Data Visualization and Effective Communication

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Data Visualization: Essential for EDA and Beyond

EDA: Exploratory Data Analysis

Should be standard first step of any statistical analysis – simple tools such as boxplots, scatterplots, histograms, etc. as advocated by Tukey and others.

A large literature on this side of the equation, including principles of good statistical data visualization (Wainer, Tukey, Cleveland, Tufte . . .).

Simple examples bring the message home even to undergraduates or others with limited experience.

Example: Anscombe Data Sets

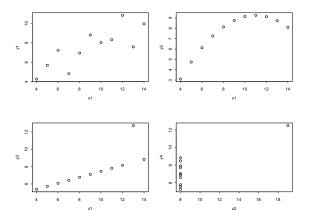
| 1-3 | 1 | 2 | 3 | 4 | 4 |
|-----|--|---|--|--|--|
| Χ | Υ | Υ | Υ | Χ | Υ |
| 10 | 8.04 | 9.14 | 7.46 | 8 | 6.58 |
| 8 | 6.95 | 8.14 | 6.77 | 8 | 5.76 |
| 13 | 7.58 | 8.74 | 12.74 | 8 | 7.71 |
| 9 | 8.81 | 8.77 | 7.11 | 8 | 8.84 |
| 11 | 8.33 | 9.26 | 7.81 | 8 | 8.47 |
| 14 | 9.96 | 8.10 | 8.84 | 8 | 7.04 |
| 6 | 7.24 | 6.13 | 6.08 | 8 | 5.25 |
| 4 | 4.26 | 3.10 | 5.39 | 8 | 5.56 |
| 12 | 10.84 | 9.13 | 8.15 | 8 | 7.91 |
| 7 | 4.82 | 7.26 | 6.42 | 8 | 6.89 |
| 5 | 5.68 | 4.74 | 5.73 | 19 | 12.50 |
| | X 10 8 13 9 11 14 6 4 12 7 | X Y 10 8.04 8 6.95 13 7.58 9 8.81 11 8.33 14 9.96 6 7.24 4 4.26 12 10.84 7 4.82 | X Y Y 10 8.04 9.14 8 6.95 8.14 13 7.58 8.74 9 8.81 8.77 11 8.33 9.26 14 9.96 8.10 6 7.24 6.13 4 4.26 3.10 12 10.84 9.13 7 4.82 7.26 | X Y Y Y 10 8.04 9.14 7.46 8 6.95 8.14 6.77 13 7.58 8.74 12.74 9 8.81 8.77 7.11 11 8.33 9.26 7.81 14 9.96 8.10 8.84 6 7.24 6.13 6.08 4 4.26 3.10 5.39 12 10.84 9.13 8.15 7 4.82 7.26 6.42 | X Y Y Y X 10 8.04 9.14 7.46 8 8 6.95 8.14 6.77 8 13 7.58 8.74 12.74 8 9 8.81 8.77 7.11 8 11 8.33 9.26 7.81 8 14 9.96 8.10 8.84 8 6 7.24 6.13 6.08 8 4 4.26 3.10 5.39 8 12 10.84 9.13 8.15 8 7 4.82 7.26 6.42 8 |

Analysis of the Anscombe Data Sets

Basic summary statistics of all four data sets are the same:

- mean of X in both cases is 9;
- variance of X in both cases is 11;
- mean of Y in all four cases is 7.5;
- ▶ variance of Y in all four cases is 4.12;
- correlation between X and Y for all four data sets is 0.816;
- fitted regression line in all cases is Y = 3 + 0.5X.

The Anscombe Data Sets Plotted



The four Anscombe data sets.



ASA Guidelines on Learning Outcomes

At the Society level, what is advocated?

- Students should be able to perform data analysis: guidelines explicitly include graphical presentation of data (EDA).
- ► Students should be able to **communicate results**: guidelines include written and oral presentation skills, but no mention of data visualization.

Visualization is Part of Effective Statistical Communication

Gelman et al. (2002): use graphs not tables of data!

Tables of numbers can be (are) hard to process without careful study.

The message can often be conveyed more effectively with an appropriate plot.

This is true for presentation of research results, not just raw data.

