

Mechanistic modeling of metastasis: cancer at the organism scale

S. Benzekry
Inria Bordeaux Sud-Ouest

ISoP workshop
July 11th, 2019

Inria

M**NC**

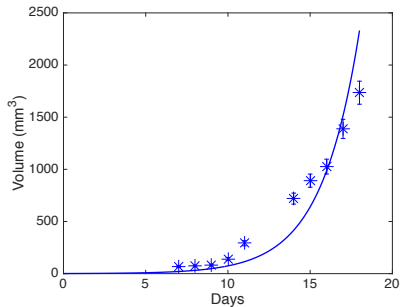
Modeling in **ONC**ology

Can mathematical models be of help in oncology?



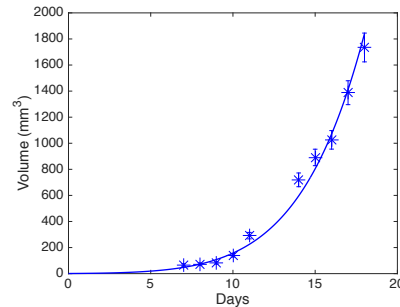
Understand (biology)

- **Theoretical** framework for description of the process
- Test different **hypotheses** and reject non-valid ones



Exponential

$$\frac{dV}{dt} = aV$$



Power law

$$\frac{dV}{dt} = aV^\gamma$$

Can mathematical models be of help in oncology?

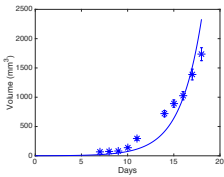


Predict and control (clinic)

- Predict tumor growth

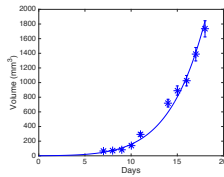
Understand (biology)

- **Theoretical** framework for description of the process
- Test different **hypotheses** and reject non-valid ones



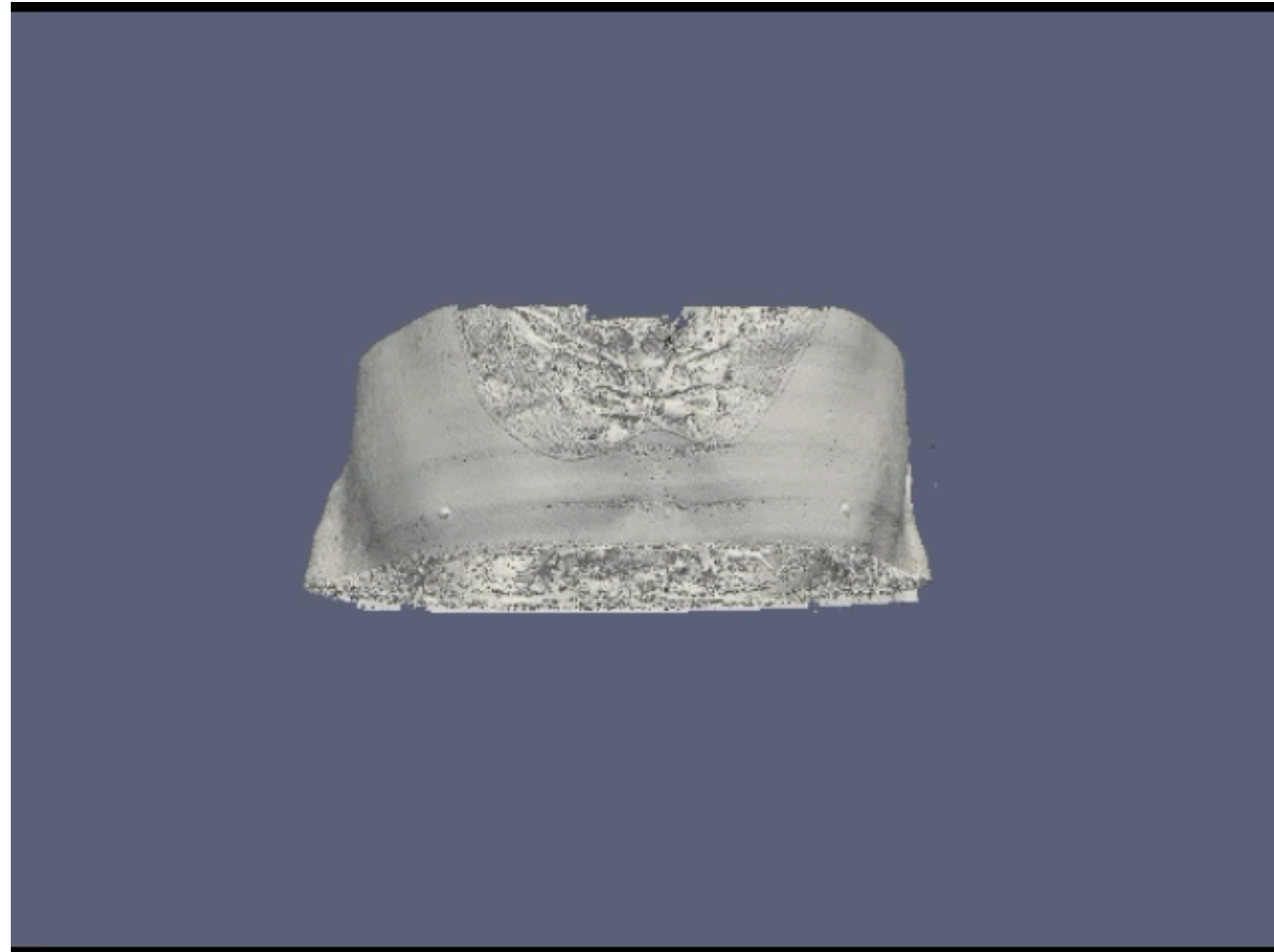
Exponential

$$\frac{dV}{dt} = aV$$



Power law

$$\frac{dV}{dt} = aV^\gamma$$



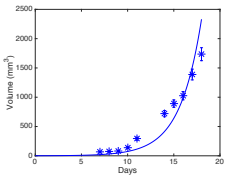
Can mathematical models be of help in oncology?



