

Multi-Scale Investigations of Liquid Flow in a Fractured Basalt Vadose Zone

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This paper introduces an approach to the problem of characterizing flow and transport in a fractured basalt vadose zone. We propose the development of physically based conceptual models on a hierarchy of scales. This approach is derived from field investigations that were conducted in the vadose zone of the Snake River Plain in southeastern Idaho. Three scales of ponded infiltration tests were carried out: a Large Scale Infiltration Test (LSIT) conducted at the Idaho National Engineering and Environmental Laboratory (INEEL) (pond area $\sim 26,000 \text{ m}^2$), intermediate-scale infiltration tests (pond area 56 m^2) conducted at the Box Canyon site (near Arco, Idaho), and small-scale infiltration tests (pond area 0.5 m^2) conducted at the Hell's Half Acre Lava Flow Site (near Shelly, Idaho). Laboratory water-dripping experiments were also conducted using fracture models with constant and variable apertures. We find that, at each scale of investigation, different models for flow phenomena must be used to explain the observed behavior. These models can be used to describe the flow processes on different scales, with no apparent scaling principles evident. To characterize flow phenomena in fractured basalt, we recommend that investigations be carried out at four scales: elemental, small-scale, intermediate-scale, and large-scale. An elemental component is a single fracture or a block of homogeneous porous media. Small-scale components include one or a few fractures and the surrounding matrix. Intermediate-scale (mesoscale) components include a basalt flow with its fracture network and other parts (fracture zones, vesicular lenses, soil, massive basalt, rubble zone) of a single basalt flow. Large-scale (regional) components include multiple basalt flows and their surrounding network of rubble zones and sedimentary interbeds.

1. INTRODUCTION

Motivation and Practical Importance. For a number of years, several theoretical, experimental, and modeling approaches have been used to investigate flow and transport

phenomena in fractured rocks, primarily under saturated conditions (National Research Council, 1996). The modeling methods include continuum approaches that perform volume averaging using the effective continuum (Long et al., 1982; Peters and Klavetter, 1988; Pruess et al., 1985), double porosity (Barenblatt et al., 1960; Warren and Root, 1963), dual permeability, and multiple interacting continua (Pruess and Narasimhan, 1985) concepts, as well as fracture network models (Bear et al., 1993; Dershowitz et al., 1992; Kwicklis and Healey, 1993; Rasmussen, 1987; Smith and Schwartz, 1993). Models developed for saturated conditions cannot, however,

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describe the significant spatial and temporally varying nature of preferential flow caused by strongly heterogeneous unsaturated flow conditions (Wang and Narasimhan, 1993). A numerical modeling study by Pruess (1998) has shown that flow in an unsaturated fracture with randomly distributed hydraulic parameters does not occur as sheet flow, but rather as a dendritic structure with zones of preferential flow. When Birkholzer and Tsang (1997) simulated flow and solute transport in unsaturated media with randomly distributed hydraulic parameters, they determined that solute transport can develop a channeling effect even under conditions of steady-state water flow.

Significant efforts have been devoted to the development of alternative models for water flow and chemical transport in heterogeneous media using simple approximations like the transfer function approach (Chesnut, 1994; Jury and Roth, 1990) and percolation theory (Sahimi, 1993). Basic laws governing flow and transport in fractured rock were initially developed from theoretical studies (Snow, 1964; Witherspoon et al., 1980). Yet for most fractured rocks, and particularly the complex system of fractured basalt, it is not yet possible to develop models directly from first principles; the results of field and laboratory investigations are of primary importance, because they provide the foundations for the basic theories and models governing flow and transport.

To develop an understanding of the flow processes in heterogeneous fractured rocks from experiments, one must recognize the inherent features and limitations of the different types of measurements that can be obtained under field conditions. To monitor flow and transport in the vadose zone, we may use point-type probes, such as tensiometers, thermistors, and suction lysimeters; and geophysical imaging methods, such as seismic surveys, ground penetrating radar (GPR) and 3-D electrical resistivity tomography (ERT) (Hubbard et al., 1997; Majer et al., 1997; Peterson and Williams, 1997). The point-type probes may or may not intersect single fractures. Responses from multiple probes must be combined using either deterministic or stochastic models to develop a macro-scale conceptual model of the flow system (Yeh et al., 1985). The shortcoming of point-type probe measurements is the difficulty of combining their responses in a meaningful way, such as integrating or volume averaging responses from a number of point measurements, especially when the practicalities of an investigation do not allow for a sufficient number of measurement locations. Geophysical imaging methods complement point-type measurements by providing a spatially averaged view of subsurface conditions. The shortcoming of geophysical methods is their lack of resolution and the difficulty of correlating electromagnetic responses, seismic velocities, etc. with the hydrogeologic parameters governing fluid flow. Neither method can be used to observe flow in single fractures or fluid movement at the fracture-matrix interface in

sufficient detail to accurately represent transport. Field measurements generally provide only average characteristics of the rock and fracture properties over space and time. The actual resolution of the measurements and the volume of rock involved in averaging remain unknown. It is also important to keep in mind that, in contrast to porous media, different geological, mechanical, and geochemical processes govern the physics of flow in fractured rocks, such as basalt. The wide variety of processes controlling flow in fractured basalt at different scales makes conventional scaling procedures in applicable.

Basaltic rocks are widely distributed in the United States and throughout the world (Korvin, 1992; Long and Wood, 1986; Tomkeieff, 1940). Our investigations were conducted in fractured basalt of the Eastern Snake River Plain in southeastern Idaho near the Idaho National Engineering and Environmental Laboratory. Contaminants of concern, such as VOCs (TCE, carbon tetrachloride, etc.) and radionuclides (Cs, Sr, U, Pu, etc.), were buried in soils overlying the basalt vadose zone or were injected directly into basalt using wells and pits. The prevailing thought at the time of burial was that contaminants would not migrate downward to the underlying Snake River Plain aquifer. However, contaminants have been found in perched water zones, interbed sediments, and the aquifer. Currently, several INEEL sites are being remediated and instrumented for long-term monitoring. It has become apparent that monitoring technologies, characterization methods, and prediction procedures developed for porous media are not sufficient when investigating fractured basalt.

Objectives. The objectives of this paper are to introduce a new approach to the multi-scale characterization of flow and transport in the fractured basalt of the vadose zone and to develop physically based conceptual models on a hierarchy of scales. We illustrate this new approach using results of field and laboratory investigations conducted in the fractured basalt near the INEEL. The results were obtained from field tests carried out at three different sites: (1) small-scale infiltration tests (ponded area 0.5 m^2) conducted at the Hell's Half Acre site (near Shelly, Idaho), (2) intermediate scale infiltration tests (ponded area 56 m^2) conducted at the Box Canyon site (near Arco, Idaho), and (3) a Large Scale Infiltration Test conducted near the INEEL Radioactive Waste Management Complex (ponded area $\sim 26,000 \text{ m}^2$). In addition to these field tests, laboratory investigations included measurements on fractured basalt cores and small-scale dripping experiments in fracture models.

The paper briefly describes the geology of the Snake River Plain basalt flows and the various processes involved in flow and transport in fractured basalts. A hierarchy of hydrogeological scales is described for use in constructing models and developing observational methods. A description of the results from laboratory water dripping experiments on an ele-

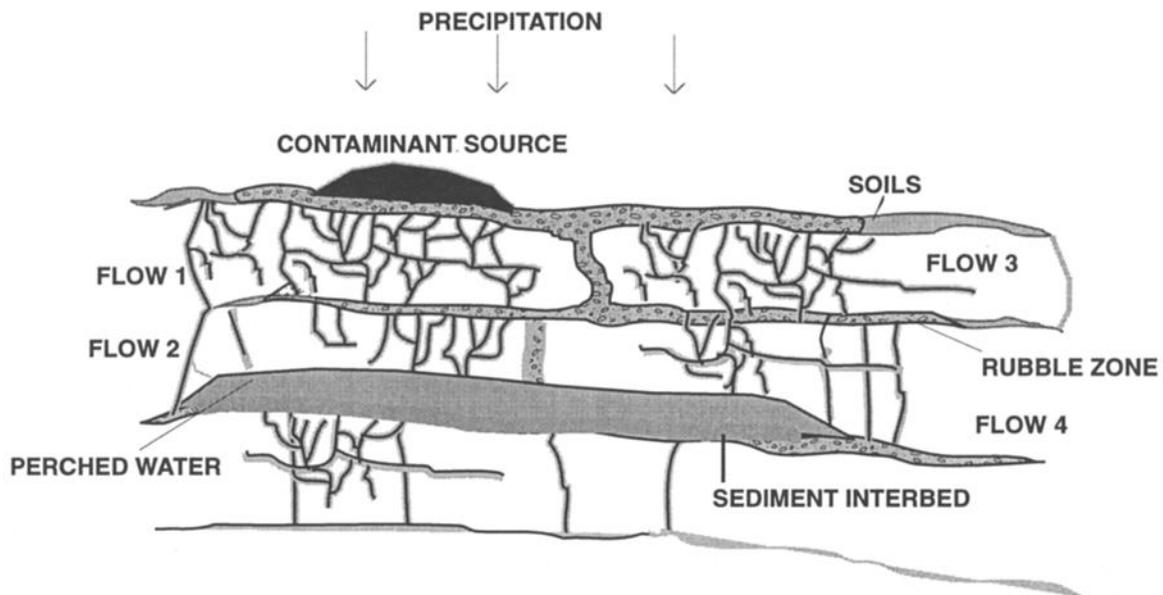


Figure 1. Schematic illustration of water flow and contaminant transport in fractured basalt, including flow through rubble zones between basalt flows and through an intra-basalt flow fracture pattern. Note that perched water zones are formed above the sedimentary layer.

mental scale is followed by an interpretation of the results from the three field infiltration tests. We conclude with a summary and present some practical applications.

2. GEOLOGY OF THE SNAKE RIVER BASALT

2.1. General Information

The Snake River Plain is primarily composed of fractured Quaternary basalts, inter-layered with sedimentary deposits (Knutson et al., 1993; Lindholm and Vaccaro, 1988). Multiple basalt flows (Figure 1) within a flow unit were formed by closely related eruption events (Lindholm and Vaccaro, 1988). Individual basalt flows are typically highly fractured, with a thickness that ranges from less than 1 m to more than 30 m, and an areal extent of up to several thousand square meters. Fracturing was caused by thermal contraction as the flow cooled and formed polygonal, often hexagonal, columns (Korvin, 1992). The upper portion of the flow is usually densely fractured, even rubblelized (Grossenbacher and Faybishenko, 1995; Lore, 1997), as a result of exposure to the atmosphere, which produced an increased cooling rate. Therefore, fracture density decreases toward the center of the flow. The lower half of the flow contains fewer fractures because of a slower cooling rate. When the basalt columns were exposed to weathering over geologic time, their surfaces weathered to breccia and were often covered with sediments that separated the flow units (Welhan and Reed, 1997). Sedimentary interbeds may have a significant lateral extent (often exceeding that of the

individual basalt flows) and their thickness ranges from a few centimeters to as much as 15 m. Geophysical logging suggests that the total thickness of the basalt in the Snake River Plain may exceed three kilometers. In the region near INEEL, the depth to the water table of the regional aquifer ranges from 60 to 200 m.