Example 1: Someone Else

Table 1. The number of genes that change their latent states from expressed to unexpressed and vice versa. The results for all 16 bra regions are shown.

| | Period |
|-----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| | 3-4 | 4-5 | 5-6 | 6-7 | 7-8 | 8-9 | 9-10 | 10-11 | 11-12 | 12-13 | 13-14 | 14-15 |
| MFC | 0 | 10 | 92 | 515 | 359 | 132 | 114 | 90 | 45 | 9 | 0 | 0 |
| OFC | 0 | 20 | 88 | 525 | 354 | 135 | 117 | 89 | 45 | 7 | 0 | 0 |
| VFC | 0 | 16 | 72 | 524 | 356 | 134 | 114 | 91 | 47 | 7 | 0 | 0 |
| DFC | 0 | 15 | 76 | 522 | 354 | 136 | 115 | 89 | 48 | 7 | 0 | 0 |
| STC | 1 | 13 | 67 | 526 | 355 | 136 | 114 | 87 | 48 | 8 | 1 | 0 |
| ITC | 1 | 15 | 71 | 529 | 350 | 135 | 117 | 86 | 49 | 7 | 1 | 0 |
| A1C | 0 | 23 | 61 | 528 | 364 | 132 | 112 | 92 | 45 | 8 | 0 | 0 |
| IPC | 0 | 12 | 66 | 526 | 355 | 134 | 114 | 91 | 48 | 6 | 0 | 0 |
| S1C | 0 | 15 | 72 | 526 | 351 | 137 | 112 | 96 | 44 | 7 | 0 | 0 |
| M1C | 1 | 15 | 70 | 526 | 360 | 127 | 114 | 91 | 47 | 7 | 0 | 0 |
| V1C | 0 | 13 | 98 | 527 | 359 | 134 | 115 | 87 | 42 | 9 | 1 | 0 |
| AMY | 1 | 28 | 106 | 538 | 343 | 130 | 112 | 89 | 37 | 8 | 0 | 0 |
| HIP | 1 | 66 | 108 | 506 | 350 | 126 | 109 | 80 | 42 | 7 | 1 | 0 |
| STR | 1 | 34 | 72 | 511 | 347 | 115 | 114 | 79 | 45 | 9 | 0 | 0 |
| MD | 2 | 30 | 77 | 499 | 329 | 126 | 112 | 71 | 39 | 7 | 0 | 1 |
| CBC | 2 | 26 | 56 | 474 | 326 | 164 | 117 | 71 | 35 | 14 | 5 | 0 |

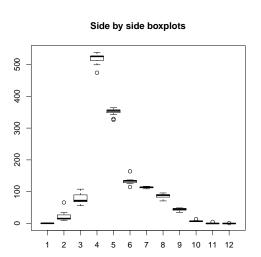
Example 1 Continued

Table shows numbers of genes differentially expressed in different brain regions over time.

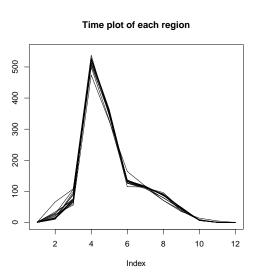
What is the take-home message of this table? Lots of numbers – are the specific values that important?

"Eyeballing" the patterns reveals commonalities. Why not a graphical presentation to make it clearer?

Example 1: Some Simple Graphical Presentations



Example 1: Some Simple Graphical Presentations



Example 2: One of My Former Students!