Predict and control (clinic)

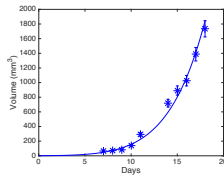
Understand (biology)

- **Theoretical** framework for description of the process
- Test different **hypotheses** and reject non-valid ones



Exponential

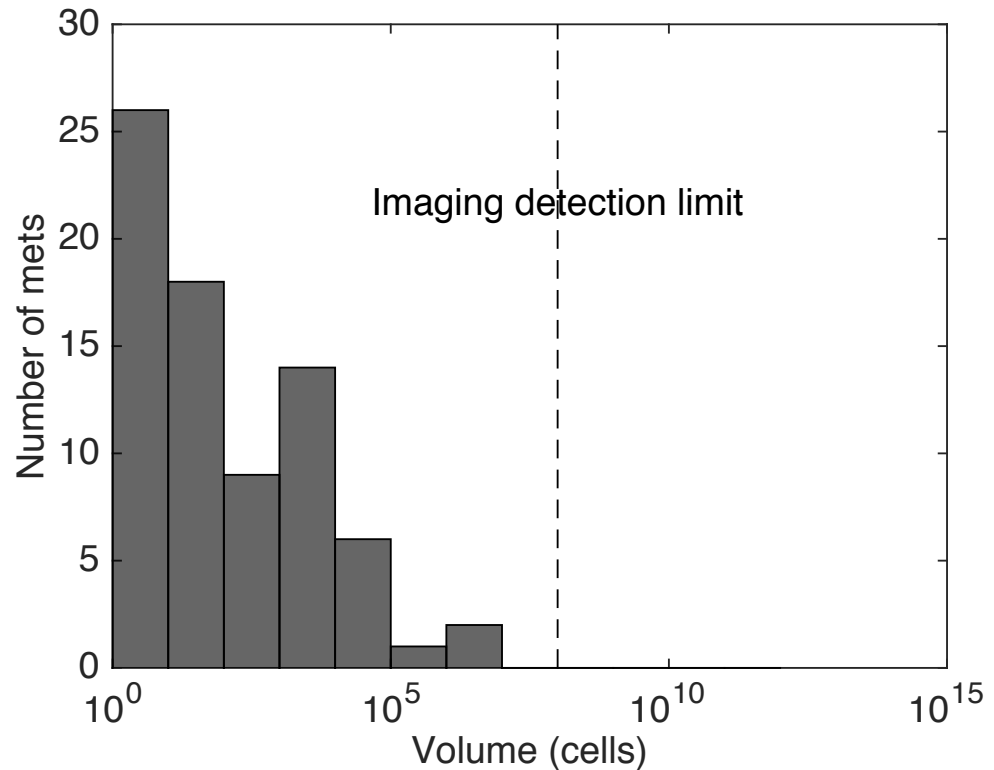
$$\frac{dV}{dt} = aV$$



Power law

$$\frac{dV}{dt} = aV^\gamma$$

- Predict **metastasis**
- **Personalize** (adjuvant) therapy



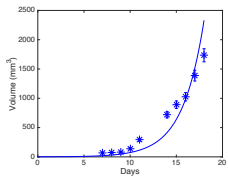
Can mathematical models be of help in oncology?



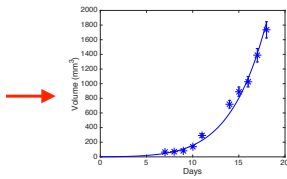
Predict and control (clinic)

Understand (biology)

- **Theoretical** framework for description of the process
- Test different **hypotheses** and reject non-valid ones



Exponential

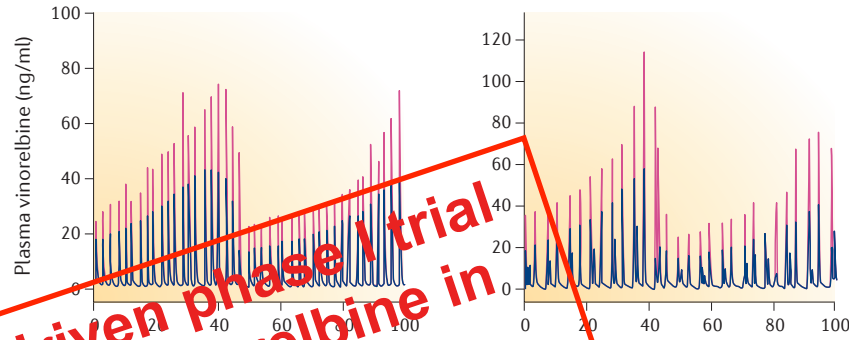


Power law

- Rational and individual design of **drug regimen**

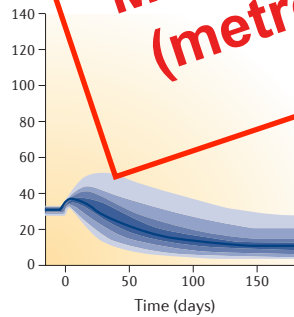
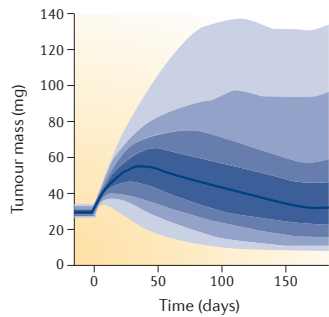
Empirical dosing
D1-D3-D5 50 mg

Model-based dosing
D1-D2-D4 60-30-60 mg

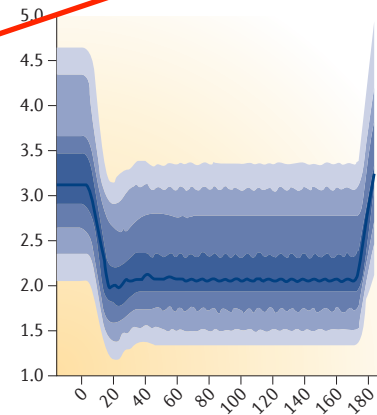
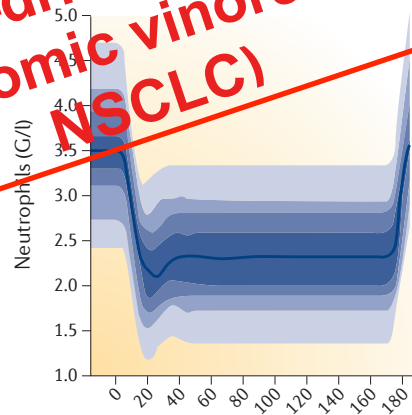


PK

Efficacy



**Modeling-driven phase I trial
(metronomic vinorelbine in NSCLC)**



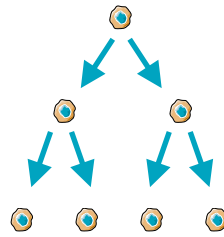
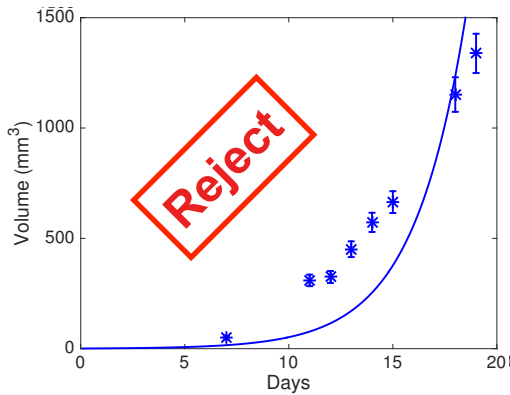
Toxicity

Tumor growth

Tumor growth

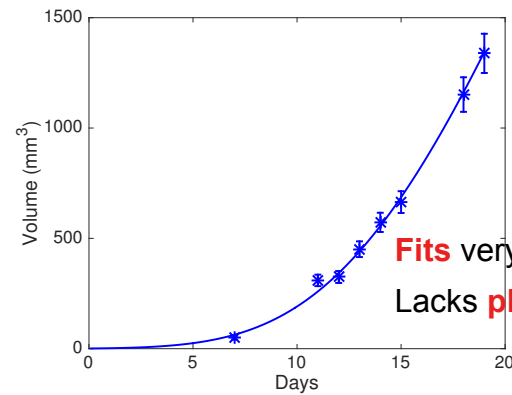
What are **minimal** biological processes able to recover the **kinetics** of (experimental) tumor growth?