The unusually complicated geometry of basalt flows with wide contrasts in the permeability of dense basalt and highly fractured rubble zones has raised concerns over how such systems should be characterized. For the Columbia basalt flows in the State of Washington, the Department of Energy (1986) has identified four domains for basalt flows: (a) the domain of a single fracture; (b) the domain of multiple fractures within the entablature and colonnade; (c) the domain of entablatures, colonnades, and flow tops; and (d) the domain of multiple basalt flows. Note that Domains a, b, and c are restricted to a single flow. We have found this classification useful for examining the basalts of the Eastern Snake River Plain, and we have used it in developing the concept of a hierarchy of hydrogeological scales.

2.2. The Research Sites

Hell's Half Acre Site. The site is located within the Hell's Half Acre (HHA) Lava Field in southeastern Idaho. The site consists of an overhanging basalt block on the edge of a collapsed lava tube. The basalt is moderately vesicular to dense, with a single fracture exposed on the surface of the block. The fracture bifurcates in the lower part of the block, resulting in

two fracture traces on the underside. A horizontal fracture, which intersects the vertical fracture, is exposed on the face of the block, approximately 25 cm from the underside. The physical layout of the site permitted access to the top, front, and underside faces of the basalt block, thus allowing the implementation of detailed instrumentation to collect data on both infiltration and outflow rates from the fracture. Access to the underside also allowed for collection of time intervals between drips falling from discrete locations along the fracture, which were then used in an analysis of chaotic behavior.

Box Canyon Site. The Box Canyon site is located in the Eastern Snake River Plain near the INEEL (Long et al., 1995). Minimal soil cover and a nearby cliff-face exposure provide an excellent opportunity to study relationships between the fracture geology and the hydrogeologic response to infiltration tests. The surface of the Box Canyon site consists of exposed weathered basalt and soils (clays and silts), which infill the near-surface fractures and basalt column joints (Engelder, 1987). The depth to the regional aquifer is about 200 m at the Box Canyon site, with a perched water zone located at a depth of about 20 m. Along the cliff face, about 30m from the infiltration pond, two distinct basalt flows with a rubble zone between them are exposed. The fractured basalt vadose zone is comprised of the following geological components: a surface sedimentary layer including basalt rubble, upper vesicular zones with numerous near-surface soil-infilled fractures, massive basalt, vertical and sub-vertical column-bounding joints, horizontal and subhorizontal fractures, central fracture zone, lower vesicular zone, and underlying rubble zone [Faybishenko et al., 1998].

Large Scale Infiltration Test Site. The LSIT site is located 1.4 km south of the Radioactive Waste Management Complex (RWMC) at the INEEL. The RWMC includes one of the largest subsurface waste disposal facilities in the DOE complex. Past disposal of low-level, mixed, and transuranic radioactive wastes occurred by direct discharge or burial in shallow, unlined pits and trenches within the surficial sediments. Flooding of the RWMC has occurred three times in the past, potentially increasing the downward mobility of the subsurface contaminants. The time required for contaminant migration to reach the aquifer is fundamentally significant to management decisions regarding remediation options.

In 1994, the INEEL conducted the LSIT to investigate hydrologic properties of the vadose zone basalts. The vadose zone thickness near the RWMC is about 190 m. The LSIT site consists of a bermed basin 183 m in diameter, which contained 32 million liters of water during the test. Beneath the basin is a thick sequence of stacked basaltic lava flows with the first major interbed at a depth of 55 m. A total of 70 wells were drilled in 16 nested clusters and in concentric rings about the basin. Four clusters were situated in the basin, the first concentric ring was at 15 from the basin perimeter, the second ring was at 91 m and the third at 230 m. Most of the wells terminated in the sedimentary interbed. Therefore, the LSIT

test investigated the hydrologic properties of a hypothetical "cylinder" of basalt that is 55 m thick and 183 m in diameter.

3. HIERARCHY OF HYDROGEOLOGICAL PROCESSES

3.1. Flow Processes and Monitoring Techniques for Different Scales

In our investigations, we have found that different conditions affect flow processes in fractured basalt at different scales. Regional groundwater flow through the aquifer is commonly studied on a regional scale, where observation wells are thousands of meters apart and model domains encompass hundreds of square kilometers. At this scale, the aquifer is highly transmissive and vertically anisotropic, with nearly all the permeability arising from the network of rubble zones surrounding individual basalt flows. Bruno et al. (1992) found that fractal models can describe the shape of basalt flows. Pumping tests have revealed that the horizontal permeability is higher than the vertical because of the large aspect ratio of individual basalt flows (Welhan and Reed, 1997). Because of anisotropy, large-scale infiltration may lead to lateral spreading of infiltrating water. The sedimentary interbeds are of relatively low permeability and may act as aquitards for perched water zones, in which contaminants can accumulate.

In contrast, at the intermediate scale, we may be interested in a site that has neither a network of rubble zones to provide high permeability flow paths nor a sedimentary interbed to block flow. At this scale, we investigate the intra-basalt flow fracture pattern. Figure 2 shows a photograph of the basalt outcrop at the Box Canyon site and the corresponding lithological cross-section, which identify the main geological features of the vertical section. These features include a flow-top breccia, vesicular and massive basalt layers, a central fractured zone, a rubble zone, and vertical and horizontal fractures (Faybishenko et al., 1998). During infiltration from rainfall and snowmelt, sediment particles have migrated into the subsurface and accumulated in both vertical and horizontal fractures to a depth of at least 2-3 m. As water moves through these soil-filled fractures, it can be imbibed into the adjacent porous, vesicular and dense basalt matrix. Water may also flow laterally in the vesicular layers and the central fractured zone. Below the central fractured zone, the downward flow is more restricted because of the wide spacing of fractures in the lower part of the basalt flow. Figure 2 shows the presence of dead-end, nonconductive fractures, which are difficult, if not impossible, to recognize from point-type measurements in boreholes. Contaminants can be trapped in these dead-end fractures and on top of horizontal fractures followed by diffusion into the basalt matrix.

Because fractured basalt is characterized by drastic differences in permeability between fractures and matrix, the results of hydraulic tests depend on the scale that is affected by these field or laboratory experiments. For example, if we take a core

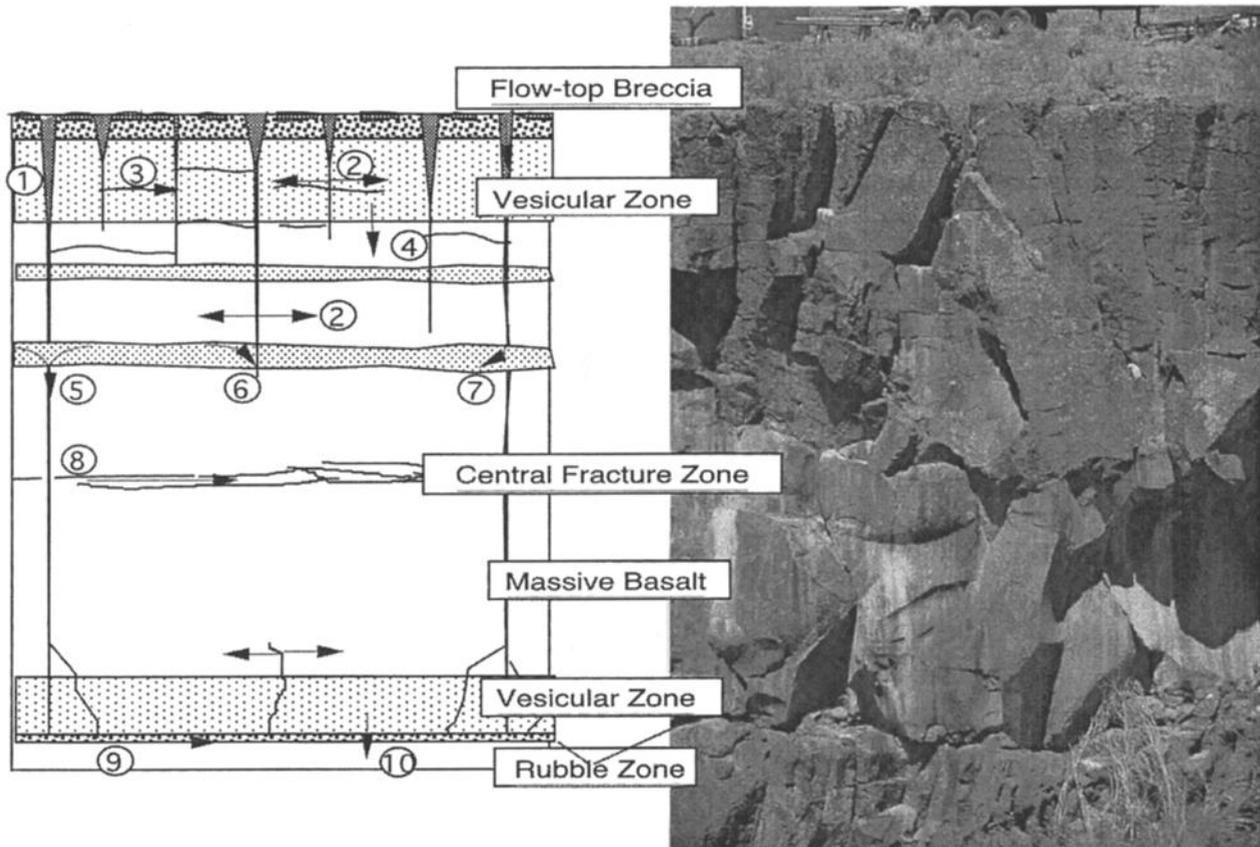


Figure 2. Schematic illustration of geological features and processes of water flow and chemical transport in fractured basalt (left): 1-flow through near-surface soil-infilled fractures, 2-fracture-to-matrix diffusion, 3-flow in a horizontal fracture connecting vertical fractures, 4-vesicular basalt-to-massive basalt diffusion, 5-funneling effect, 6-vesicular basalt-to-nonconductive fracture diffusion, 7-conductive fracture-to-vesicular basalt flow and diffusion, 8-lateral flow and advective transport in the central fracture zone, 9-lateral flow and advective transport in the rubble zone, and 10-flow in the underlying basalt flow, and photo of the Box Canyon cliff face 30m for the field site (right). The depth to the rubble zone is 10m.

containing a fracture, the permeability may be very high, but the permeability of this fracture when determined under field conditions may appear to be much less, because the fracture may not be connected to the main water pathway. In addition to the effects of the flow geometry and lithology, the flow processes in the vadose zone are also controlled by variations in moisture content and permeability of both the fractures and matrix (Mantoglou and Gelhar, 1987a,b). Because the relationship between moisture content and permeability of partially saturated rocks is nonlinear (Pruess and Tsang, 1990; Persoff and Pruess, 1995), the flow processes in the vadose zone are also nonlinear. It is known from the theory of nonlinear dynamics that a combination of several nonlinear processes may lead to chaotic variations of the system parameters (Abarbanel, 1996; Tsonis, 1992). In such systems, small changes in initial and boundary conditions may create new macro-flow structures for different flow processes with no

parent scaling principles involved (Gleick, 1987; Haken, 1983).

Because a variety of flow and transport processes occur in different parts of the fractured basalt and rubble zones, the overall system is complex, requiring complex models to describe it. In order to obtain realistic data to develop and calibrate such models, it is necessary to use the proper instrumentation consistent with the nature of the hydrogeological processes that control the behavior of the total system. However, we face the problem of an inconsistency between the scale of measurements and the scale of flow and transport processes in fractured basalt. For example, the radius of influence for single probes (e.g., tensiometers, suction lysimeters) used to monitor flow and contaminant transport in the vadose zone is about to 30-40 cm. Obviously, this is much smaller than the rock volume being characterized. Thus, single probes used to investigate strongly heterogeneous and fractured rocks only

reveal a limited volume, and the collected data may not be representative of the total system.

