonal component – iterate between detrending and estimating the seasonal
- 4 cannot describe trends and cycles by explicit formulas – estimate trends by moving averages
- 5 need to deal with extreme observations – used moving medians or trimmed means instead of moving averages

Outcome: Ratio-to-moving average approach, with some adjustment for extreme values

2. Use of electronic computers for seasonal adjustment

Primary motivation: to increase the number of seasonally adjusted series

1954 Census Bureau – Julius Shiskin and colleagues develop an approach (Method I) for doing seasonal adjustments on the Univac 1

1955 Method II, X-1 variant

⋮

1965 Method II, X-11 variant

Impacts of doing seasonal adjustment on electronic computers

- reduced costs so many more series could be seasonally adjusted
- calculations required could be more complicated
- time spent determining how best to reduce a given series was reduced
 - methods had to automatically deal with things previously left to professional judgment
- automatic nature lent an air of objectivity to the process
 - contrast to some early methods that used free-hand smoothing
- regression used to estimate and adjust for trading-day effects (Young 1965)

3. Relevant developments in time series modeling

Early developments:

- autoregressive models (Yule 1927)
- moving average models (Slutsky 1937, Wold 1938)
- AR models with seasonal lags (Whittle 1952,1953a,1954a)
- regression models with time series errors (Whittle 1954b,Durbin 1960a)
- model estimation (Whittle 1953a,b,1954b; Durbin 1959,1960a,b; Walker 1961,1962)

Book by Box and Jenkins (1970): *Time Series Analysis: Forecasting and Control*

Developed a systematic approach to seasonal ARIMA modeling

Airline model: $(1 - B)(1 - B^{12})z_t = (1 - \theta_1 B)(1 - \theta_{12} B^{12})a_t$

- nonseasonal differencing for detrending
- seasonal differencing to allow for changing seasonality
- book was followed by software development

4. Combining time series modeling and traditional (X-11) seasonal adjustment

- X-11-ARIMA (Dagum 1980)
 - ARIMA forecast extension to do linear filtering at ends of series
 - log-additive adjustment
- RegARIMA modeling for estimation and inference about calendar effects (Bell and Hillmer 1983)
- Use of time series outlier detection for Additive Outliers and Level Shifts (Chang 1982, Bell 1983, Tsay 1986)
- X-12-ARIMA (Findley et al. 1998)

5. Model-based seasonal adjustment

- Attempts based on regression (1922-1972) had little impact
- Canonical ARIMA model-based adjustment (now in use)
 - Box, Hillmer, and Tiao (1978); Hillmer and Tiao (1982)
 - Burman (1980)
 - Software developed
 - Gomez and Maravall (1997) – TRAMO/SEATS
 - X-13 (U.S. Census Bureau 2012) – combines features of X-12-ARIMA and TRAMO/SEATS
- Approaches based on directly specifying ARIMA component models
 - BAYSEA (Akaike 1980)
 - Structural models – Harvey (1989), Durbin and Koopman (2001)

6. Comparing X-11 and model-based seasonal adjustment

Cleveland and Tiao (1976) compared, for trend and seasonal filters:

- X-11 filter weights w_j^{X11} (for derivation, see Wallis 1974) obtained with “default” choices of the MAs (3×5 seasonal MA and 13-term Henderson trend MA), and
- filter weights w_j^{MB} from signal extraction with component models of a given form (see below).

They determined the component model parameter values to

$$\min \sum_j (w_j^{X11} - w_j^{MB})^2$$

summing over the values of j for which the X-11 weights were appreciable ($j = -42$ to 42).

Cleveland and Tiao determined the following 3-component model ($Y_t = S_t + T_t + I_t$) for approximating both the X-11 seasonal and trend filters:

$$(1 - B^{12})S_t = (1 + .49B^{12} - .49B^{24})b_t \quad \sigma_b^2/\sigma_c^2 = 1.3$$

$$(1 - B)^2 T_t = (1 + .64B + .83B^2)c_t$$

$$I_t = \text{white noise} \quad \sigma_I^2/\sigma_c^2 = 14.4.$$

The implied model for Y_t is that $(1 - B)(1 - B^{12})Y_t$ follows an MA(25) model.