Exponential



$$\frac{dV}{dt} = aV$$

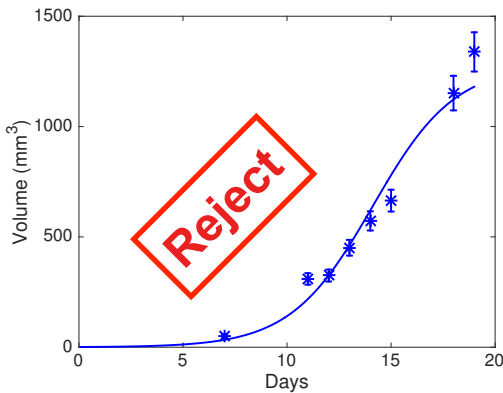
Gompertz



$$\frac{dV}{dt} = \alpha e^{-\beta t} V$$

Fits very well
Lacks **physiological** interpretation

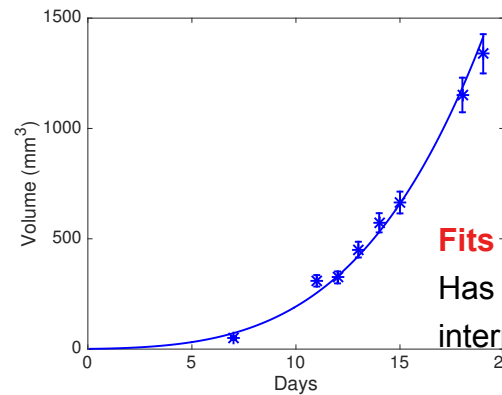
Logistic



Competition

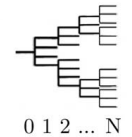
$$\frac{dV}{dt} = aV \left(1 - \frac{V}{K}\right)$$