As the investigated rock volume increases, additional point measurements over larger volumes may not improve the characterization of the medium. This is because the number of monitoring points is limited in a practical sense, and these points may be located in different parts of the system, which are not hydraulically connected. To determine how well the point measurements represent the system, we need additional independent information. A promising method for obtaining this information is to combine point-type measurements with geophysical methods, such as GPR and ERT. GPR can be used to determine the spatial distribution of wetted zones in basalt between boreholes that are separated from 2 to 4 m, but cannot be used in monitoring the dynamics of fast fluid flow in individual fractures (as will be shown below in Section 7).

The hydraulic properties of saturated geologic media are known to correlate with the scale of observations from the laboratory scale to thousands of meters (Dagan, 1989; Gelhar, 1993; Neuman, 1990; 1994; Molz and Boman, 1995). However, the approach used for scaling of saturated hydraulic parameters may not be applicable for the unsaturated fractured basalt, because: (1) different hydraulic processes govern flow on different scales, and (2) the scale of measurements in the vadose zone (using point-type, near-borehole, and cross-borehole measurements) is inconsistent with the scale of flow processes in the field. Heffer and Koutsabeloulis (1993) determined that despite the presence of a scaling relationship for the fracture frequency and the fracture trace lengths from single cores to thousands of meters, the scaling of hydraulic properties determined for small dimensions cannot be applied to the larger dimensions. Thus, in order to provide a proper description of the processes governing flow and transport in basalt, we use a hierarchy of scales with appropriate models and methods of investigation

3.2. The Concept of a Hierarchy of Hydrogeological Scales

The concept of a hierarchy of scales for investigation of fractured rocks is based on the assumption that the whole system is composed of a number of components that behave differently on different scales. In describing flow problems in basalt, we propose a four-level hierarchy of hydrogeological components, which includes elemental, small-scale, intermediate-scale, and large-scale components. The relationship between these components is illustrated in Figure 3.

Elemental components of the flow system include a single fracture or a block of porous media (matrix). Elemental components can be studied using small laboratory cores, fracture replicas, or point-size probes under field conditions. Results of experiments on this scale can be used to describe the details of specific flow and transport processes in fractures, matrix, or fracture-matrix interactions (Ho, 1997). Some examples of these flow processes are: (1) water dripping from a fracture under field conditions in boreholes, tunnels, caves, and other

underground openings; (2) film flow (Tokunaga and Wan, 1996) and water meandering along a fracture surface in laboratory experiments (Su et al., 1998); and (3) water dripping within flow channels, or flow intermittence along a fracture surface in laboratory experiments. The size of the elemental component is from a few centimeters to 10-20 cm.

Small-scale components include a volume of rock within a single basalt flow with one or a few fractures. Results of field local experiments on this scale can be used to describe in detail some of the flow and transport processes in one or a few intersecting fractures. Small-scale infiltration experiments are conducted to investigate fracture-matrix interaction, water dripping phenomena, and small-scale averaging of flow rates and water pressures measured in fractures and matrix. The areal extent of small-scale components is approximately 0.5-1 m².

Intermediate-scale (mesoscale) components include the volume of rock within a basalt flow involving all types of fractures, including the fractured flow top, dense flow interior, the less fractured flow bottom and fractures intersecting the basalt flow and rubble zone. The results of field experiments at this scale can be used to describe volume averaged flow and transport processes within a single basalt flow. The essential issue is the study of movement in the fracture-network within a single basalt flow. We also study other basalt-flow features such as vesicular or massive basalt, fracture zones in the upper and lower fractured colonnade, and the central fractured zone or entablature. The areal extent of intermediate-scale components is approximately 10-100 m².

Large-scale (regional) components involve the volume of rock containing several basalt flows and the rubble zones between them. At this scale, we can study flow in the fracture networks and regional hydrogeological processes, which are affected by the network of vertical and horizontal rubble zones, as well as sedimentary interbeds. The areal extent of a large-scale component usually exceeds 1,000 m².

To analyze the time-series data sets obtained from monitoring water-dripping phenomena in laboratory and small-scale field infiltration tests, we use the methods of nonlinear dynamics, described below.

4. USING NONLINEAR DYNAMICS METHODS TO ANALYZE TIME-SERIES DATA SETS

A conventional method for analyzing time-series data is to conduct a Fourier type analysis, which decomposes a signal into different frequency components. This method is effective for linear systems, but the resulting frequency components may appear as noise for deterministic-chaotic functions (Abarbanel, 1996), because there are an infinite number of frequencies comprising chaotic motion. The Fourier transformation is used to analyze time-varying scalar signals with no assumption about the underlying physics of the processes. In contrast, the methods of nonlinear analysis assume that (1) the

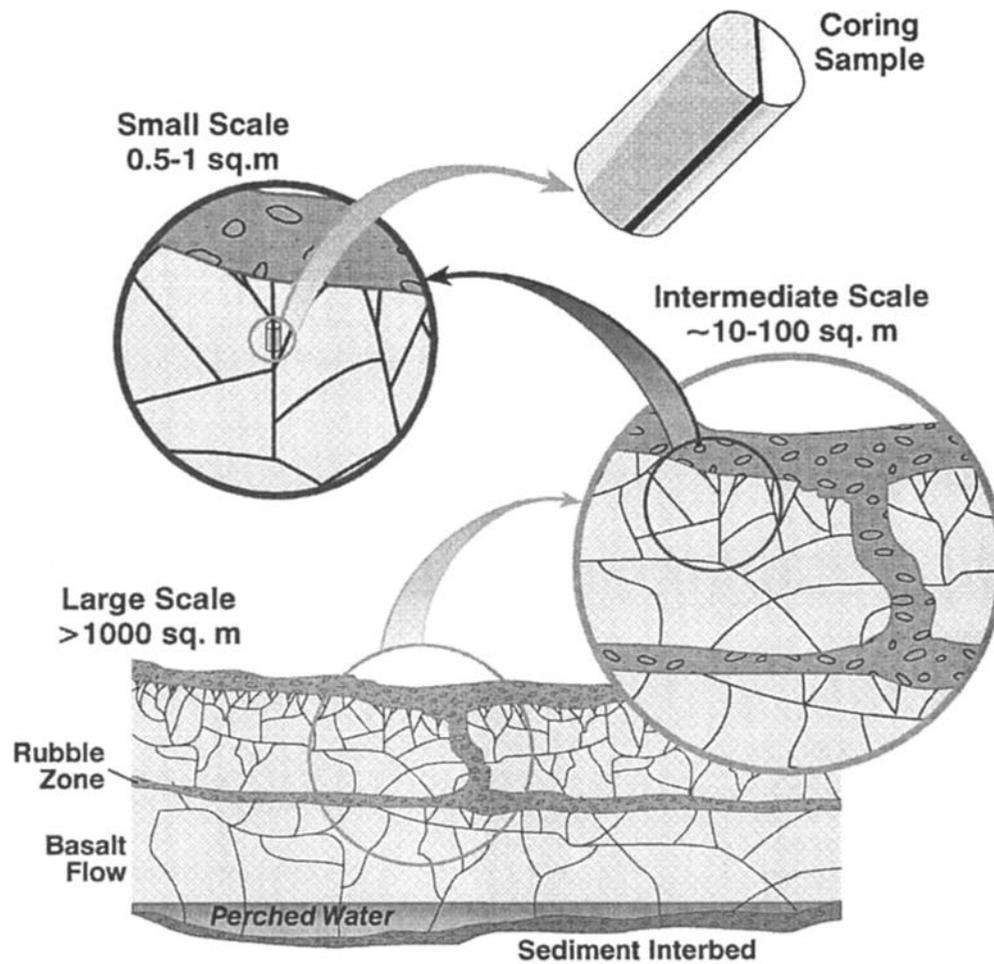


Figure 3. A four-level hierarchy of scales of hydrogeological components in fractured basalt.

time-varying function contains information about the processes affecting this function, and (2) multi-dimensional vectors describe the time evolution of the function. The space in which these vectors evolve is called a state space or phase space, for which the dimension is an integer (Abarbanel, 1996).

In unsaturated rocks, useful phase-space variables are moisture content, water pressure, and flow velocity, which depend on each other in a nonlinear fashion. Another variable, that one can measure directly in laboratory and small-scale field experiments, is a water dripping frequency. The nonlinear flow processes in the fractured rock vadose zone are subject to chaotic fluctuations, implying that trajectories through phase space may not be steady or periodic. Furthermore, because the vadose zone processes are dissipative, the volume of a phase space occupied by the trajectories decreases with time. For such a system, the basic idea behind the nonlinear time-series analysis is to reconstruct the phase-space and then plot an attractor in the phase space. The attractor is a set of points

in phase-space toward which nearly all trajectories converge (Grassberger and Procaccia, 1983). In other words, the attractor describes the typical system behavior. An attractor for a chaotic system often has a fractal structure, and it is called a strange, or chaotic, attractor (Moon, 1987).

Because the phase-space variables depend on each other, the time-series analysis of any one of those variables may give us an understanding about the physics of the whole system. Therefore, we choose a single scalar variable P (e.g., water pressure, dripping frequency) and plot its trajectory through a pseudo phase space whose dimensions are $P(t)$, $P(t+\tau)$, $P(t+2\tau)$, ... $P(t+(n-1)\tau)$. In order to plot the attractor, we need to determine the correlation time, τ , which is the time interval between data points when the relationship between the points almost vanishes, and the embedding dimension, n , of the attractor. The embedding dimension is the dimension of the pseudo phase space needed to unfold the attractor of a nonlinear system from the observation of a scalar signal. That is, it is the number of coordinates required in order that the orbits



Figure 4. Video images of a cycle of water dripping within a flow channel along a dense basalt fracture surface mated to a transparent replica of the second half of the fracture. Time is given in the left-bottom corner of each image. Water was applied at 0.33 mL/hr to the top of the fracture. Fluorescein was added to the water to promote visualization by near-UV light. The fracture was inclined at 20° from the horizontal.

composing the attractor no longer cross one another in the pseudo phase space. The method of false nearest neighbors (Kennel et al., 1992) is used to determine the embedding dimension of the attractor. Some diagnostic parameters (capacity dimension, correlation dimension, Hurst exponent, and Lyapunov exponent) are used to recognize whether the system

contains a deterministic-chaotic component in otherwise random-looking time-series data (Moon, 1987).

Chaotic phenomena are common in the fields of physics, ecology, biology, economics, geology, etc. (Tsonis, 1992). However, the claims for chaos in hydrologic systems have to be carefully assessed, because the number of observations are often limited and not sufficient to calculate diagnostic parameters of chaos (Pasternak, 1996). Despite the fact that we cannot precisely identify all factors and processes affecting the system, we can determine the system bounds within which the system is supposed to behave over long periods of time. Identifying the chaotic nature of a system enables the determination of the number of variables that must be measured to define behavior. It also indicates that for chaotic systems, which are sensitive to initial conditions, only short-term predictions of the time-trend of the data functions are possible. Long-term predictions of the time-series of the data functions are not possible, but the attractors can be used to determine the bounds of the parameters characterizing the long-term behavior of the system.