| MSDR | Gau-100 | Gau-150 | Gau-200 | Three-basis | Four-basis | Five-basis |
|------|---------|---------|---------|-------------|------------|------------|
| 61 | 0.1623 | 0.1622 | 0.5558 | 0.4671 | 0.7679 | 0.9611 |
| 62 | 0.2038 | 0.1905 | 0.4340 | 0.2114 | 0.5591 | 0.6899 |
| 63 | 0.2414 | 0.3821 | 0.6499 | 0.6545 | 0.9390 | 0.7945 |
| 64 | 0.3442 | 0.4448 | 0.6301 | 0.4059 | 0.6394 | 0.7436 |
| 65 | 0.2356 | 0.1928 | 0.4863 | 0.4960 | 0.5908 | 0.8987 |
| 66 | 0.5023 | 0.7017 | 0.9157 | 0.8081 | 0.9743 | 1.2199 |
| 67 | 0.3824 | 0.3794 | 0.6036 | 0.6648 | 0.8743 | 1.2336 |
| 68 | 0.2493 | 0.3406 | 0.5928 | 0.6634 | 0.5390 | 1.0485 |
| 69 | 0.8143 | 1.1373 | 1.4314 | 0.8004 | 0.9590 | 1.1643 |
| 70 | 0.1939 | 0.1482 | 0.4286 | 0.3198 | 0.4163 | 1.1748 |
| 71 | 0.1649 | 0.1678 | 0.5540 | 0.3882 | 0.6757 | 0.9063 |
| 72 | 0.2553 | 0.3342 | 0.5304 | 1.0922 | 0.5524 | 0.6870 |
| 73 | 0.4075 | 0.6141 | 0.9003 | 0.4205 | 0.8913 | 1.0452 |
| 74 | 0.2166 | 0.2648 | 0.5312 | 1.0820 | 0.6708 | 0.6594 |
| 75 | 0.3120 | 0.4904 | 0.8536 | 0.4647 | 0.9848 | 0.9745 |
| 76 | 0.1766 | 0.1160 | 0.3457 | 0.2793 | 0.3736 | 0.8522 |
| 77 | 0.8709 | 0.3477 | 0.4978 | 0.8225 | 1.2576 | 0.8071 |
| 78 | 0.2349 | 0.2540 | 0.4855 | 0.6369 | 0.7949 | 0.6010 |
| 79 | 0.6453 | 0.5982 | 0.9221 | 0.8624 | 0.9046 | 0.9034 |
| 80 | 0.2405 | 0.3073 | 0.5337 | 0.4678 | 0.6635 | 1.0207 |
| 81 | 0.3252 | 0.4411 | 0.7044 | 0.6559 | 1.1675 | 0.8254 |
| 82 | 0.4240 | 0.2898 | 0.3791 | 0.6646 | 0.8815 | 0.5478 |
| 83 | 0.1954 | 0.1831 | 0.6250 | 0.2075 | 0.5067 | 0.8635 |
| 84 | 0.4911 | 0.6099 | 0.7161 | 0.9085 | 1.2724 | 0.7338 |
| 85 | 0.2792 | 0.4200 | 0.6602 | 0.3675 | 1.1654 | 1.2136 |
| 86 | 0.2607 | 0.1908 | 0.3377 | 0.5706 | 0.4438 | 1.2555 |
| 87 | 0.2180 | 0.3365 | 0.5484 | 1.1003 | 0.6575 | 0.6170 |
| 88 | 0.3140 | 0.4890 | 0.7676 | 1.1869 | 0.5138 | 0.6278 |
| Mean | 0.3350 | 0.3762 | 0.6293 | 0.6311 | 0.7727 | 0.8954 |

Table 1: MSDR for different time points (61-88) under the Gaussian-type model approach and the nonparametric model approach. The difference between the two approaches is significant. See text for explanation.

Example 2 Continued

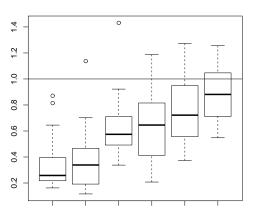
Table shows measure of error for different fitting methods, at different time points in a neuroimaging data set.

Values close to 1 indicate better performance – hard to pick out in the mass of numbers.

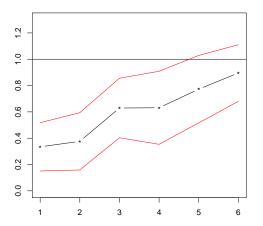
Is it necessary to look at each time point separately?

Example 2: Some Simple Graphical Presentations

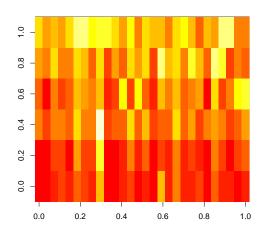
MSDR values for each method



Example 2: Some Simple Graphical Presentations



Example 2: Some Simple Graphical Presentations



Example 2 Continued

First three methods are parametric with increasing values of the parameter. Immediate conclusion: larger parameter value gives better fit.

Second three methods are nonparametric with increasing number of basis functions. Immediate conclusion: more basis functions give better fit.

Nonparametric methods give better fit overall than parametric methods.

Aside from some outliers, parametric methods are less variable in general.

Visualization Helps ... But Plot Something Meaningful!

The "flip side" of the tables versus plots dilemma is a plot for the sake of a plot.

Or, more critically – a contentless plot.