Power law

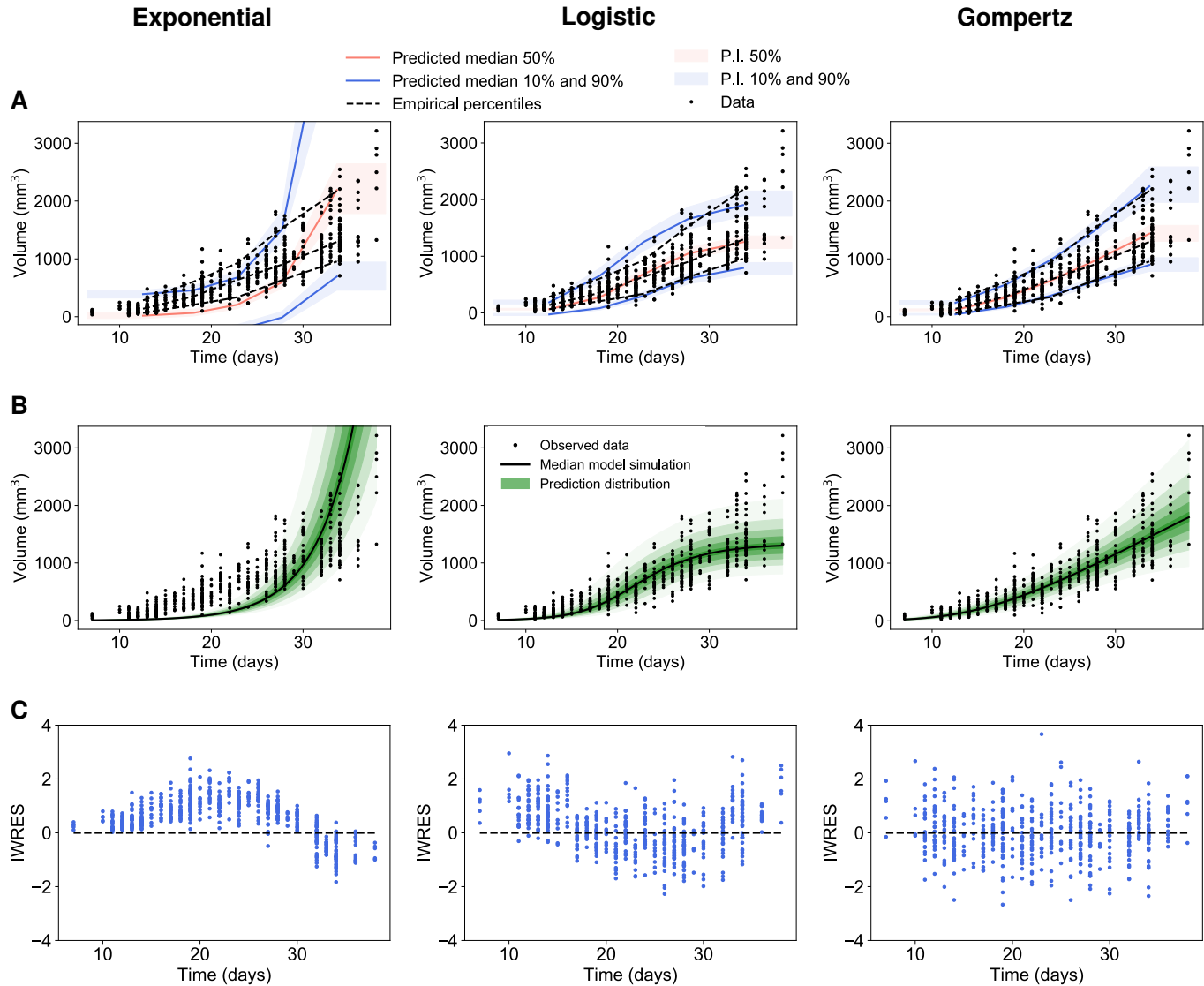


$$\frac{dV}{dt} = \alpha V^\gamma$$

Fits very well
Has **physiological** interpretation

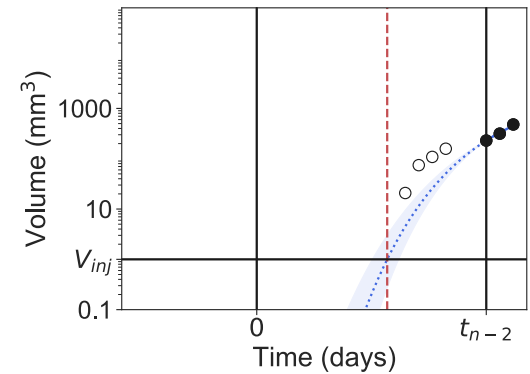
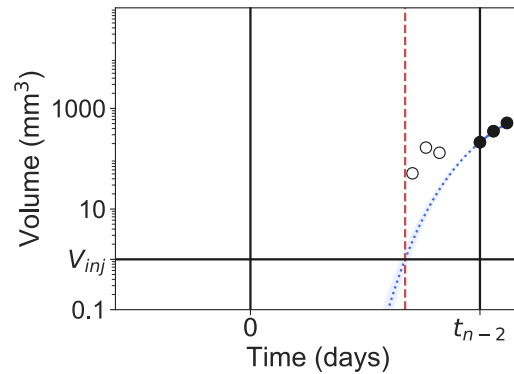
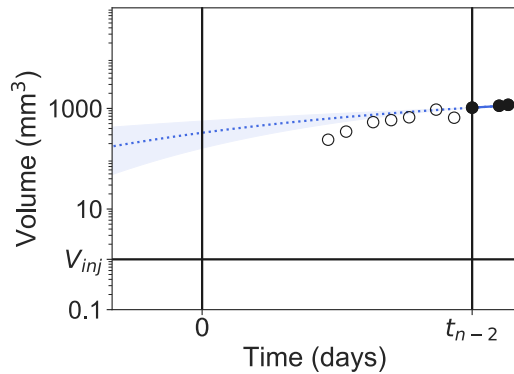


Population fit of tumor growth models

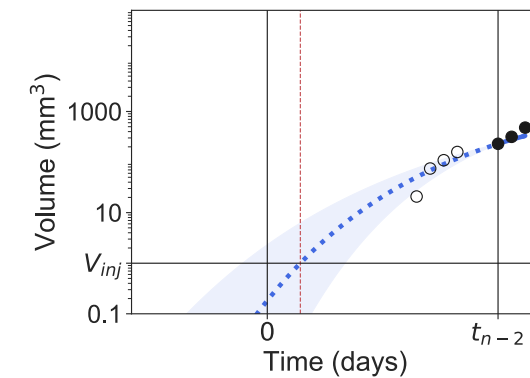
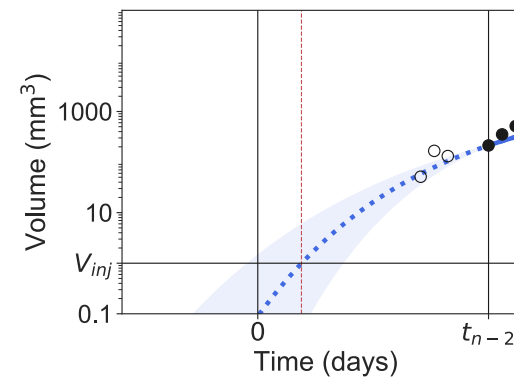
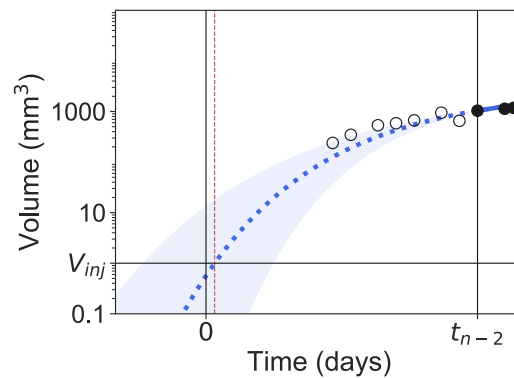


Bayesian estimation for prediction of tumor age

No a priori (MLE)



With a priori (Bayesian)

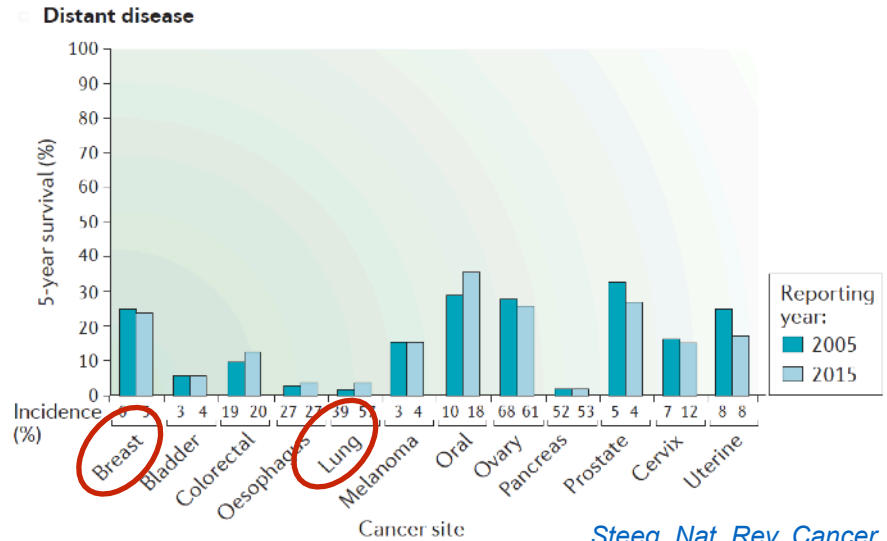
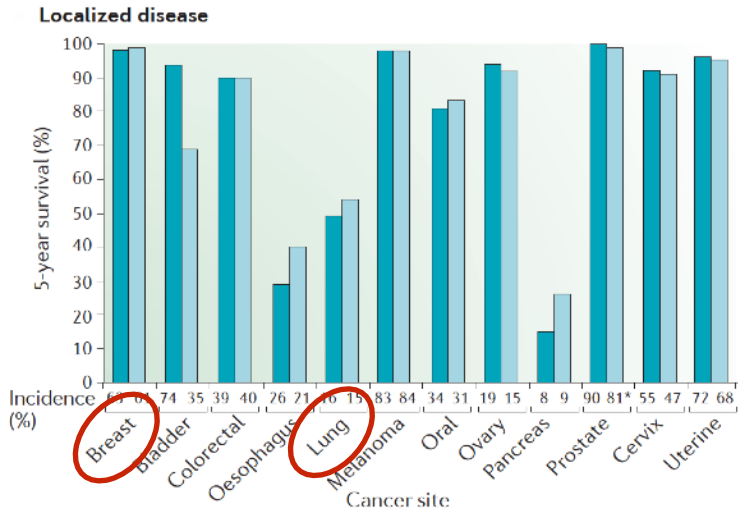