5. LABORATORY INVESTIGATIONS OF FLOW IN FRACTURE MODELS

5.1. Test Design

Water seepage within a fracture can proceed through channels that undergo cycles of snapping (dripping) and reformation under low-flow conditions even in the presence of constant boundary conditions (Su et al., 1998). Figure 4 shows a cycle of water dripping within a flow channel along a dense basalt fracture surface mated to a transparent replica of the other fracture half (Geller et al., 1996). In order to investigate the physics of this time-varying intermittent flow under laboratory conditions, we designed a series of water dripping tests within smooth-walled and rough-walled transparent fracture models having sub-millimeter apertures (Figure 5). Water was supplied at constant rate through a capillary tube inserted into the fracture models. The time variation of the water pressure at the tube entrance was measured over a range of flow rates. Video images of flow confirmed that the pressure fluctuations occurred in response to flow behavior, as drops formed and detached within the flow channel (Figure 6). Pressure data were also acquired for dripping from the tube open to atmosphere.

5.2. Test Results and Conceptual Model of Flow in Fracture Models

Figure 6 compares the time variation of pressure and corresponding attractors for the flow rate of 0.25 ml/hr for three different cases of water flow through a 0.18 mm ID capillary tube: (1) open air, (2) a constant aperture fracture model (0.35 mm separation between smooth glass plates), and (3) a vari-

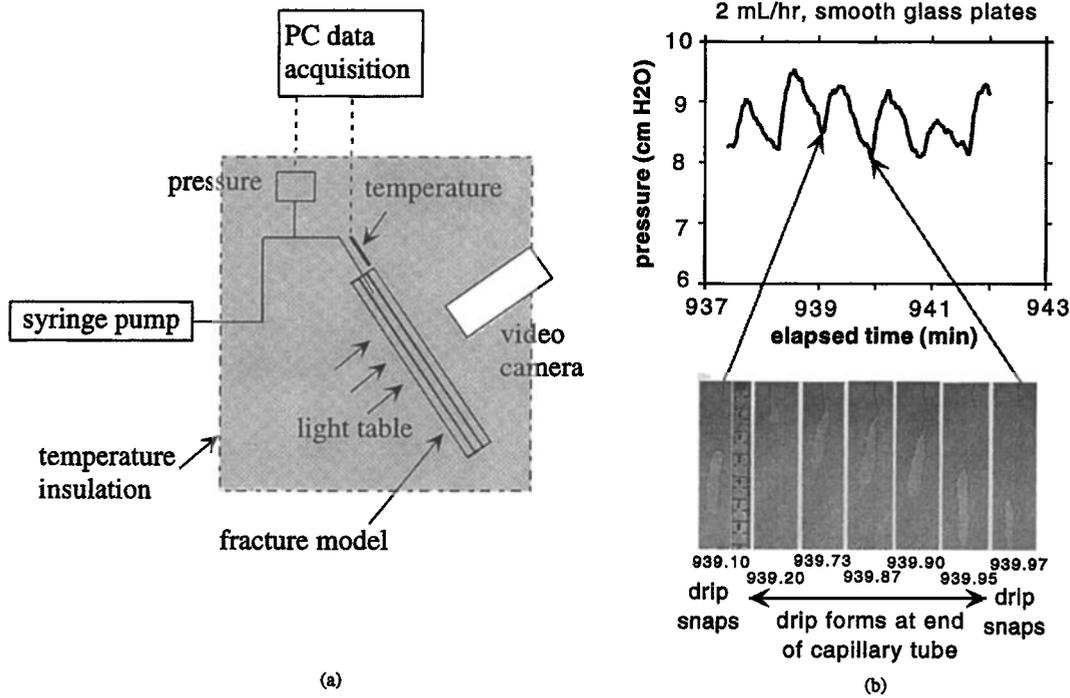


Figure 5. Experimental setup for monitoring water-dripping in fracture models: (a) The fracture model is 20 cm x 30 cm glass plate pairs, smooth or textured, separated by 0.35 mm shims; the model is inclined 60° from the horizontal; (b) Time-series of water pressure measured at the entrance to the capillary tube and corresponding video images of drip formation. Note that the water thread snaps when the pressure is minimal. We assume that the weight of the water drop overcomes capillary forces arising from the presence of the small fracture model aperture.

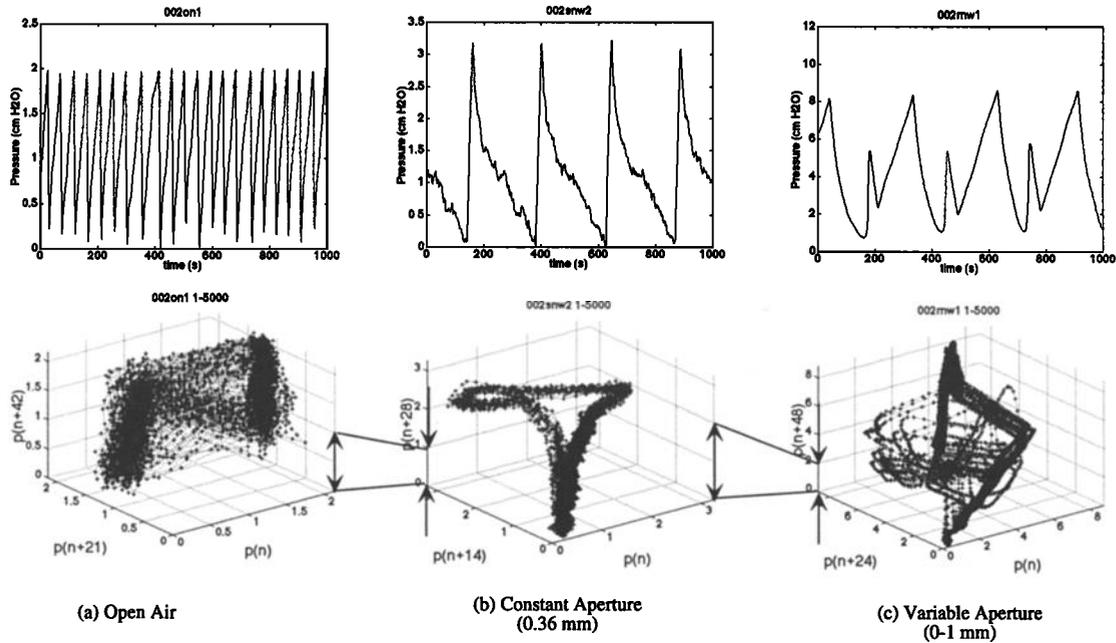


Figure 6. Time-series data (above) and attractors (below) for 0.25 mL/hr flow rate through 0.18 mm ID capillary tube: (a) Open-air drips, (b) Constant aperture, 0.36 mm, glass plate pair, and (c) Variable aperture, 0-1 mm, fracture model. As the geometry surrounding the tube becomes more complex, the magnitude of pressure fluctuations increases and the attractors change from noisy to more deterministic chaotic.

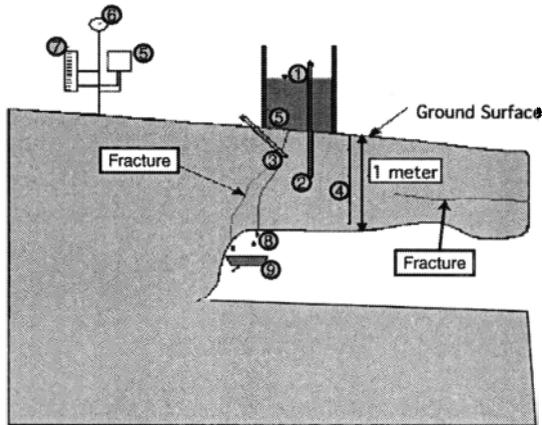


Figure 7. Design of a small-scale infiltration test at the Hell's Acre site in Idaho and the types of measurements conducted: 1-Water level and infiltration rate in the water gallery, 2-Basalt-matrix water pressure using tensiometers, 3-Fracture-matrix water pressure using tensiometers, 4-Temperature of rocks, 5-Ambient air and water temperature, 6-Barometric pressure, 7-Precipitation, 8-Outflow drip intervals, and 9-Outflow volumetric flow rate in 20x30 cm pans.

able aperture fracture model (textured-glass plates). Comparison of the attractors in Figure 6 shows a progression of the systems from noisy to more deterministic-chaotic, as the geometry surrounding the dripping water becomes more complex. Calculation of the diagnostic parameters of chaos confirms that the magnitude of the random component decreases and the contribution of the deterministic component increases from the open air, to constant aperture, to variable aperture system. Pressure data at higher flow rates (up to 10 ml/hr) and for larger diameter tubes (0.8 mm ID) had an increased random component.

These experiments show that under certain conditions, flow behavior along water channels in a fracture model has a significant chaotic component. For such systems, a deterministic-chaotic model with a random component should be used to describe flow behavior.

6. SMALL-SCALE INFILTRATION TEST

6.1. Test Design

The objective of the field investigation conducted at the Hell's Half Acre site was to evaluate flow processes on the meter scale (Podgorney et al., 1997; 1999). The research site consists of an overhanging basalt block (approximately 1 m thick and an areal extent of 2 by 3 m) on the edge of a collapsed lava tube. A single vertical fracture is exposed at the surface of the basalt block. This fracture bifurcates in the lower part of the block, resulting in two fracture traces on the underside. A horizontal fracture, which intersects the vertical fracture, is exposed on the face of the block, approximately 25 cm from the underside.

A 40 x 80 cm infiltration pond was built on the upper surface of the basalt block, surrounding the surface expression of the fracture (Figure 7). The site was instrumented to collect extensive data sets to describe both the temporal and spatial variations of the following parameters: water head in the infiltration pond, water and rock temperature, tensiometric pressures at 14 locations, barometric pressures, infiltration rates, and outflow rates as water drip intervals from 20 dripping points and as volume from 12 pans on the underside of the outcrop. The design of this test allowed us to investigate the flow processes for elemental (e.g., water dripping at individual drip points) and small-scale (e.g., flow rates at individual pans) components. The water dripping rates, or time intervals between drip events, can be used to characterize the elemental components. The area below the fracture is covered with a grid of 20 x 30 cm pans, which are used to collect the water dripping from the fracture. Each pan collected one or more drips, combining several elemental components, averaging the outflow rate from the area above it. The water is routed from the pans to bottles attached to load cells to measure the outflow. The outflow rates determined from the pans can be used to characterize the small-scale components.

During infiltration experiments, the upper boundary condition was a constant water level in the surface pond. The infiltration tests were run for 1 to 18 days. The drainage periods between infiltration tests lasted up to several weeks to allow for sufficient drying of the fracture space. Successive tests started when the water pressure in the rock was approximately -100 mbars. We can assume that under this pressure the fractures were dry, and the matrix was partially desaturated.

6.2. Test Results and Conceptual Model of Flow on a Small Scale

We assume that the drip rates collected during these tests can be used to characterize the elemental components, while the infiltration and volumetric outflow rates combined with the tensiometric pressures can be used to characterize small-scale components. In order to provide a general understanding of the flow processes, we begin with the analysis of data obtained using the infiltration and volumetric outflow rates. Typical plots of the time variations in the volumetric infiltration rate and outflow rates at five locations along the fracture on the underside of the outcrop are shown in Figures 8a and 8b. We subdivided the time of the experiment into two periods (indicated these figures).