Extensions to the work of Cleveland and Tiao

- Burridge and Wallis (1984) developed
 - models to approximate **symmetric and asymmetric X-11 seasonal adjustment filters**, and
 - model-based approximations to X-11 filters using the **optional 3×3 and 3×9 seasonal MAs**.
- Chu (2000) used higher order models and so obtained better approximations to various X-11 filters.
- Planas and Depoutot (2002) restricted consideration to **canonical decomposition of the airline model for approximating the X-11 filters**.
- Depoutot and Planas (1998) considered **picking an X-11 filter** (through choice of seasonal and trend MAs) **to approximate a given airline model-based adjustment filter** obtained from the canonical decomposition.

Statistical (MSE) comparisons of X-11 and model-based seasonal adjustments (Chu, Tiao, and Bell 2012)

- 1 Assume Y_t follows the airline model and the true S_t and N_t come from the canonical decomposition of this model.
- 2 Let N_t^{X11} be the X-11 seasonal adjustment for any given choice of
seasonal MA: $(3 \times 1, 3 \times 3, 3 \times 5, 3 \times 9, \text{ or } 3 \times 15)$
Henderson trend MA: $(9, 13, 17, \text{ or } 23\text{-term})$.

Compute $E[(N_t^{X11} - N_t)^2]$ for all 20 of these combinations and let \hat{N}_t^{X11} be the X-11 estimate among these with the lowest MSE.

- 3 Let \hat{N}_t be the MMSE linear predictor of N_t from the model. Examine the increase in MSE from using \hat{N}_t^{X11} compared to \hat{N}_t by

$$\text{X-11 MSE \% increase} = 100 \times \frac{E[(\hat{N}_t^{X11} - N_t)^2] - E[(\hat{N}_t - N_t)^2]}{E[(\hat{N}_t - N_t)^2]}.$$

Comparing MSEs for X-11 and Model-based Filters
 Canonical decomposition of the airline model with $\theta_1 = .5$

	θ_{12}			
	.2	.5	.8	.9
Best X-11 seasonal MA	3×1	3×5	3×15	3×15
MSE % increase for X-11 symmetric filter	14%	6%	10%	33%
concurrent filter	3%	1%	3%	9%

Summary of Conclusions from Chu, Tiao, and Bell

- Length of best X-11 seasonal MA increases with θ_{12} . X-12 automatic filter selection sometimes picks shorter seasonal MAs than the best (assessed in a small simulation study).
- The best X-11 filters generally do pretty well for estimating the canonical decomposition, especially for concurrent adjustment or (Bell, Chu, and Tiao 2012) finite sample adjustments with a series that is not long.
- Lone exception where best X-11 filter does poorly: seasonal adjustment in the middle of a very long series when θ_{12} is large (.9).
- Other X-11 filters with a seasonal MA close to the best choice (for example, 3×3 when $\theta_{12} = .5$) have only slightly larger MSEs. X-11 filters far from the best can have larger MSE increases.

7. Some current issues and possible future directions for seasonal adjustment

Seasonally adjusting time series with sampling error

$$Y_t = S_t + T_t + I_t \quad \rightarrow \quad Y_t = S_t + T_t + I_t + e_t$$

e_t = sampling error in Y_t

- Question: Is seasonal adjustment estimating

$$N_t = T_t + I_t$$

$$\text{or } A_t = Y_t - S_t = T_t + I_t + e_t?$$

- For more on this topic, see next talk by Dick Tiller.

Variances for seasonal adjustment

- For model-based adjustment – falls out of the calculations
- For X-11, variance approximations were given by
 - Pfeffermann (1994); Scott, Pfeffermann, and Sverchkov (2012)
 - Bell and Kramer (1999)
- For "exact" MSEs of X-11 adjustments, use the approach of Bell, Chu, and Tiao (2012)
- Questions to be answered:
 - Is seasonal adjustment estimating N_t or $Y_t - S_t = N_t + e_t$?
 - How to present the results, which produce a different variance for every time point.

Modeling and adjusting for weather effects or seasonal heteroskedasticity

- Boldin and Wright (2015) – model effects of unusual weather on employment data
- Trimbur and Bell (2012) – model seasonal heteroskedasticity (higher variance in winter months) for U.S. regional housing starts and building permits
- Concurrent session I: Talks by Osbert Pang and Thomas Trimbur

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