- Fit
- ⋯ Prediction
- P.I.
- Data (predictions)
- Data (fit)
- - - Predicted time

Metastasis

Metastasis (μετά = beyond, στάσιζ = place)

- Metastases are the **main cause of death** (>90%) from solid cancers *Lambert and Weinberg, Cell, 2017*



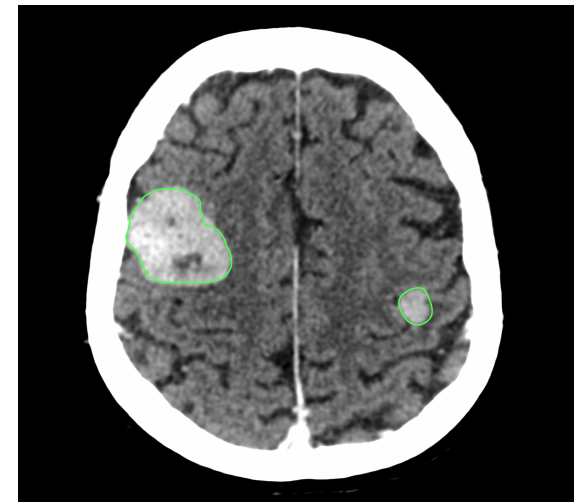
Breast

- 94% of cases are local or regional at diagnosis but 30% will relapse *Pollard, N Eng J Med, 2016*
- Estimate the amount of **residual distant disease** at diagnosis in order to **personalize** the adjuvant (chemo)-therapy
- Avoid heavy **toxicities** for low risk patients

Lung

- 57% of cases are metastatic
- Decide whether to use **whole brain radiation therapy** or just (stereotactic) surgery
- Avoid cognitive impairment of the patient

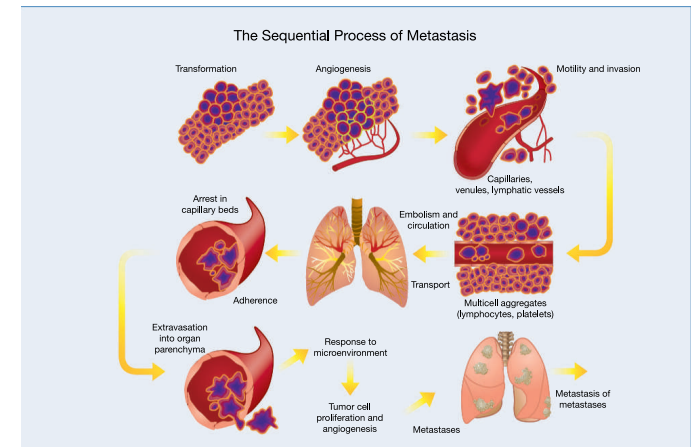
Steeg, Nat. Rev. Cancer, 2016



Institut Bergonié, Bordeaux

Some biological questions of interest to mathematical modeling

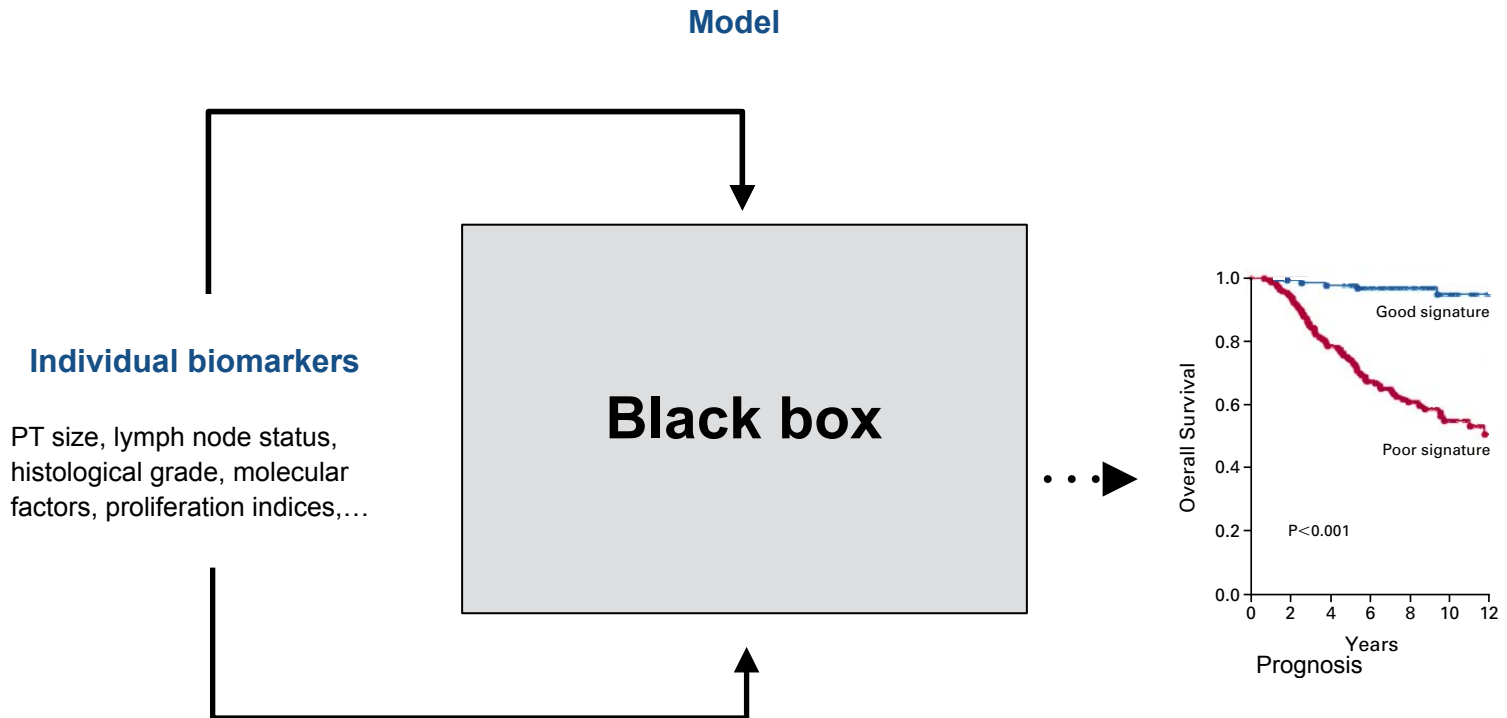
- **Minimal** model of metastatic dissemination and colonization able to reproduce the **systemic dynamics** of a solid cancer disease
- Investigate the relevance of several processes:
 - (early VS late event [Klein, Nat Rev Cancer, 2009](#))
 - (metastases of metastases [Gudem et al., Nature, 2015](#))
 - (dormancy [Chambers and Groom, Nat Rev Cancer, 2002](#))
 - **tumor-tumor interactions**
 - (cancer-immune interactions)
 - **differential effect of therapy** [Ebos et al. \(Kerbel\), Cancer Cell, 2009](#)
 - ((pre-)metastatic niche [Peinado et al. \(Lyden\), Nature, 2005](#))
 - systemic inhibition of angiogenesis [O'Reilly et al. \(Folkman\), Cell, 1990s](#)
 - (self-seeding [Norton, Nat Med, 2001](#))