Period 1. Immediately following the beginning of flooding, the infiltration rate increases due to the quick saturation of fractures and initially high water imbibition into the dry basalt. As water imbibes into the porous matrix, air is presumably pushed out into the surrounding fractures. In fractures, air becomes entrapped in the low aperture zones, thus blocking some flow pathways. This blockage leads to an overall decrease in the hydraulic conductivity of rocks and, consequently, to a decrease in both infiltration and outflow rates to

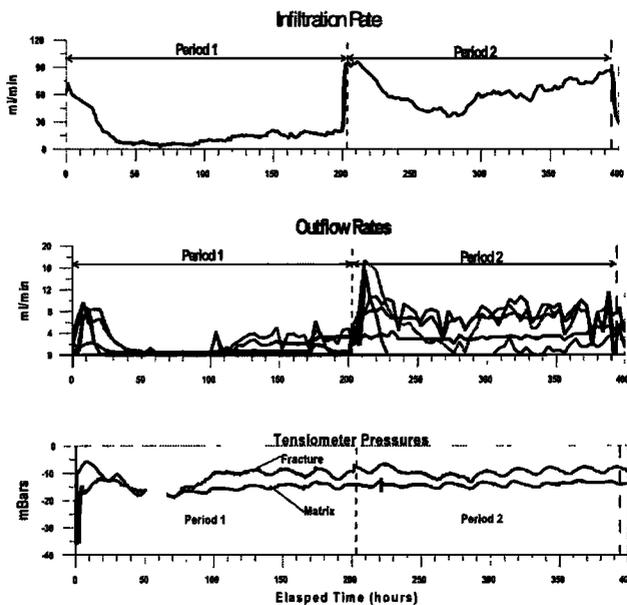


Figure 8. Results of a small-scale infiltration test: (a) Infiltration rate, (b) Outflow rates in five pans, and (c) Tensiometer fracture and matrix pressures.

minimum values at times between 50 and 100 hours (Figures 8a and 8b). Other factors that could affect the dynamic flow behavior are dissolution, colloid and particle translocation, sealing of fractures and matrix by biofilms, air pressure, barometric pressure, swelling clays, and earth tides. Figure 8b shows that the outflow rates become nearly the same at all observation locations. At this time, the water pressure measured in the fracture and matrix is practically the same (Figure 8c, tensiometers 2,4, and 5), which indicates no flow between the fracture and matrix. Note that tensiometer 9, which is located outside the footprint of the infiltration gallery, also showed a decrease in water pressure.

Subsequently, the flow rate increases, presumably as entrapped air dissolves into moving water and is removed in both free and dissolved phases. An identical flow behavior was observed in soils in the presence of entrapped air (Faybishenko, 1995). Comparison of Figures 8a and 8b shows that during Period 1, the trend and magnitude of the volumetric outflow rates are different from those of the infiltration rate. The simultaneous increase in the flow rates and tensiometric pressure (Figure 8c) supports the hypothesis of increasing rock saturation. The flow rates increased until the saturation reached a critical value, and most likely some flow paths were opened, at which time the flow rate increased drastically. This change is shown in Figure 8a as a boundary between Periods 1 and 2.

Period 2. During Period 2, the pattern of the infiltration rate is identical to that of the volumetric outflow rates for Locations 2, 3, and 8. This correspondence indicates a direct hydraulic connection between the surface pond and these loca-

tions. The trend of the outflow rates for Locations 8 and 12 is different because they are situated outside of the footprint of the pond. The magnitude of the flow rate increase at different locations along the fracture is quite varied and is accompanied by significant high frequency flow-rate fluctuations.

In general, it can be seen that small variations in the minimum values of the flow rate (between 50 and 100 hours during Period 1) may lead to a wide range of flow rates thereafter. This shows that flow is quite unstable in time and space. The cumulative outflow through fractures was about 60% of the cumulative inflow, indicating that the remainder was presumably imbibed into the matrix, trapped in dead-end fractures, or lost to evaporation.

Figure 8c shows that despite an initial rapid increase in flow during Period 2, the trend of the increase in tensiometric pressure remained essentially the same as that during Period 1. This indicates that the saturation of the matrix continued with time, but the rock was not fully saturated. It is important to note that tensiometers are not able to reflect rapid, high-frequency fluctuations, which were observed for this flow rate. Furthermore, under field conditions tensiometers may not detect a positive water pressure, which is likely to develop in fractures under ponded conditions. This occurs because the porous tip of the tensiometer averages the pressure over the volume of the tensiometer (Finsterle and Faybishenko, 1998), which is connected to both fracture and the adjacent unsaturated rock matrix, resulting in a negative capillary pressure. Despite these limitations, the water pressure trends (Figure 8c), combined with the flow rate data (Figures 8a and 8b), indicate: (1) a rapid fracture saturation just after the beginning of flooding, (2) water imbibition into the matrix, and (3) water flow through fractures.

An analysis of the results of water dripping observed at one of the drip points, Drip Point 6, is shown in Figure 9. A random-looking time variation of water-drip intervals is shown in Figure 9a. The analysis of these data showed that the optimum time delay $\tau = 3$, and the dimension needed to unfold the attractor is $n = 5$. Figure 9b shows a three-dimensional attractor with a definite structure. The spread of points on the attractor reveals the presence of a combination of both chaotic and random components for the frequency of water dripping from the fracture.

7. INTERMEDIATE-SCALE INFILTRATION TEST AT THE BOX CANYON SITE

7.1. Test Design

The field investigation at the Box Canyon site was conducted in order to develop a conceptual model of the geometry and physics of flow and transport at the intermediate scale. We investigated a fracture pattern at the Box Canyon outcrop and conducted a series of ponded infiltration tests at the center of the basalt flow about 30 m away from the outcrop exposure (Faybishenko et al., 1998b; 1999). Because the spacing between the largest basalt column bounding fractures (which

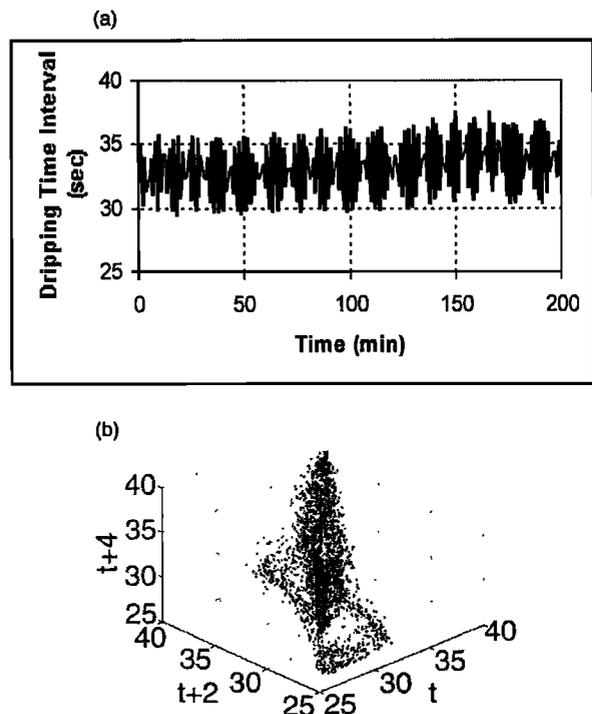


Figure 9. Variations of time-intervals of water dripping: (a) time-series data (only first 200 points are shown), (b) a 2D attractor using $\tau = 2$, which was plotted using 2,000 points.

corresponds to the diameter of largest basalt columns) is as large as 4 - 4.5 m, we constructed a 7 x 8 m pond. We assumed that all types of fractures exist beneath the pond, including at least a few fractures transecting the entire basalt flow. Monitoring of water flow and tracer transport was conducted in 38 vertical and slant boreholes, which were instrumented using tensiometers, suction lysimeters, electrical resistivity (ER) probes, time domain reflectometry (TDR) probes, and thermistors. Water-content distribution was de-

termined using neutron logging, ground penetrating radar, and ER tomography.

7.2. Conceptual Model of the Geometry of the Fracture Pattern

Figure 10 shows a map of the Box Canyon outcrop. In the upper $\sim 2/3$ of the flow thickness, the joint spacing increases with depth. The base of the basalt flow shows an inverted fracture pattern, in which the lower basalt contact contains a smaller fracture spacing than in the center of the flow. At the exposed upper surface, the spacing is as small as 0.3 - 0.5 meters. The upper $2/3$ of the basalt flow has more fractures than the lower $1/3$. In some basalt flows, a region near the center of the flow contains highly fractured rock that does not display the typical columnar structure (Long and Wood, 1986; Tomkeieff, 1940). The fracture map in Figure 10 shows that the central fracture zone can be seen below the infiltration site.

The map shown on Figure 10 was used to construct a 2D conceptual model of the geometry of the fracture pattern (Figure 11). This model is based on the assumption that there are four generations of vertical column-bounding fractures. Starting from the surface, the two smallest basalt columns of size n (1st generation) merge into a column of size $2n$ (2nd generation). Below this, two columns of size $2n$ merge into a column of size $4n$ (3rd generation), and then two columns of size $4n$ merge into a column of the size $8n$ (4th generation). Visual inspection of several basalt outcrops in the field showed that every set of vertical fractures is connected through horizontal vesicular layers and fractures, which are included in the model as well. In addition, Figure 11 shows the presence of some dead-end, or nonconductive, fractures. However, at this time we do not have a quantitative evaluation of dead-end fracture spatial distribution.

7.3. Conceptual Model of Flow

Field Observations. During flooding at the surface, the upper 30-60 cm of vesicular, highly weathered basalt behaves

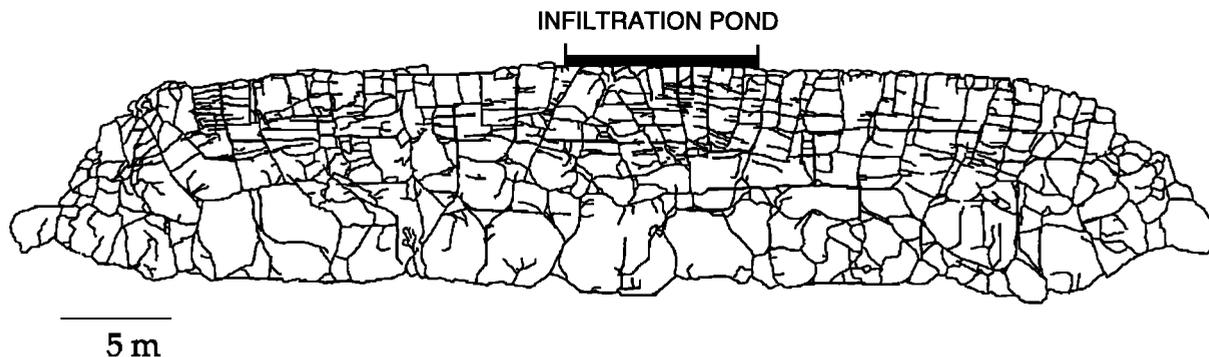


Figure 10. Fracture map of the basalt flow outcrop at the Box Canyon site located about 30 m from the research site. Figure shows that the width of the infiltration pond was about twice as much as the width of the largest basalt columns (Faybishenko et al., 2000).