Example: A Plot With No Content

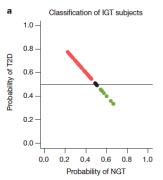


Figure 4 | Stratification of IGT women based on gut microbiota profiles. a, Use of the MGC model trained for discriminating NGT and T2D to classify IGT women (n = 49) as either NGT (green) or T2D (red).

Example: A Plot With No Content

What is plotted here?

Analysis of microbial communities in diabetic and healthy people leads to a prediction for which members of a third group will become diabetic.

Vertical axis gives probability of being Type 2 Diabetic; horizontal axis gives the probability of being healthy.

Probability of being healthy and probability of being Type 2 Diabetic add up to 1! So the graph **could only** be a straight line of slope -1.

Colors: red for individuals with probability greater than 0.5 of being Type 2 Diabetic; green for individuals with probability less than 0.5 of being Type 2 Diabetic.

Information to ink ratio of roughly zero ...



Example: A Plot With No Content

This Figure appeared in *Nature*.

Big Data Can Exacerbate the Problem

With "Big Data" visualization can be particularly challenging – traditional graphical techniques may not (typically won't be) appropriate.

One implication: A need for statisticians to develop new analysis **and** visualization tools that are tailored to the application.

Another implication: Out of desperation confusing, contentless, or misleading graphical representations of data may be published.

Huge opportunity for us to make an impact here!

Example: Why Big Data Are Challenging

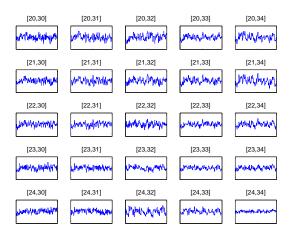
Functional magnetic resonance imaging (fMRI) data – data collected on the working of the human brain over time (on the scale of 10 minutes, often).

For a single individual:

- Multiple time points, usually on the order of several hundred.
- Multiple voxel locations, usually on the order of several hundreds of thousands.

Typical goal is to discover those voxels that are reacting to a particular task performed by the subject while in the MR scanner.

Time courses for 25 voxels

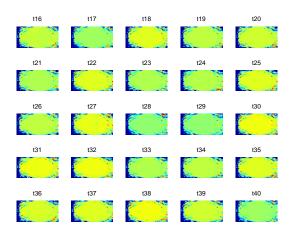


There are thousands of voxels – it's not feasible to visualize all the individual time courses **and** make sense of them.

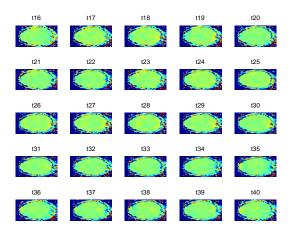
The goal is to find those voxels with time courses that match (in some way) the design of the experiment – signal changes that correlate with changes in stimulus.

Needed: visualization techniques that rely on (sufficient) dimension reduction, principal components, clustering, etc.

Images for one slice of data, 25 time points, unscaled



Images for one slice of data, 25 time points, scaled



"Brain course" images are even harder to interpret, as from time point to time point it is difficult to see the changes.

Scaling makes a big difference here.

We are left with the difficulty of visualizing masses of data – and fMRI data are small(ish) by Big Data standards.

A Final Example: Everyone Is Doing It ...

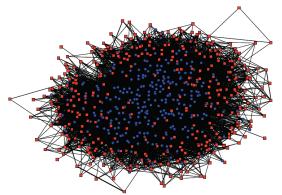


Fig. 2. Social network of whales sighted at least 20 times. Blue nodes are individuals observed lobtail feeding, red nodes are those never observed lobtail feeding. The network was laid out by spring-embedding using Netdraw (25) software.

A Final Example: Everyone Is Doing It ...

Interactions of several hundred whales via more than 70,000 sightings. Analysis of the occurrence of "lobtail" tactic of fin-slapping shows cultural diffusion.

Data collected over three decades – what information can be mined from a massive data set such as this? And how to display?

Network analysis is very popular, and especially in the Big Data setting. But what does the network graph mean for **these** data?

Conclusions

Visualization is an important part of the statistician's toolbox, both for exploratory data analysis and presentation of our own research results.

We do a pretty good job at introducing the former, but even now, are not as effective in emphasizing the latter (to our students, in our own practice . . .).

Big Data poses new and exciting challenges for data visualization and communication of large, complicated structures.

Plenty of opportunity for us as a community to make contributions in this area.