Talmadge and Fidler, Cancer Res, 2010

Metastasis: a forgotten major player in modeling

- The majority of mathematical modeling efforts in oncology are focused on (primary) **tumor growth**
- Existing models are based on a statistical, **biologically agnostic**, prediction of survival



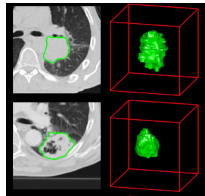
Metastasis: a forgotten major player in modeling

- The majority of mathematical modeling efforts in oncology are focused on (primary) **tumor growth**
- Existing models are based on a statistical, **biologically agnostic**, prediction of survival

Clinical data

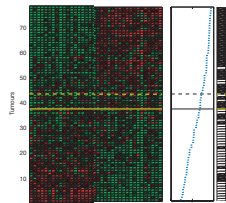
PT size, lymph node status, histological grade, molecular factors, proliferation indices,....

Imaging data (Radiomics)



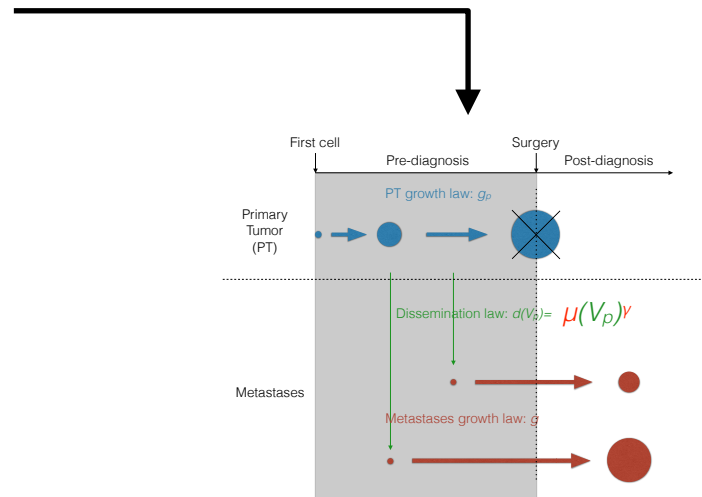
Aerts et al., Nat Commun, 2014

Molecular data (-omics)



van't Veer et al., Nature, 2002

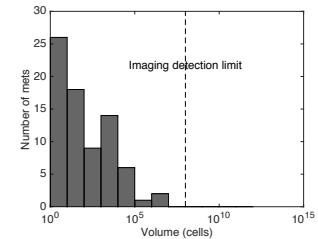
Biologically-based model



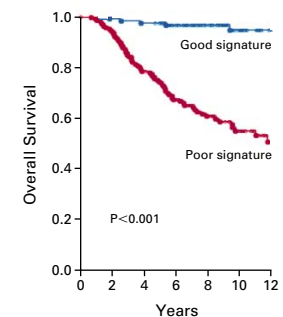
$$\frac{dV_p}{dt} = (\alpha_p - \beta_p \ln(V_p)) V_p$$

$$\begin{cases} \partial_t \rho(t, v) + \partial_v ((\alpha - \beta \ln(v)) v \rho(t, v)) = 0 \\ g(V_0) \rho(t, V_0) = \mu V_p(t)^\gamma \\ \rho(0, v) = 0 \end{cases}$$

Prediction



Diagnosis



Prognosis

Simulation and individualization of therapy

Injection (or first cell)

Surgery

Pre-surgical

Post-surgical

PT growth law: $g_p(V_p) = V_p(a_p - \beta_p \ln(V_p))$

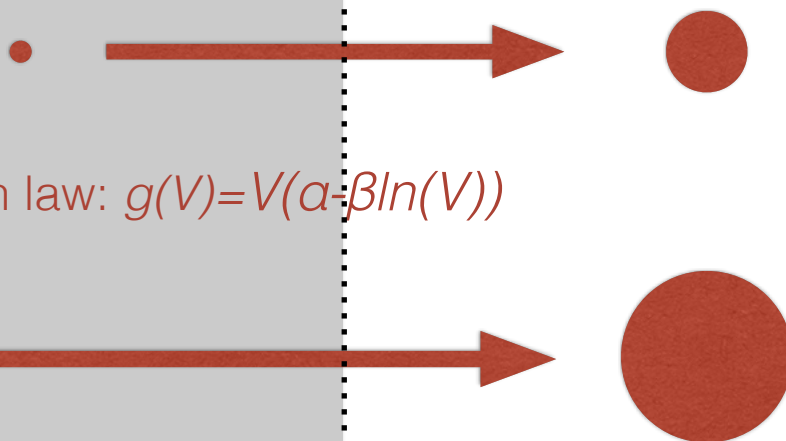
Primary
Tumor
(PT)



Dissemination law: $d(V_p) = \mu(V_p)^\nu$

Metastases

Metastases growth law: $g(V) = V(a - \beta \ln(V))$



Mathematical formalism

- Primary tumor V_p grows with rate g_p [size.day⁻¹]

$$\frac{dV_p}{dt} = g_p(V_p), \quad V_p(t=0) = V_i$$

- **Population** of metastases represented by a **density** $\rho(t,v)$ [size⁻¹] structured in **size** v