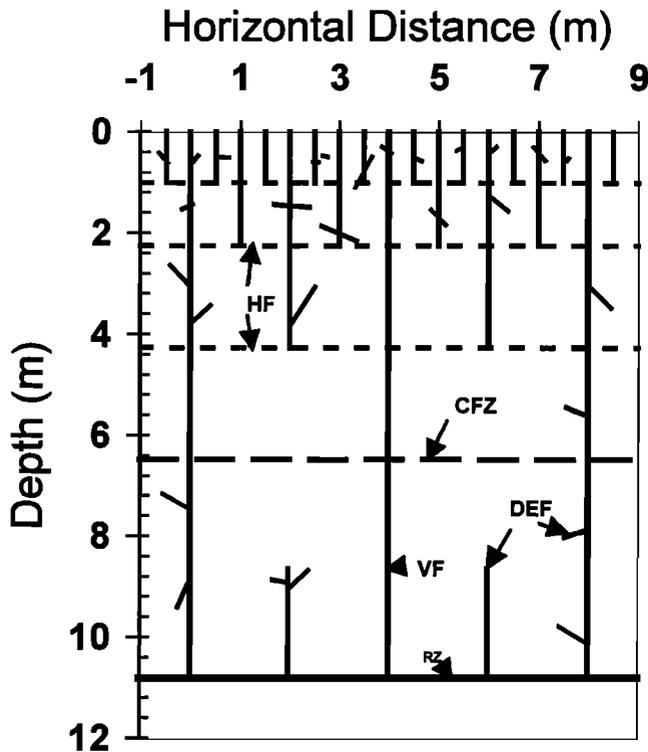


Figure 11. A conceptual model of the fracture pattern showing the vertical (VF) and horizontal fractures (HF), central fracture zones (CFZ), rubble zone (RZ) and dead-end fractures (DEF). The locations of dead-end fractures are arbitrary.

more or less like a uniformly saturated, porous medium. A series of infiltration tests (Faybishenko et al., 2000) showed that the infiltration rate into the subsurface decreased exponentially with time according to Horton's model (Horton, 1940). The near-surface basalt is supposed to be subject to sealing by biofilms, soil particles, and entrapped air that can reduce the fracture and matrix permeability. As the infiltration flux decreases, the fractures below 30–60 cm, which were saturated at the beginning of flooding, may later become desaturated.

Because of the complexity of the fracture network, it is possible to have the effects of both divergence and convergence of flow paths in different parts of the basalt flow. An important factor affecting water flow in basalt is the funneling that develops as a result of the convergence of flow paths caused by the decrease in the number of conducting fractures with depth. At the same time, drastic variations in permeability of fractures and matrix may create a significant divergence of flow paths and a significant dispersivity effect for chemical transport. This process decreases the tracer concentration in the rubble zone, which was investigated during the infiltration tests at Box Canyon (Faybishenko et al., 1999). We assume that dead-end fractures may accumulate contaminants that will diffuse over time into the matrix. However, it is impossible to

identify a priori which fractures will transmit water and contaminants during an infiltration test.

A complex flow geometry was observed using the GPR survey. Plate 1 shows an example of the radar velocities between two boreholes located four meters apart just outside the pond. This figure also shows generalized lithological and fracture logs for these wells. The red color indicates a low radar velocity associated with higher moisture content, and the blue color indicates a higher velocity as affected by lower moisture content. This could indicate either drier conditions or lower porosity in the rocks. This figure shows three horizontal low-velocity zones, presumably wetted zones, located in vesicular basalt and the central fracture zone. We hypothesize that subvertical column-bounding fractures connect these horizontal zones and extend below them to the underlying rubble zone. Unfortunately, individual fractures cannot be resolved by the GPR tomograms because of the small volume of the fractures. Assuming an aperture of 1 mm and a fracture spacing of 2 m, the effective fracture porosity is $1 \text{ mm}/2 \text{ m} = 0.0005$, which is quite small compared to the matrix porosity (~5%). Therefore, we cannot expect such small fractures to show up on the tomogram, even though they are the main conduits for water flow under both saturated and unsaturated conditions.

Field investigations showed that because the number of probes is limited, the results of measurements are usually incomplete and are significantly dependent on the type of instrumentation. For example, tensiometers, ER and TDR provide “point”-type, passive measurements over the length of the sensors, which is usually 5–20 cm, and they detect water only if water contacts the probe (Figure 12). Neutron logging of the moisture content and water sampling with suction lysimeters provide small-scale, near-borehole measurements within distances of 30–40 cm from the borehole. The cross-borehole radar tomography and electrical resistivity tomography measurements, which are effective over a distance of 2–4 m, can provide important information on the relative moisture content within fractured zones, but the resolution cannot provide information about flow in individual fractures. Because information about these flow processes provided by field measurements is limited, we supplemented the field data with mathematical modeling to investigate flow and chemical transport.

Modeling of Water Flow and Tracer Breakthrough Curves.

We generated a relatively simple 2D numerical model using the numerical simulator TOUGH2 (Pruess, 1987; 1991) to simulate water flow and conservative tracer migration underneath the Box Canyon pond (Doughty, 1998). We created a vertical cross-section model of 20 x 20 m in extent, using a regular rectangular grid with a 0.5-m grid spacing (as shown in Plate 2a). The flow properties of the model were assigned using a deterministic approach designed to approximately duplicate the fracture pattern and types of rocks observed at the Box Canyon cliff face (Figure 10). Gridblocks representing

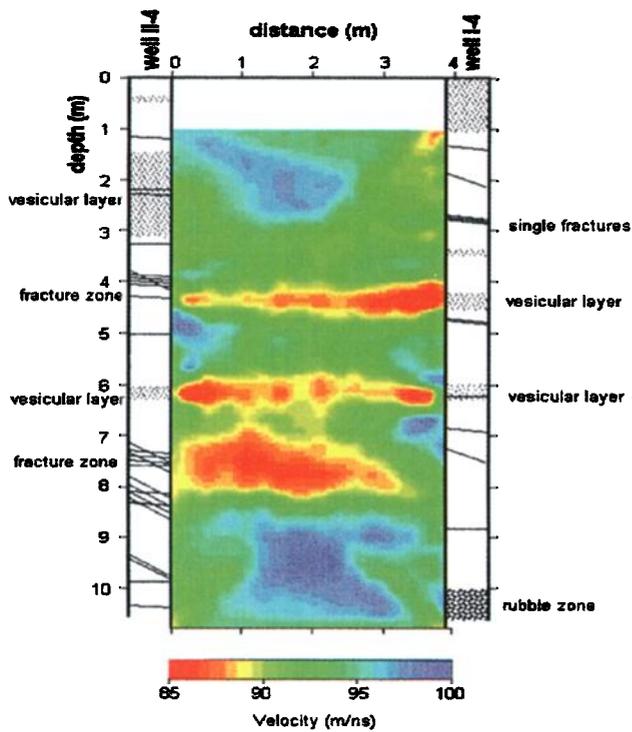


Plate 1. An example of the radar velocities between two boreholes located four meters apart just outside the pond. The red color indicates low radar velocity zones associated with a higher moisture content, and the blue color indicates higher velocity zones with a lower moisture content. The field data were taken in October 1998 by K.H. Williams, and the data inversion was conducted by J. Peterson of LBNL.

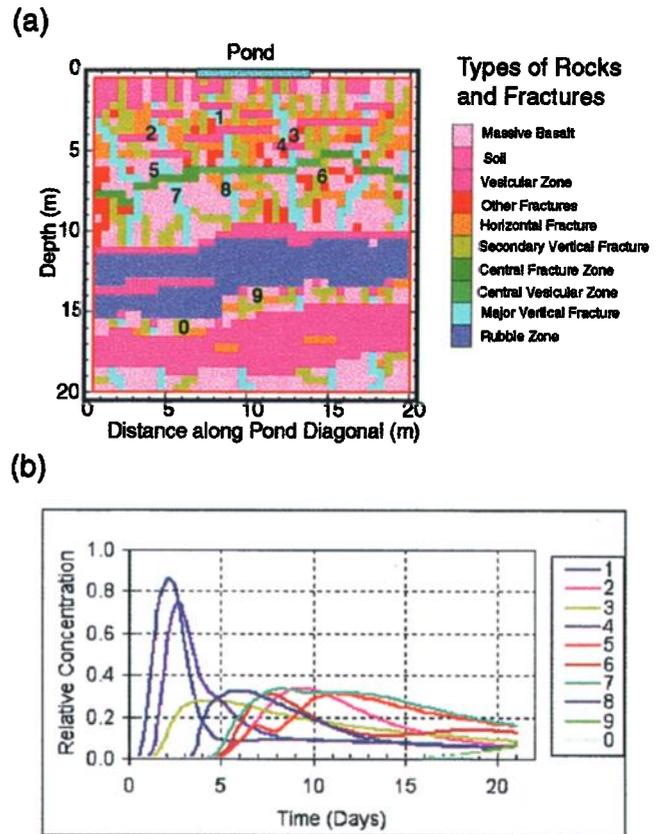


Plate 2. The geometry and types of rocks (a) used for the 2-D modeling of Box Canyon infiltration test, and breakthrough curves (b) obtained for different locations. Location numbers on plate (a) correspond to numbers of breakthrough curves on plate (b).

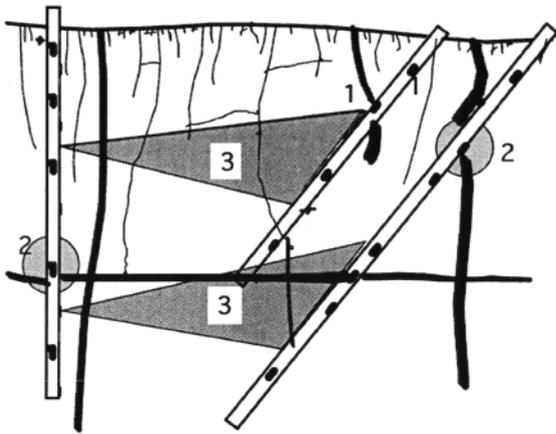


Figure 12. Schematic presentation of types of measurements in fractured rocks using: 1- Point-type, passive, probes (tensiometers, ER and TDR) of a 5-20 cm size, which detect water only if water contacts the probe; 2-Near-borehole moisture content measurements using neutron logging, and water sampling using suction lysimeters within the distance of 30-40 cm from the borehole; and 3-Cross-borehole radar and 3D ER tomography on the distance up to 10-12 m.

vertical fractures are assigned high vertical permeability to allow preferential flow through the fractures, low horizontal permeability to limit fracture-matrix flow, and small porosity to account for the small aperture of the fractures. For grid-blocks representing horizontal fractures, the assignment of horizontal and vertical permeability is reversed.

The processes that were modeled included water and air flow, as well as transport of a conservative liquid tracer. The pond was treated as a constant head and concentration boundary. Plate 2a shows the locations of the monitoring points for tracer breakthrough curves (BTCs). Plate 2b shows a wide range in the behavior of the BTCs. For example, Curves 1 and 4 show sharp peaks, suggesting strongly preferential flow with a small fracture-matrix interaction. Curves 2, 3, 5, and 7 show long tails, suggesting significant matrix diffusion. Curves 4, 5, 6, and 7 show double humps, suggesting a convergence of multiple flow paths. This modeling of breakthrough curves thus confirms the notion that fracture network geometry, along with the type of rocks in which the fractures are imbedded, determines the overall pattern of flow and transport. Results from the modeling of moisture changes (Doughty, 1998) are consistent with field observations and show that vertical preferential flows occur primarily along the column-bounding fractures. A slower imbibition occurs into the surrounding rock matrix. Layers and lenses of vesicular basalt, the central fracture zone, and the rubble zone provide conduits for lateral flow of both water and air, resulting in the wide variety of BTCs seen in Plate 2b. The character of the BTCs does not show a correlation with depth or lithology of the monitoring point. Rather, the BTCs are dependent on the overall geometry

of the fracture pattern, including the fractures above and below the monitoring location.

Summary of the conceptual model of flow. The tree-type of the intra-basalt flow fracture pattern, which can create flow funneling, and the chaotic nature of flow processes discovered on the elemental and small scales support the hypothesis that flow and transport in basalt at the intermediate-scale can also be chaotic. At the same time, the limited number of single-point probes usually available to monitor intermediate scale field experiments cannot be expected to explicitly reveal spatially chaotic flow characteristics, which may occur as a result of a fractal flow-path structure (Barton and Larsen, 1985; Cox and Wang, 1993; Fedder and Jossang, 1995; Hardy and Beier, 1994). Furthermore, for the observations at the intermediate scale, processes all along the flow path from the pond to the monitoring point affect behavior, leading to higher attractor dimensions and precluding unequivocal identification of chaos in time-series data. Therefore, we believe that the optimal way to analyze the field monitoring data is to simulate the geometry of the fracture pattern with deterministic models (such as those shown in Figures 11 and 14a), along with stochastic models of hydraulic parameters (Mantoglou and Gelhar, 1987a,b; Yeh et al., 1985) for the different types of fractures and rocks.

8. LARGE-SCALE INFILTRATION TEST AT THE RADIOACTIVE WASTE MANAGEMENT COMPLEX

8.1. Test Design

The LSIT, which was conducted south of the RWMC at the INEEL, was probably the largest infiltration test ever conducted in the United States. It was designed to assess flow and transport phenomena at the scale of several basalt flows, separated by rubble zones, between the surface and a sedimentary interbed at a depth of 55 m. An area of approximately 26,000 m² was flooded for a month using water that was pumped from the underlying Eastern Snake River Plain aquifer and then piped into the 183 m diameter infiltration basin (Wood and Norrell, 1996). After 6 days of flooding, several short-lived radioactive tracers, as well as a NaBr tracer, were added to the infiltration basin. The total volume of water supplied to into the pond was 134 million liters. After mixing was accomplished, no water was added to the basin for 11 days while the tracer pulse infiltrated. The total duration of the infiltration test was 7 months. Subsurface migration of infiltrating water and tracers was monitored by several techniques (as described below).

The monitoring well network consisted of 70 wells combined in 16 clusters, as shown in Figure 13. Given the heterogeneous nature of the fractured vadose zone, it was anticipated that we would be able to detect preferential flow and lateral spreading of water along rubble zones, as well as the formation of perched water bodies above the sedimentary interbeds. The arrangement of wells within 100 m of the infiltration ba-

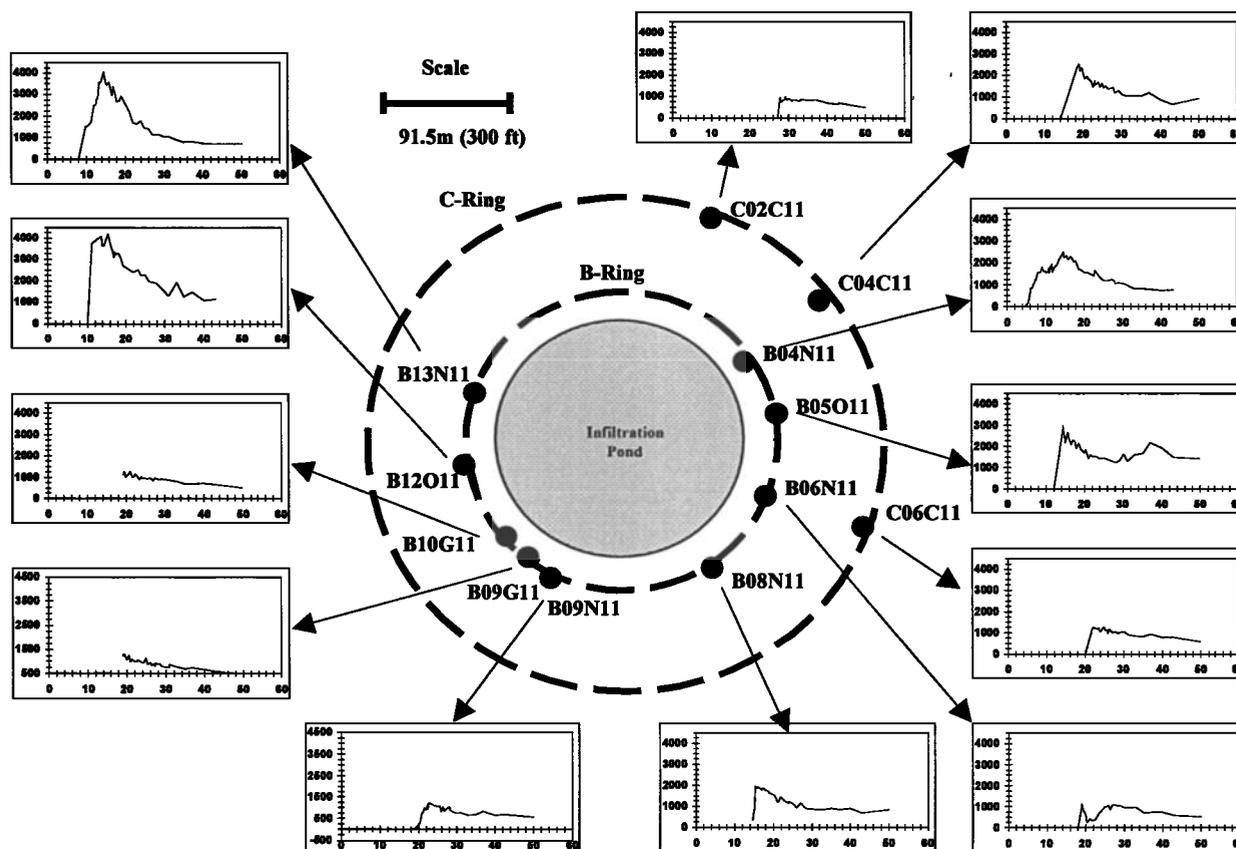


Figure 13. General layout of the infiltration pond and the borehole monitoring system during the LSIT, and breakthrough curves of Se-75 (horizontal axis is time in days since the tracer was introduced in the basin, and vertical axis is activity of Se-75 in pCi/L) determined in boreholes screened in a perched water zone.

sin (in and around the infiltration basin) provided a means of monitoring water and tracers flowing vertically beneath and laterally away from the infiltration basin. Monitoring the subsurface water movement began immediately after of flooding started using multiple monitoring systems. The following types of data were collected: (a) neutron logging to determine changes in the moisture content of rocks in the near vicinity of the monitoring wells, (b) gamma spectroscopy to track the movement of the gamma-emitting radioactive tracers, (c) water sampling to determine water and tracer breakthrough curves, and (d) perched water level measurements.

8.2. Test Results and Conceptual Model of Flow

Despite the expectation of some lateral flow, no water or tracer was observed in boreholes beyond the footprint of the infiltration pond except for perched water that formed on top of the sedimentary interbed at a depth of 70 m. The perched water moved down the slope of the interbed through a widespread rubble zone immediately above the low permeable sedimentary interbed. The fact that infiltrating water was not observed in partially saturated fractured basalt outside the ba-

sin suggests high permeability of intra-basalt vertical fractures and rubble zones sufficient to transmit all water downward. Another reason for unsaturated flow below the infiltration basin is that a near-surface, low permeable layer (crust) restricted flow into the vadose zone from the surface. Thus, the LSIT showed that in addition to the effect of an intra-basalt fracture pattern (studied at the intermediate-scale), we have to take into account the geometry and permeability of inter-basalt rubble zones. Furthermore, low-permeability sedimentary layers can create perched water zones that induce a lateral spread of water and contaminants.

Figure 14 shows the arrival times for water at different depths of the vadose zone, which was determined using neutron logging. This figure also includes the arrival times into open boreholes screened at the depth of 55 m, indicating the incipient formation of perched waters. The left dashed line in Figure 14 shows the first arrival time for water at different depths. From this figure, the velocity of the downward distribution of the wetting zone is from 10m/day (at a depth of 6m) to 2 m/day (at a depth of 50m). Smaller scales of observation would have to consider local hydrogeologic features that may

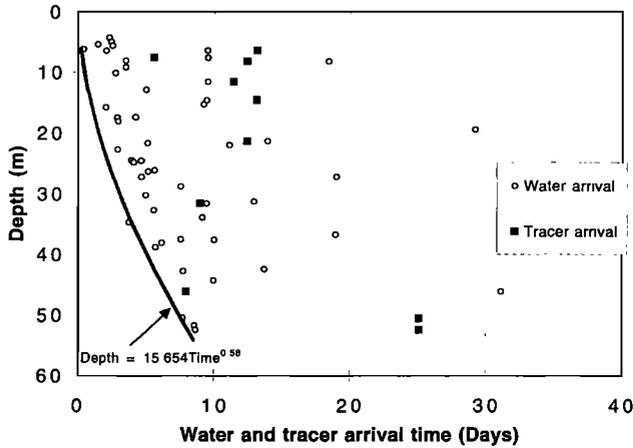


Figure 14. The relationship between the time of water arrival (determined from neutron logging) and the Se-75 tracer arrival and depth during the LSIT. Note that the tracer arrival is calculated from the time the tracer was introduced into the basin.

account for wide departures from the average wetting zone travel time of 5 m/day determined by Bishop and Porro (1995).

Figure 15 shows a variety of tracer breakthrough curves observed at different locations in the vadose zone during the LSIT. One can see a conventional BTC near the surface, multi-modal curves as affected by migration from different fractures, and no tracer detected at some points. Note that although some locations became saturated quickly after the beginning of flooding, the tracer had not arrived after a month. This non-appearance can be attributed to changes of water-flow pathways over time. Water may flow into dead-end, non-conductive fractures easily, but because it cannot continue flowing out of the fractures, no subsequent tracer can flow into these fractures by advection. Tracer can enter these fractures only by diffusion or flow through the surrounding basalt, both of which are relatively slow processes. Thus, a combination of the water and tracer experiments can be used to identify zones of preferential flow and locations of dead-end, nonconductive fractures.

9. DISCUSSION

The complex geometry of basalt flows with their intra-basalt fracture networks and wide variations in the permeability of the dense basalt and highly fractured rubble zones have raised concerns over how flow and contaminant transport in such systems should be characterized. The of geological and hydrogeological complexity of such systems, as well as the uncertainty of measurements, a hierarchy of scales, methods, and models should be used to characterize flow and transport phenomena in fractured basalt.