- Secondary tumors **grow** in size with rate $g(v)$

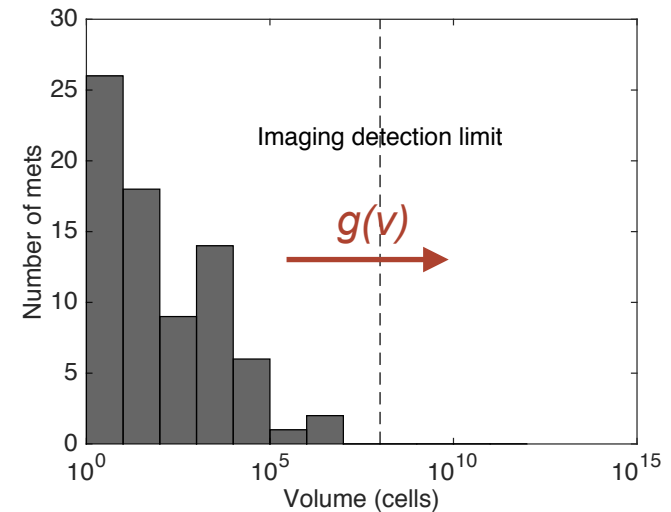
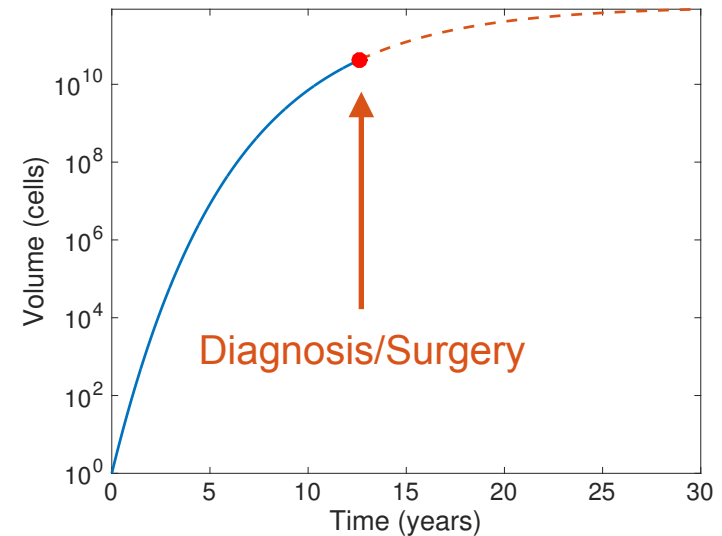
$$\partial_t \rho(t, v) + \partial_v (g(v) \rho(t, v)) = 0$$

- They are spread by the PT with **dissemination rate** $d(V_p(t))$ [day⁻¹]

$$g(V_0) \rho(t, V_0) = d(V_p(t)) \left(+ \int_{V_0}^{+\infty} d(v) \rho(t, v) dv \right)$$

→ fast computation of the metastatic burden

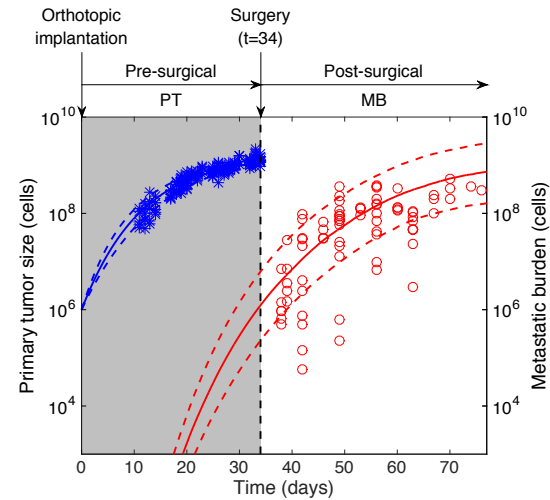
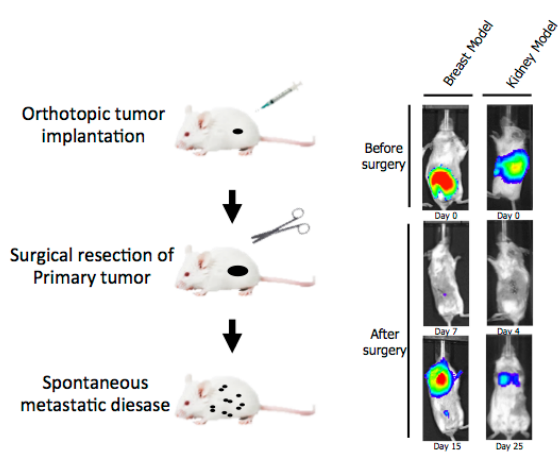
$$M(t) = \int_{V_0}^{+\infty} v \rho(t, v) dv = \int_0^t d(V_p(t-s)) V(s) ds$$





Ebos lab
Roswell Park Cancer Institute

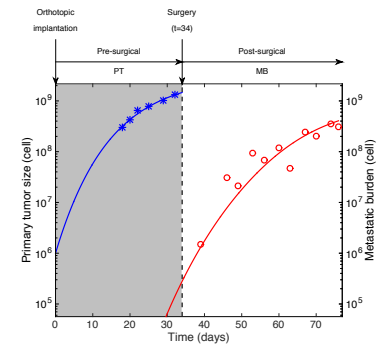
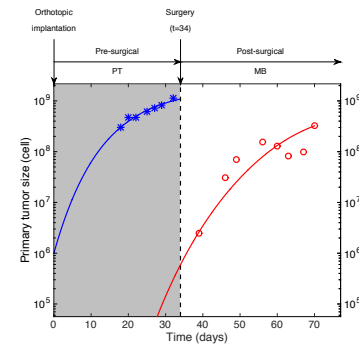
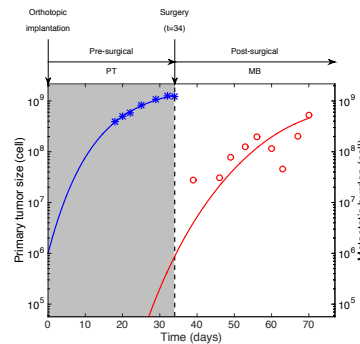
Validation on animal data



- * Data primary tumor
- Median model primary tumor
- - - 10th and 90th percentiles model primary tumor
- Data metastatic burden
- Median model metastatic burden
- - - 10th and 90th percentiles model metastatic burden

Nonlinear **mixed-effects**
statistical model for inter-
animal variability

$$\theta^i = \theta_{pop} + \eta_i, \quad \eta_i \sim \mathcal{N}(0, \omega^2)$$



⇒ **same growth** for PT and mets: $\alpha_p = \alpha$, $\beta_p = \beta$

Differential effects of anti-angiogenic therapies between primary tumor and metastases

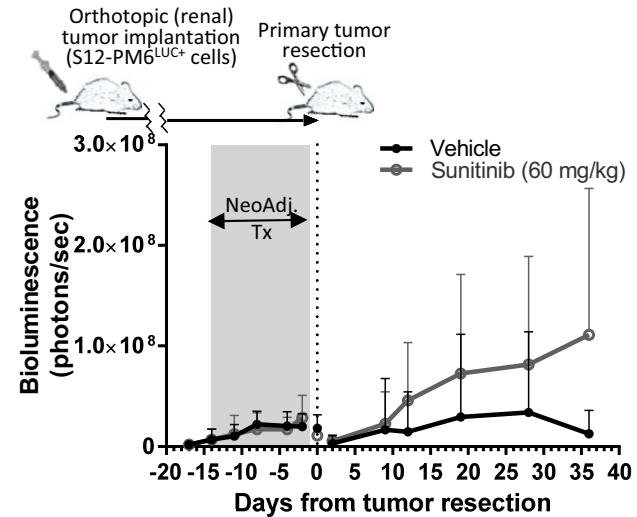
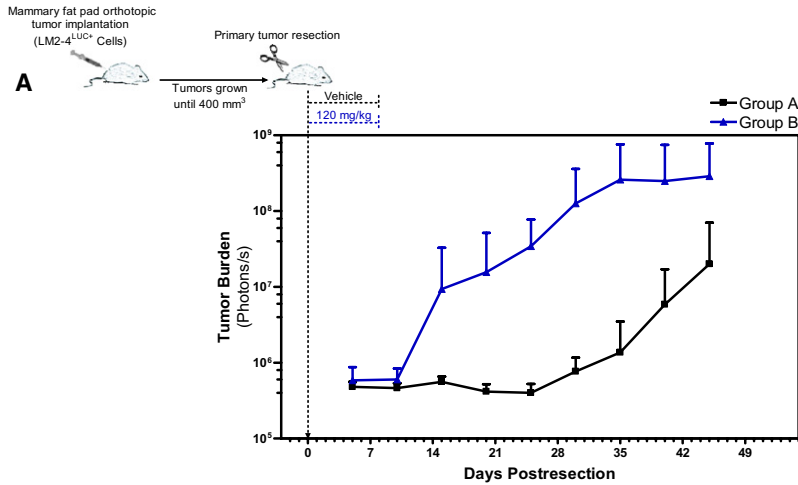


Accelerated Metastasis after Short-Term Treatment with a Potent Inhibitor of Tumor Angiogenesis

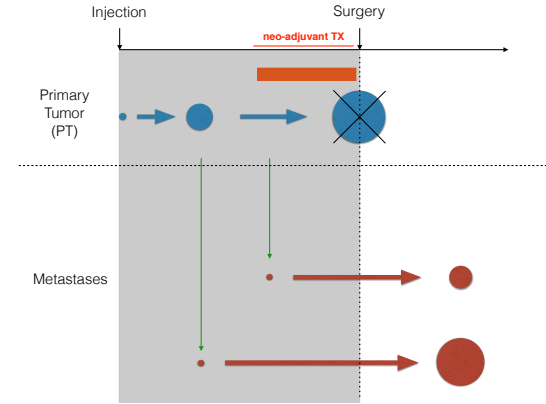
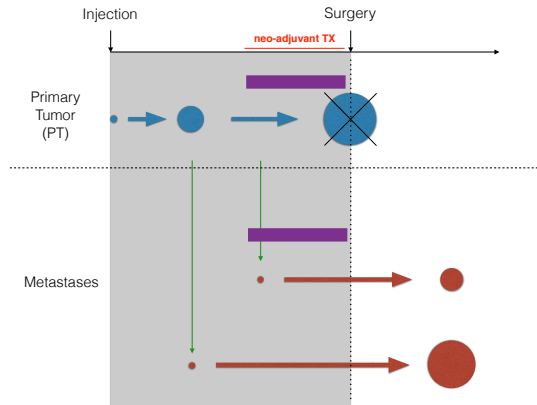
John M.L. Ebos,^{1,2} Christina R. Lee,¹ William Cruz-Munoz,¹ Georg A. Bjarnason,³ James G. Christensen,⁴ and Robert S. Kerbel^{1,2,*}

Neoadjuvant antiangiogenic therapy reveals contrasts in primary and metastatic tumor efficacy

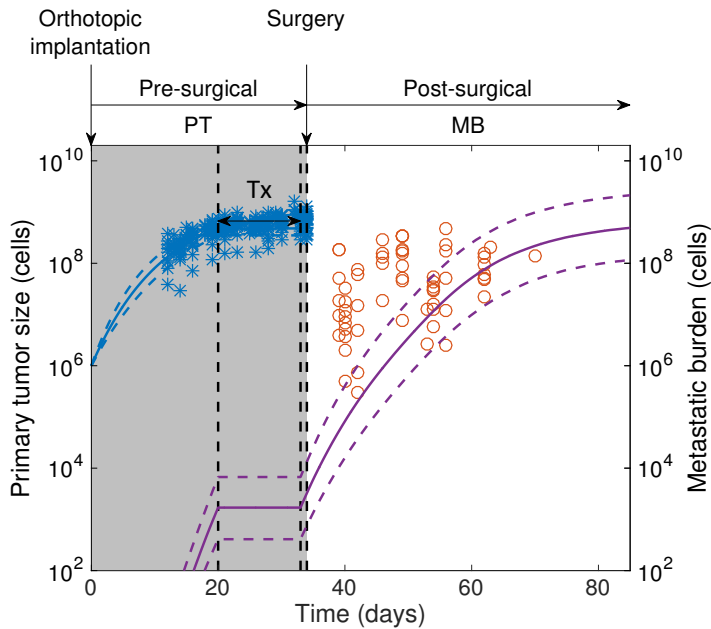
John M L Ebos^{1,2}, Michalis Mastroi¹, Christina R Lee², Amanda Tracz¹, John M Hudson², Kristopher Attwood³, William R Cruz-Munoz², Christopher Jedszko², Peter Burns^{2,4} & Robert S Kerbel^{2,4}



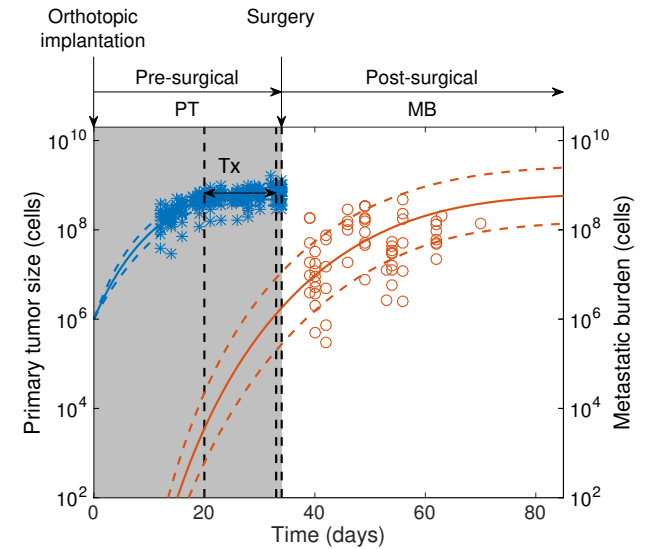
Testing hypotheses for neo-adjuvant TKI effect



or



- ★ Data PT
- Data MB
- Median PT
- Median MB
- - - 10th and 90th percentiles PT
- - - 10th and 90th percentiles MB
- simulation of therapy on metastases



Clinical application - Brain Metastasis from NSCLC