Elemental scale investigations are needed to study in detail the physical nature of spatial and temporal characteristics of flow processes in a single fracture or a block of the basalt ma-

trix. Small laboratory cores, fracture replicas, or point-size measurements collected under field conditions must be used in these investigations. The size of measurements is from a few centimeters to 10-20 cm. Laboratory investigations of flow in a single fracture in basalt have revealed the phenomenon of film flow (Tokunaga and Wan, 1996) as well as water channeling and meandering along narrow pathways on the fracture surface (Su et al., 1998). Laboratory experiments using capillary tubes inserted into fracture replicas have shown that water does not flow uniformly along a fracture surface, but flows intermittently with dripping occurring along flow channels. The dripping and meandering within the fractures generates nonperiodic fluctuations in water pressure, which are not stochastic in nature. The pressure fluctuations can be described using deterministic-chaotic models with a certain stochastic component that is not a dominant factor controlling the system behavior. The results of studies on the elemental level can be used to develop a better understanding of dripping from a

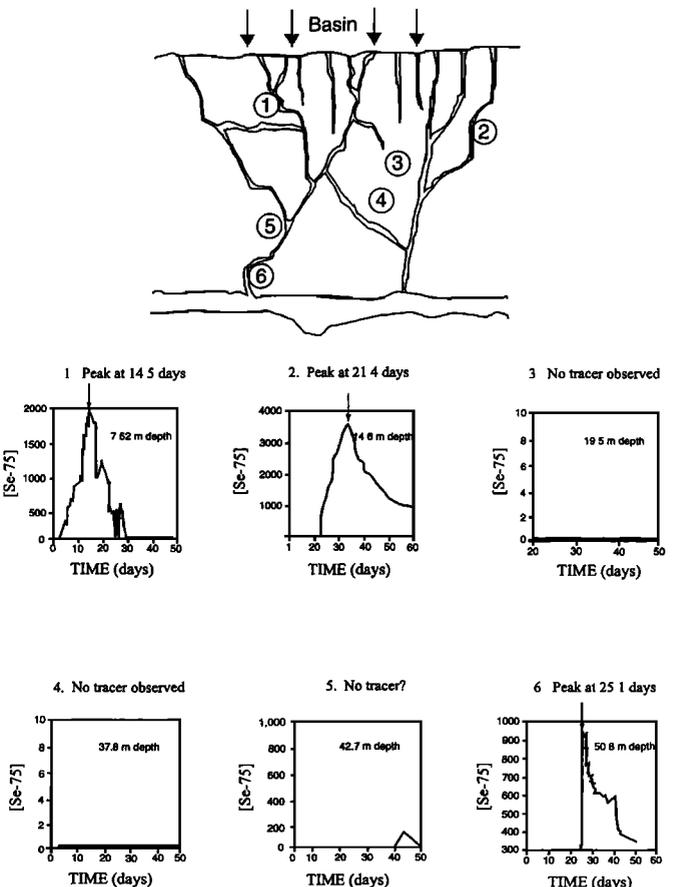


Figure 15. Types of breakthrough curves for Se-75 activity (pCi/L) for several locations in vadose zone below the LSIT basin. Horizontal axis is time in days since the trace was introduced in the basin (from Wood and Norrell, 1996).

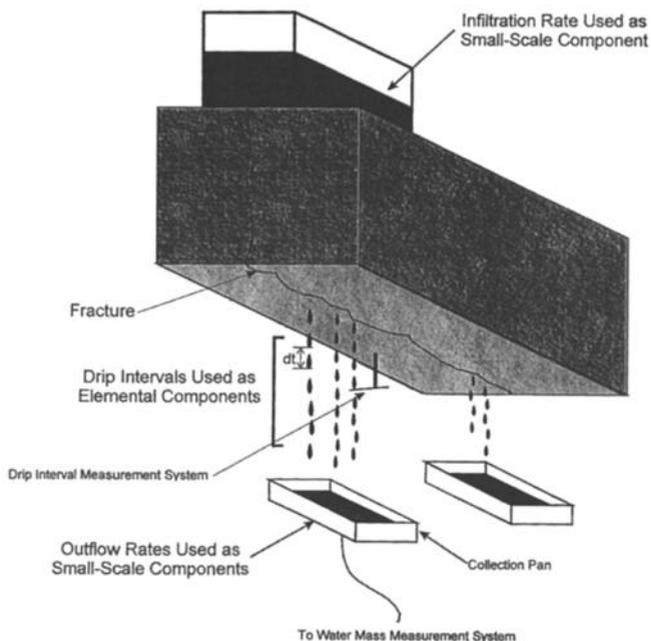


Figure 16. A conceptual model of a field infiltration test showing water dripping, which can be considered as an elemental component, and a collection of water into pans that can be considered as a small-scale component.

fracture under field conditions in boreholes, tunnels, caves, and other underground openings. However, laboratory studies of fractured rocks have certain limitations, because we cannot determine how to combine the individual processes in characterizing the total system.

Small-scale investigations involve a volume of rock within a single basalt flow with one or a few fractures over an areal extent of approximately 0.5-1 m². Field experiments on this scale conducted by Nativ et al. (1995) and at the Hell's Half Acre site (Podgorney et al., 1997; 1999) confirmed that the fracture flow includes dripping. Figure 16 illustrates a conceptual model of flow through a block of fractured basalt dripping phenomena at many locations along the fracture. These locations are not stable and meander with time. The intervals of water dripping from a single location can be described using a chaotic model with some random component. At the same time, the volumetric outflow rates combined from several dripping locations exhibit spatial and temporal instability, with primary low frequency fluctuations and secondary high-frequency fluctuations. The fracture-matrix water interaction and entrapped air data (Persoff and Pruess, 1995), which are presumably the main factors affecting the spatial and temporal flow instability, were also identified in several studies (Glass et al., 1991; Lenormand and Zarcone, 1989; Nicholl et al., 1993).

With the increasing scale of the field investigations, the combination of many degrees of freedom may lead to attrac-

tors of such high dimension that the overall behavior of the system does in fact look stochastic (despite the deterministic chaotic nature exhibited on the elemental scale). Contrary to laboratory conditions, water pressures cannot be measured so accurately under field conditions because single tensiometers, as used conventionally, provide volume-averaged pressure measurements for the liquids within porous cup (Finsterle and Faybishenko, 1997). Thus, the averaged pressure measurements do not exhibit the high-frequency fluctuations that actually take place because of dripping, as is observed in both the field and laboratory. However, a comparison of water pressures measured using tensiometers installed in both the fracture and matrix can be used to determine the general trend of the rock saturations. The most important practical application of these small-scale investigations is to study the physics and models of flow taking into account the fracture-matrix interaction.

Intermediate-scale investigations are conducted within the volume of rock involving the intra-basalt flow fracture-network over an areal extent of approximately 10-100 m². A series of ponded infiltration tests at the Box Canyon site showed that during flooding of the surface, the upper 30-60 cm of vesicular, highly weathered basalt acts more or less like a uniformly saturated porous medium. The infiltration rate decreases with time exponentially. The fractures that were saturated at the beginning of flooding may become desaturated thereafter. Important factors affecting the decrease in the infiltration rate into fractured basalt are plugging of the fractures by soil particles, biofilms, and entrapped air, as well as a funneling effect resulting from a convergence of flow paths as the number of conducting fractures decreases with depth. Vertical flow occurs through subvertical, column-bounding fractures, which interconnect the horizontal layers of vesicular basalt, the central fracture zone, and the rubble zone. These highly permeable zones provide conduits for lateral flow of both water and air and create a divergence of flow paths leading to a significant dispersivity for contaminant transport.

We assume that the presence of dead-end fractures, which may trap and retain contaminants, will promote long-term diffusion of these materials into the matrix. Unfortunately, individual fractures cannot be resolved by existing field hydrogeological and geophysical methods, because of the small volume in the pore space of the fractures. Because single probes can easily miss a zone of preferential flow, field measurements provide limited information about the flow processes. In this case, modeling is needed to investigate flow and chemical transport.

Modeling showed the importance of taking into account coupled processes of two-phase (water and air) flow (Doughty, 1998). Modeling also revealed that a different BTC behavior exists that reflects strongly preferential flow with fracture-matrix interaction and suggests the convergence of multiple flow paths. The BTC at a given location depends on the entire flow path from the pond to that location and is

strongly affected by the overall geometry of the path and lithology along the fracture pattern.

The practical application of the intermediate-scale investigation is to understand the flow processes underneath single tanks such as those at the RWMC in Idaho and at Hanford.

Large-scale investigations involve a volume of rock containing several basalt flows and the rubble zones between them over an area that usually exceeds 1,000 m². At this scale, we can study flow in the fracture networks and regional hydrogeological processes, which are affected by the vertical and horizontal rubble zones, as well as sedimentary interbeds. The limited number of single probes that were available to monitor the LSIT cannot explicitly reveal all the spatial and temporal flow characteristics of the vadose zone. However, the creation of the perched water zone above the sedimentary interbed at a depth of about 55 m is a clear indication of flow through the vadose zone. The wide range of the times (from 10 to more than 30 days) for the water appearances at a depth of 55 m indicates there was a nonuniform flow of water through the vadose zone. The difference in the water and tracer arrival times can be attributed to changes in the flow pathways with time.

The practical application of the large-scale investigation is to understand the flow processes and develop models in order to study the distributed flow and contaminant transport problems that exist under the RWMC and elsewhere at INEEL or in the tank farms at Hanford.

10. CONCLUSIONS

The laboratory and field infiltration tests have all shown that a typical feature of flow in fractured rocks is channeling that occurs at all scales of investigation, including individual fractures, the intra-basalt fracture network, and the inter-basalt rubble-zone network. However, the instrumentation used in laboratory and small-scale field conditions (in particular, to record dripping phenomena) is not practical for use at the larger field scales. Field measurements of flow characteristics in fractured rocks using single probes (such as tensiometers) are uncertain, because the locations of the probes in relation to the flow paths are not precisely known, and these probes can only provide an average value for the fracture and matrix hydraulic characteristics.

An important feature of flow in the basalt vadose zone is that the hydraulic system includes both unsaturated and saturated rocks. During flooding at the surface, the saturated zones have a limited and local extent within flow channels in the fractures and vesicular zones. Single probes, which cross the saturated fractures, also intersect the matrix, and hence, these probes measure an averaged water pressure in the fracture-matrix system. However, it is difficult to separate the contribution of the fracture from that of the matrix (Finsterle and Faybishenko, 1997). Using available monitoring techniques under field conditions, we cannot perfect our knowledge of initial conditions; we can only measure approximate values for the different parameters (pressure, moisture content, tempera-

ture, concentrations) or determine the ranges of these parameters.

Because a variety of natural conditions affect the hydraulic processes in unsaturated fractured basalt, field and laboratory investigations in the vadose zone should be conducted on four different scales: elemental, small-scale, intermediate-scale, and large-scale. We find that, at each scale of investigation, different conceptual models for flow and transport phenomena must be used to explain the observed behavior. Because different methods of measurement are needed, one can obtain data to use in creating models describing different flow processes with no apparent scaling principles evident. Instead, a hierarchy of models is needed to discriminate between the observed flow phenomena at each of the different scales.

Fluid flow in fractured basalt of the vadose zone can be considered a nonlinear dynamic process, in which the behavior, both temporally and spatially, may be chaotic (Sposito and Weeks, 1997; Weeks and Sposito, 1997). The chaotic nature of flow results from nonlinear processes and the strong spatial and temporal variations in moisture content, hydraulic conductivity, and fracture connectedness. As a result, a nonlinear system in fractured basalt can have small variations in flow parameters that may lead to significant variations in the predicted results. The dissipative nature of the system implies that its phase-space volume decreases with time, leading to the formation of strange attractors that characterize the range in which the flow parameters are expected to change. The dynamics of such systems are sensitive to the initial conditions. The response of such systems may include a stochastic component that it is not necessarily a dominant factor in the overall system behavior. If the stochastic component is not dominant, then a stochastic analysis will not provide useful information.

We also find that under field conditions with a limited number of single-probe measurements, we can detect neither the spatial nor temporal chaotic variations of the flow parameters, and therefore, one must use conventional (i.e., non-chaotic) stochastic or deterministic methods to describe flow and transport processes. If the stochastic component is not a dominant factor, then a stochastic analysis will provide incorrect answers and should be replaced by a chaotic analysis. If the stochastic component is significant (or if the phase-space dimension is so large that the dynamics look stochastic), then a stochastic analysis is the most appropriate tool to use. Because the system exhibits sensitivity to initial conditions, we can predict only the range in which the flow rate is expected to change, but not the exact flow rates. Where elemental and small-scale components are involved, the flow data can be analyzed using methods of nonlinear dynamics. Where intermediate and large-scale components are involved, a combination of deterministic and stochastic methods of flow analysis can be used.

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